

# PC VIII: Femtochemistry and/or Photochemistry



# Organization

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## Physikalische Chemie VIII: Spektroskopie II

- Some exercises with *Mathematica*
- Exercises 2 weeks
- Debriefing: Thursday 8.00-10.00 in room 34-K-01 or 13K24 (through 13 K 26), every second week, start Oct. 4
- Return exercises Wednesday before 12.00
- Computer-Exam
- Script (password PCseven7)

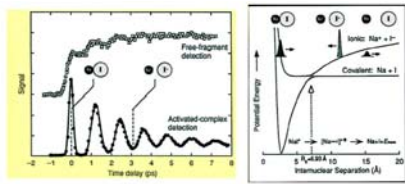
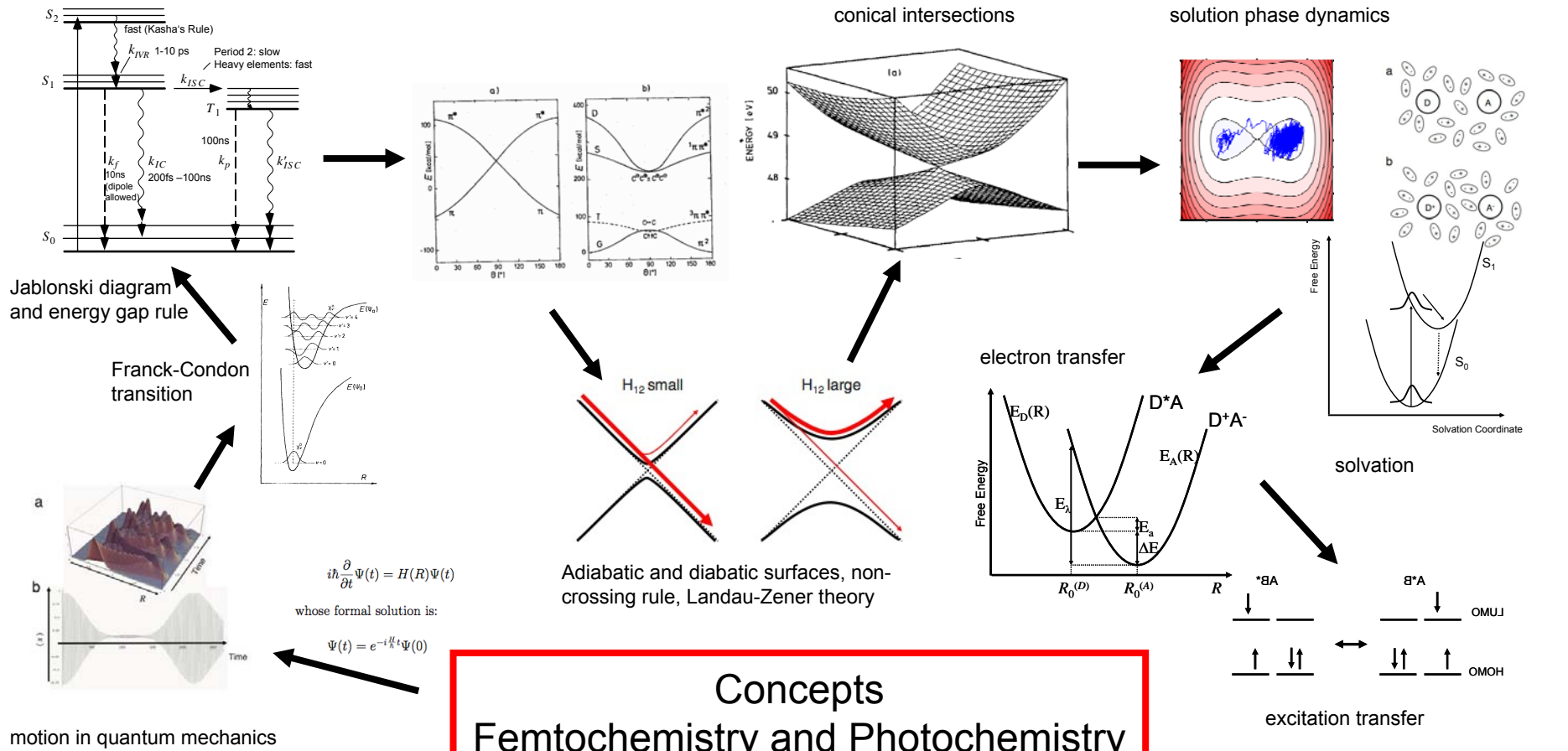
Tutor: Fivos Perakis                      34 K 30



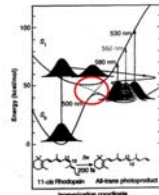
# Femtochemistry: Basic Concepts

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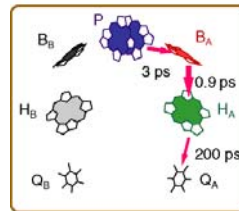
- Examples of Photochemical Reactions
- Experimental Methods
- Motion in Quantum Mechanics: Wavepackets
- Franck-Condon Transition
- Jablonski Diagram, Fermi Golden Rule, Energy Gap Law
- Prototype Potential Energy Surfaces
- Non-Crossing Rule, Avoided Crossings, Conical Intersections
- Born Oppenheimer Approximation and its Breakdown
- Adiabatic and Diabatic Surfaces
- Mixed Quantum-Classical Methods, Landau Zener Theory
- Solvation
- Electron Transfer Theory
- Excitation Transfer: Exciton- and Förster Transfer



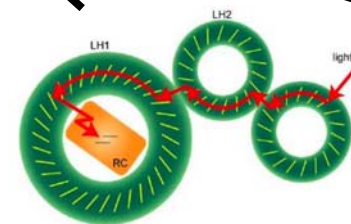
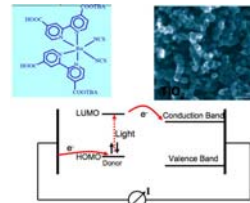
gas-phase chemistry



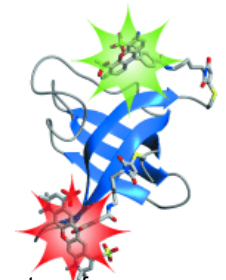
vision



natural and artificial photosynthesis



coherent and incoherent excitation transfer





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# Femtochemistry

Nobel Prize 1999

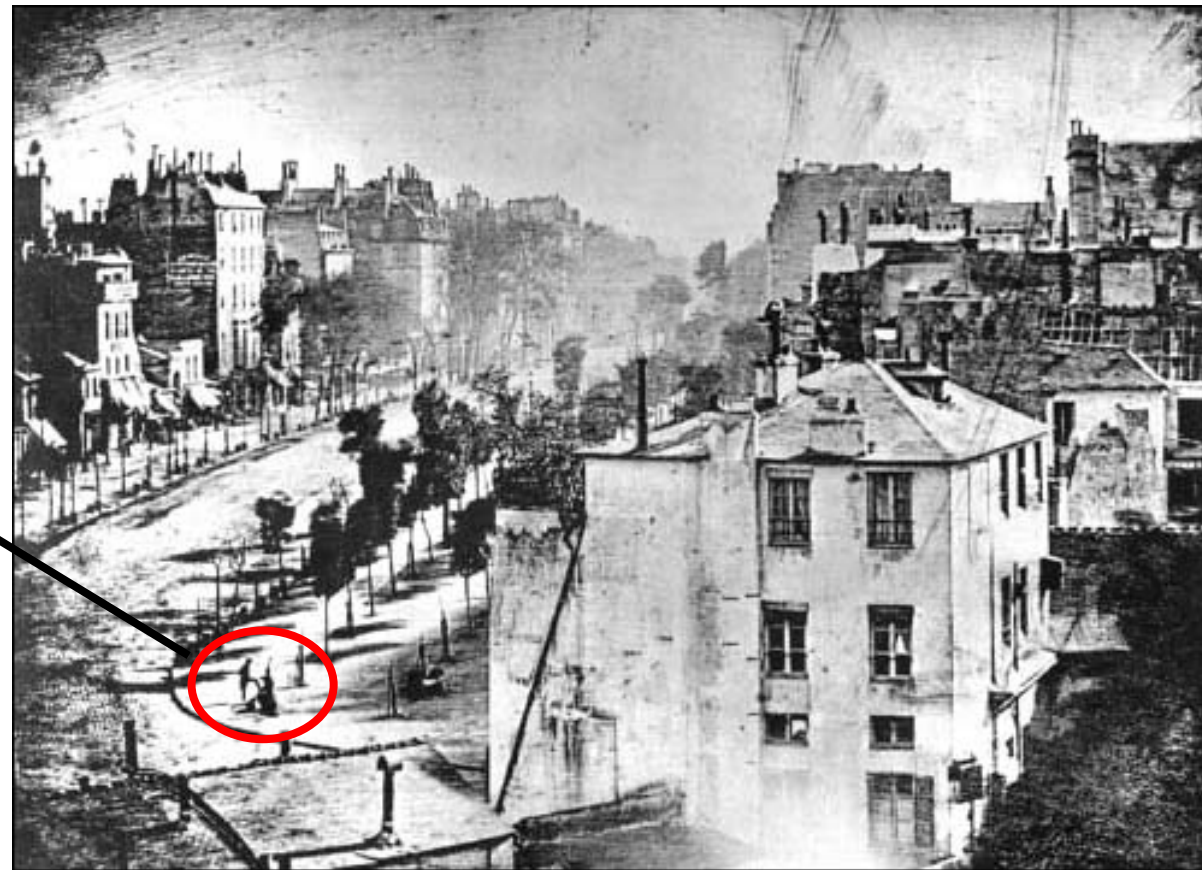
Ahmed Zewail



# The First Time-Resolved Photo

**Louis Jacques Mande Daguerre, 1839**

**Exposure Time: 10-20 min**

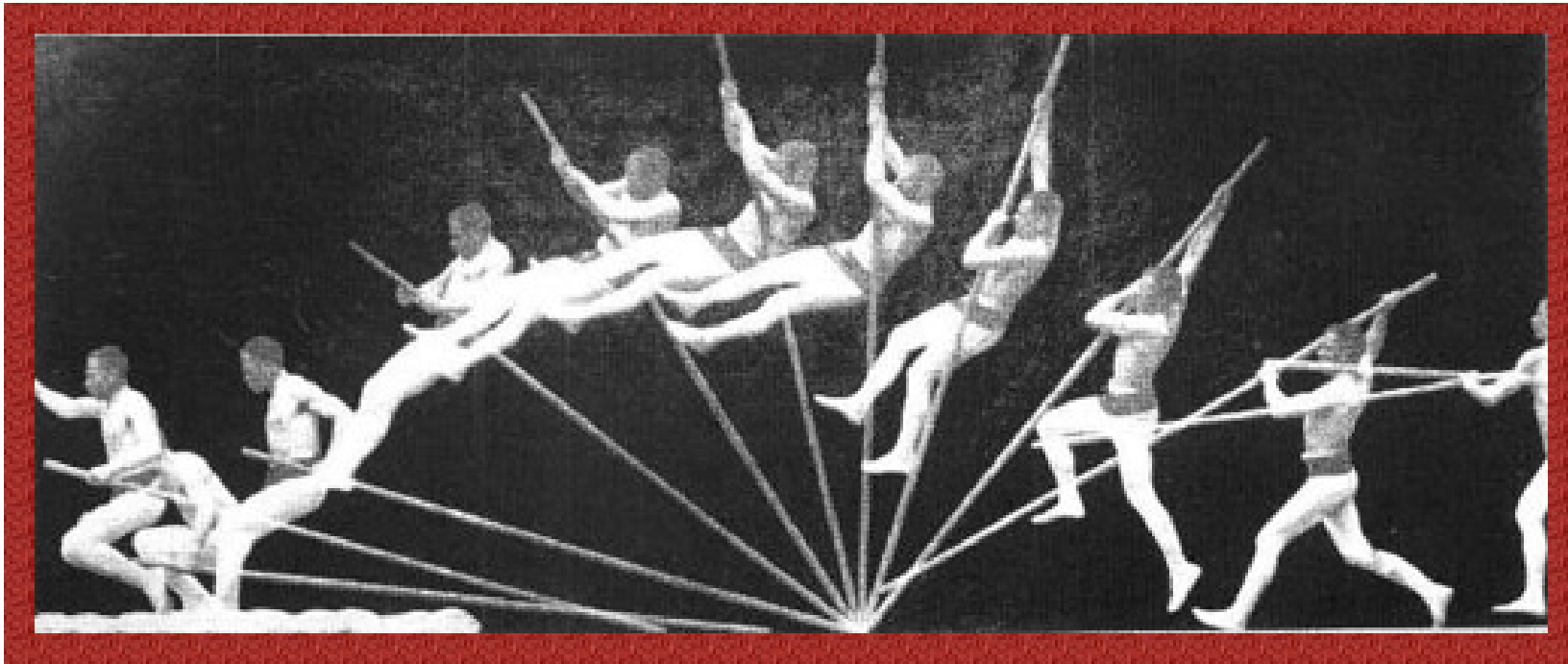


<http://www.rleggat.com/photohistory/history/daguerr.htm>



# Stroboskop

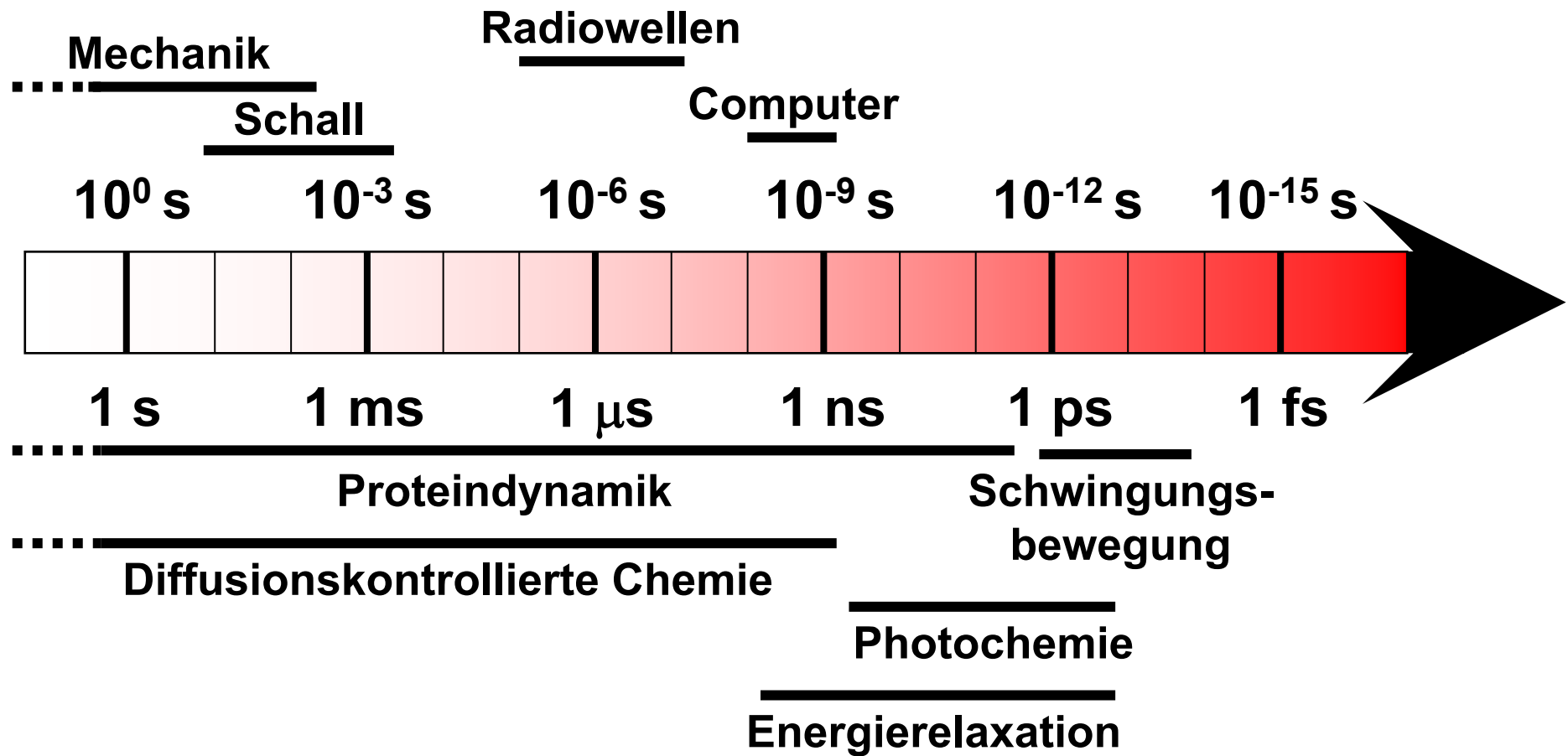
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**Zeitauflösung: 1 ms**  
**ca. 1880**



# Zeitpfeil







# 100 Femtosekunden

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**Lichtgeschwindigkeit: 300.000 km/s**

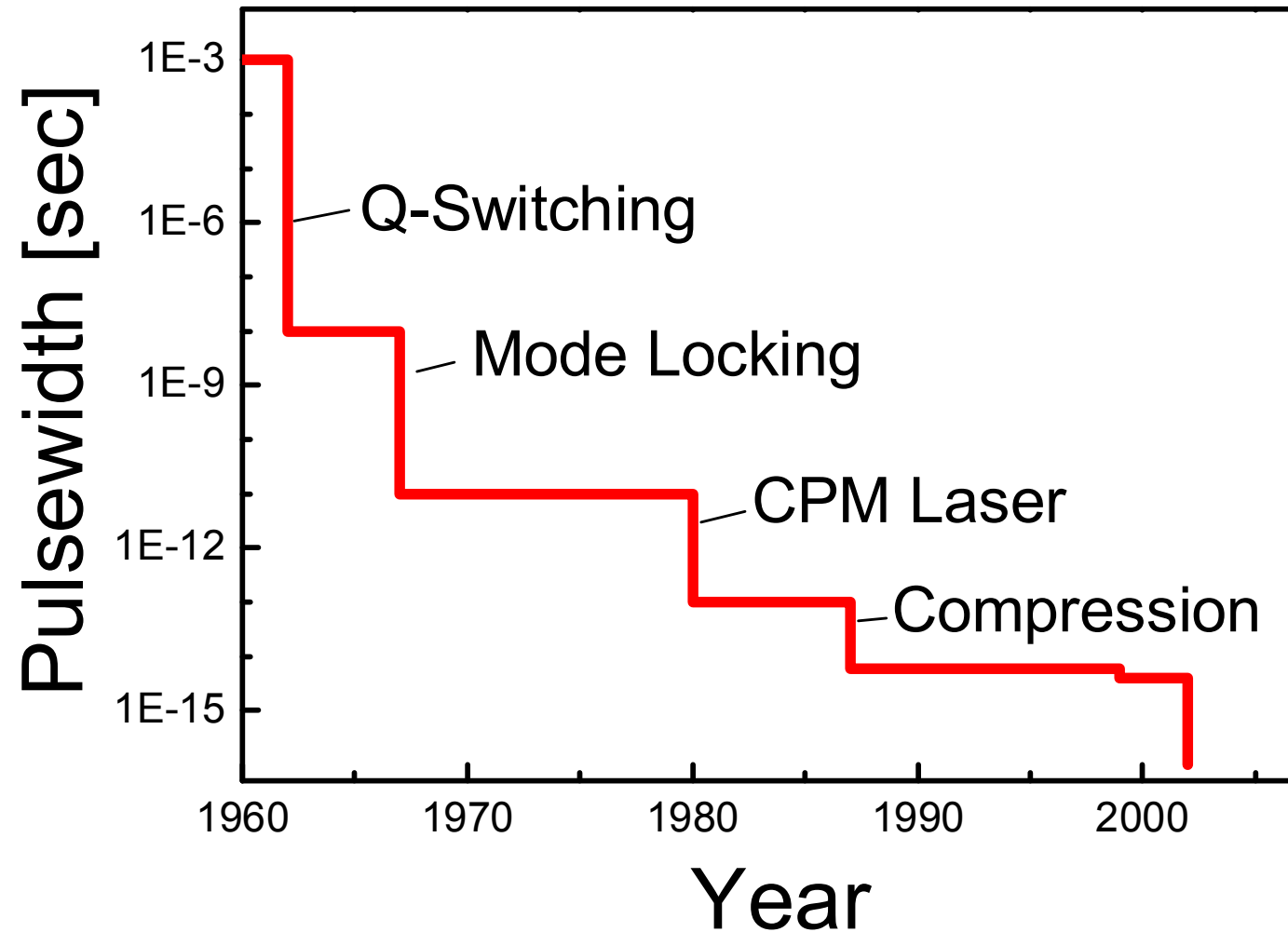
**1 s:            Erde → Mond**

**8 min:        Erde → Sonne**

**100 fs:        Dicke eines dünnen Blatt Papiers**

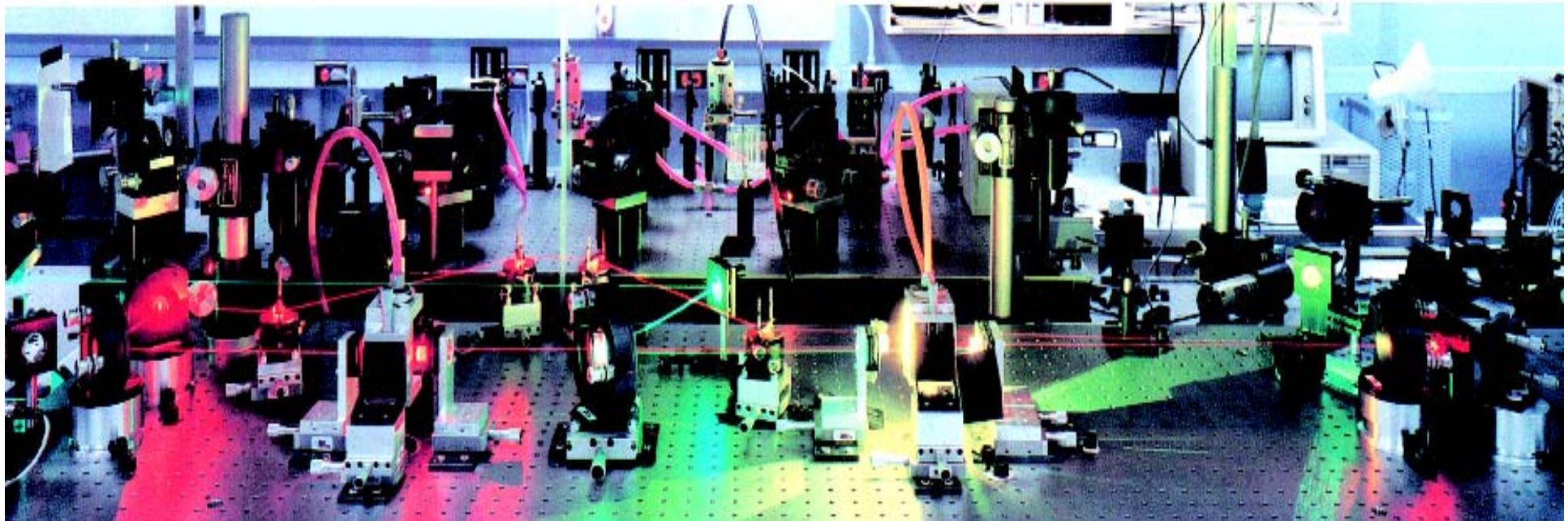


# Short Pulses with Lasers





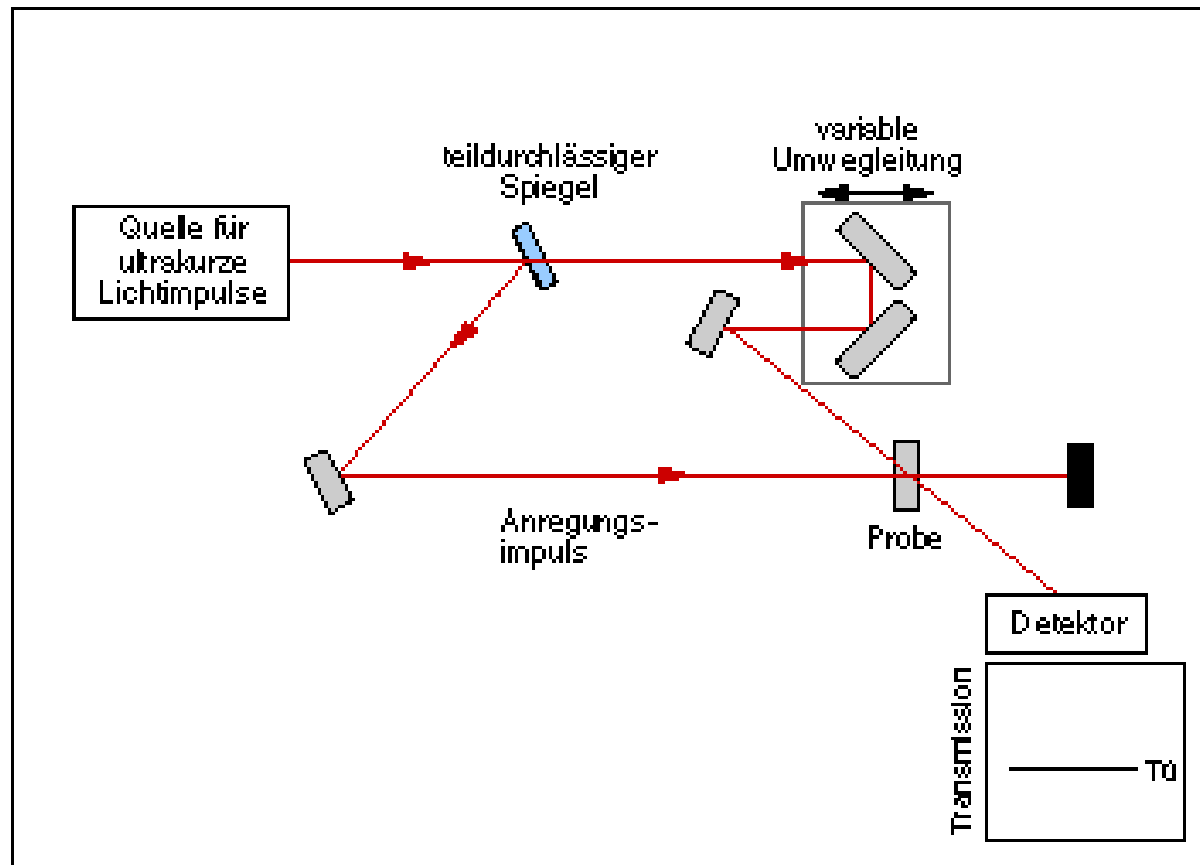
# Femtosecond Lasers



**CPM Laser 1980**

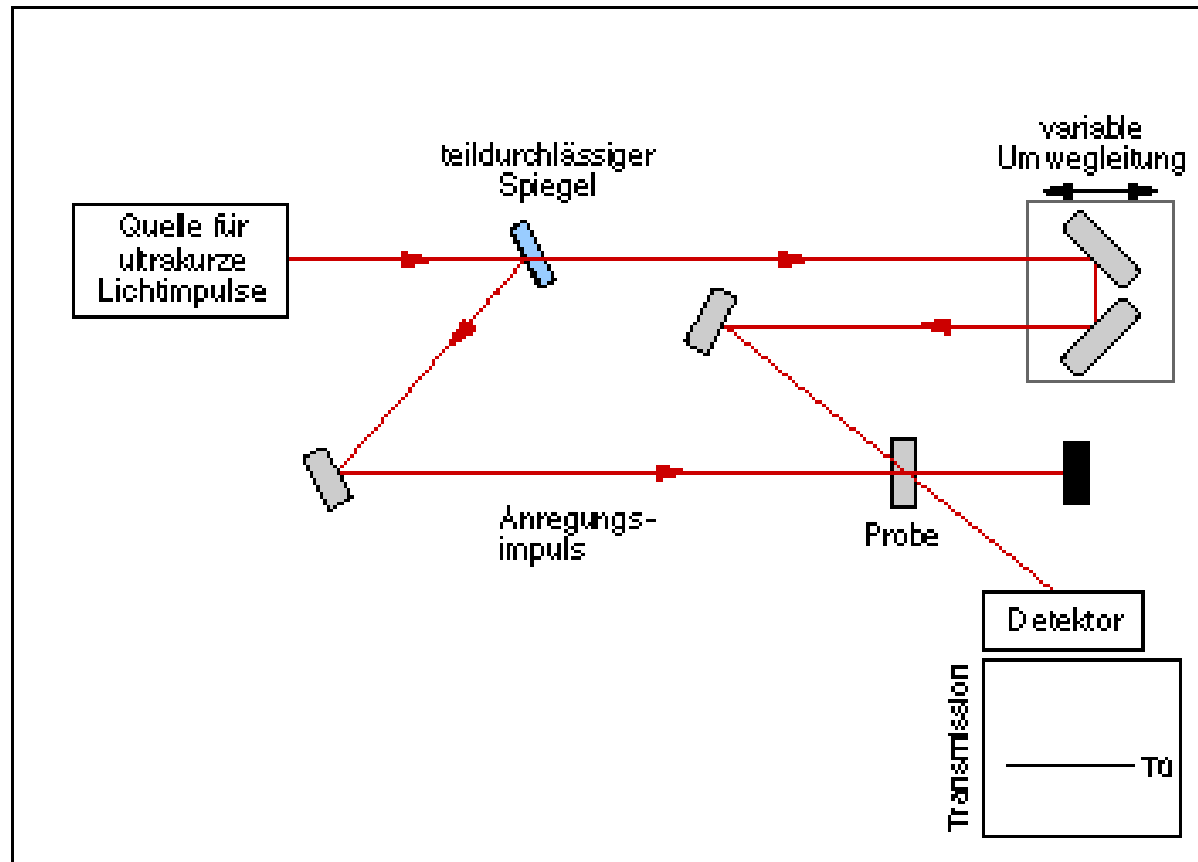


# Pump-Probe Spectroscopy



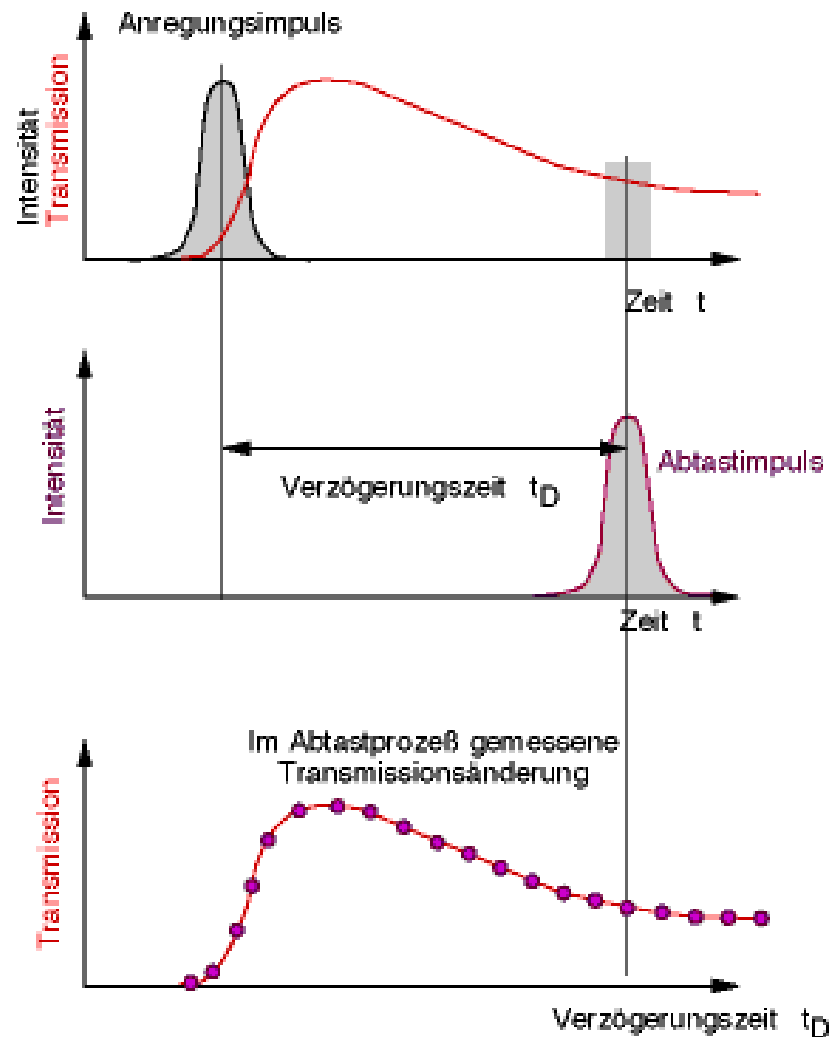


# Pump-Probe Spectroscopy



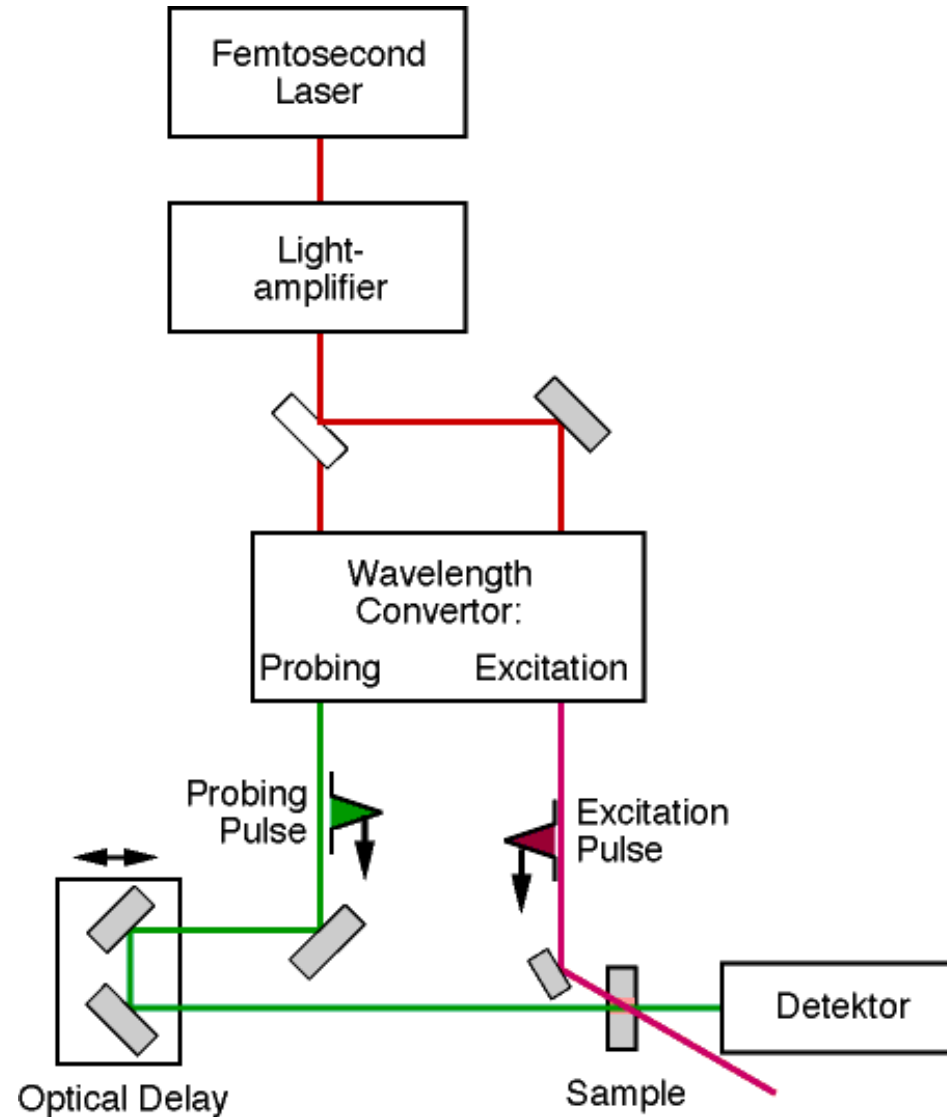


# Pump-Probe Spectroscopy





# Pump-Probe Spectroscopy





# Femtochemistry: Basic Concepts

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- **Examples of Photochemical Reactions**
- Experimental Methods
- Motion in Quantum Mechanics: Wavepackets
- Franck-Condon Transition
- Jablonski Diagram, Fermi Golden Rule, Energy Gap Law
- Prototype Potential Energy Surfaces
- Non-Crossing Rule, Avoided Crossings, Conical Intersections
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- Solvation
- Electron Transfer Theory
- Excitation Transfer: Exciton- and Förster Transfer





# Photochemical Reactions in Nature: Isomerization of Bacteriorhodopsin

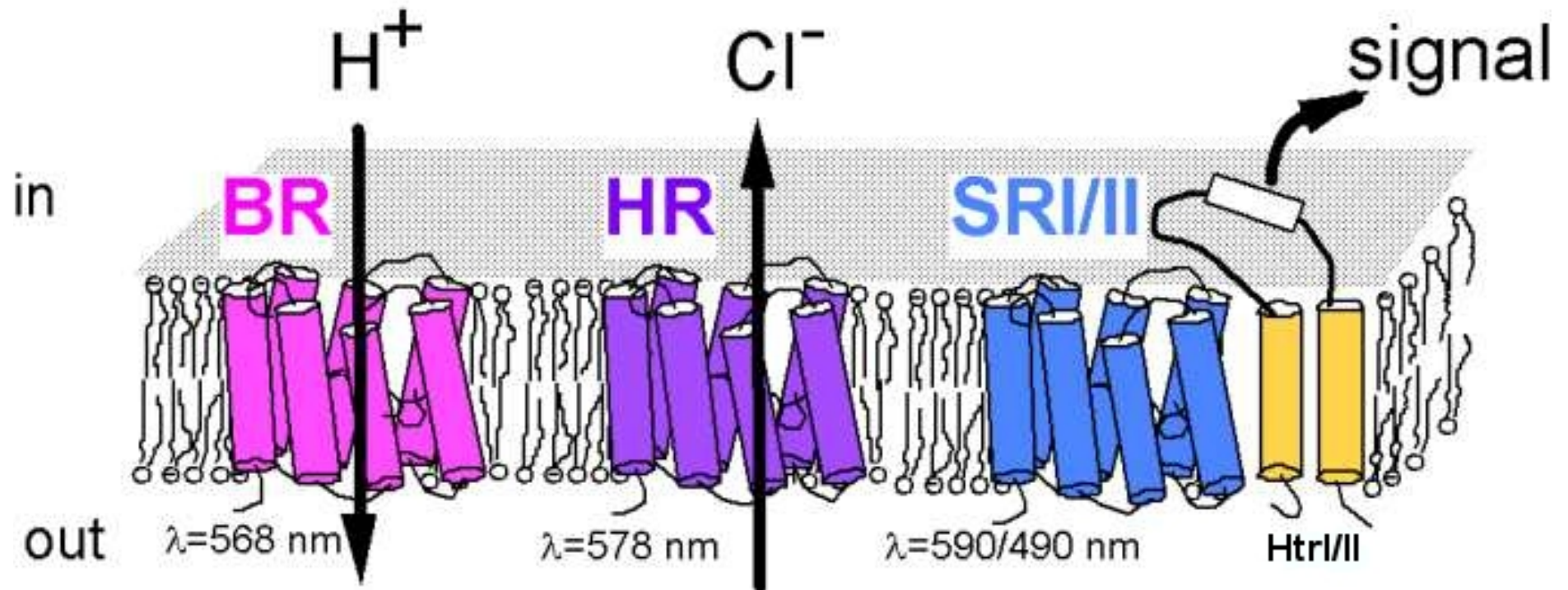
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Wikipedia, Halobacteria in the salt lake Chokrak (Ukraine)

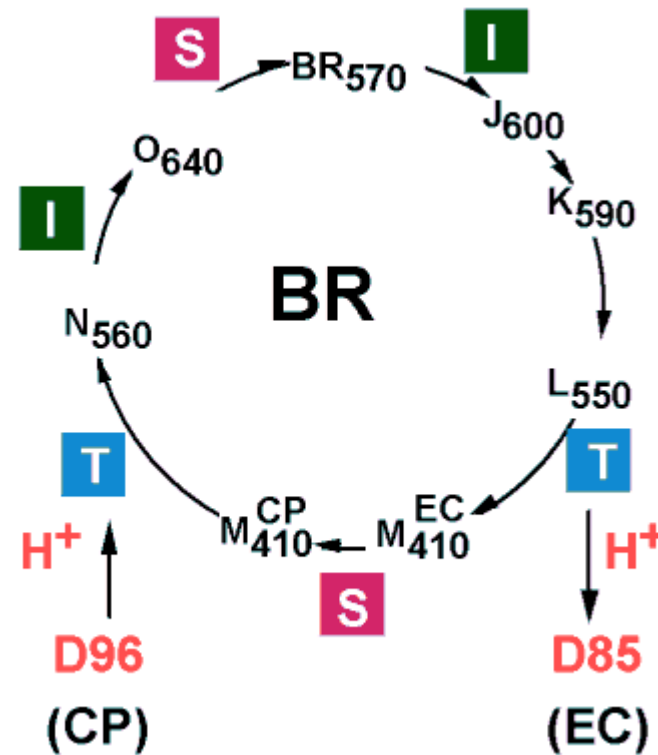
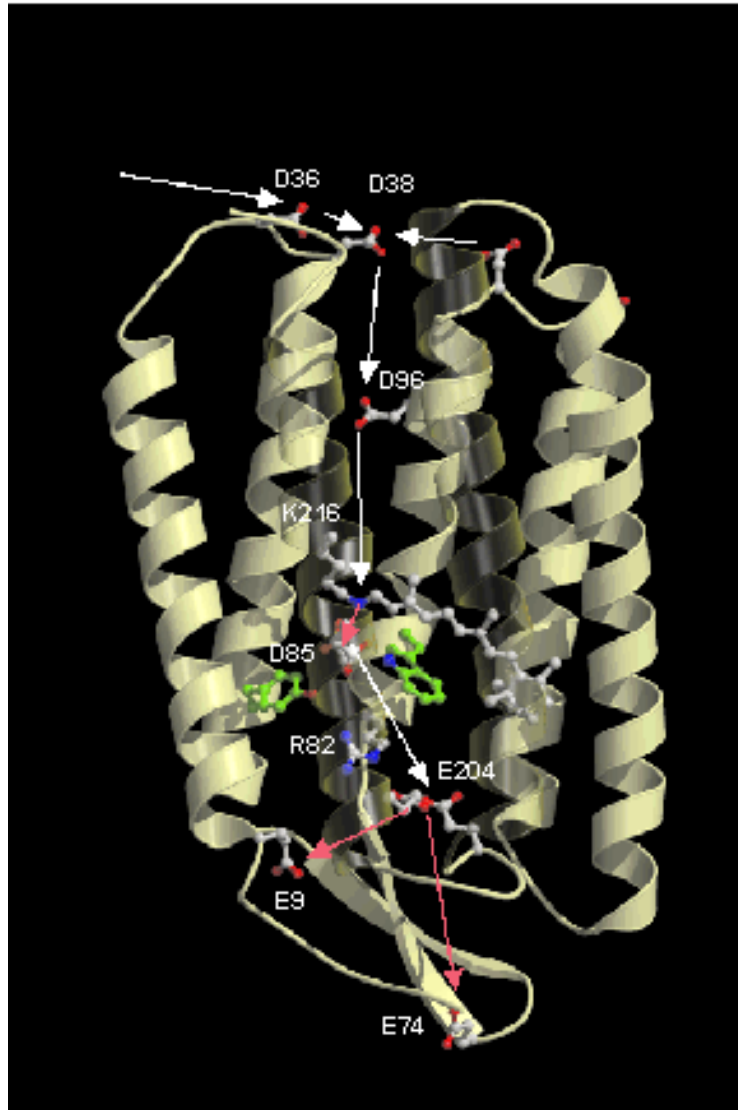


# Photochemical Reactions in Nature: Isomerization of Bacteriorhodopsin



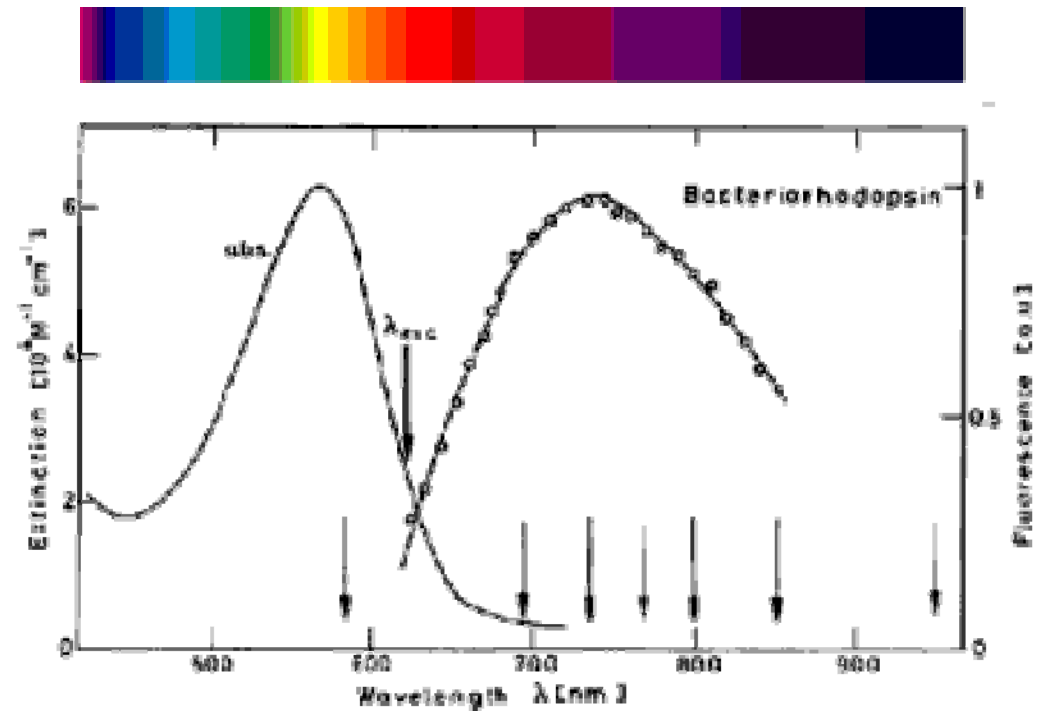
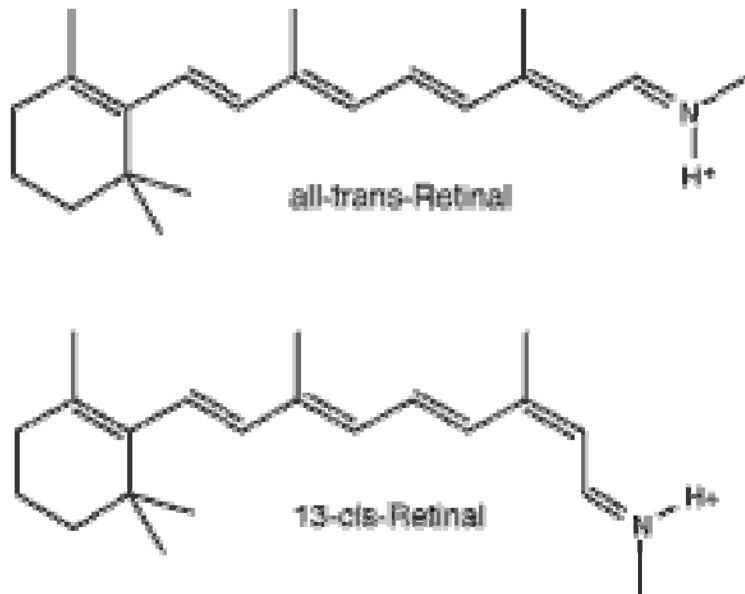


# Photochemical Reactions in Nature: Isomerization of Bacteriorhodopsin





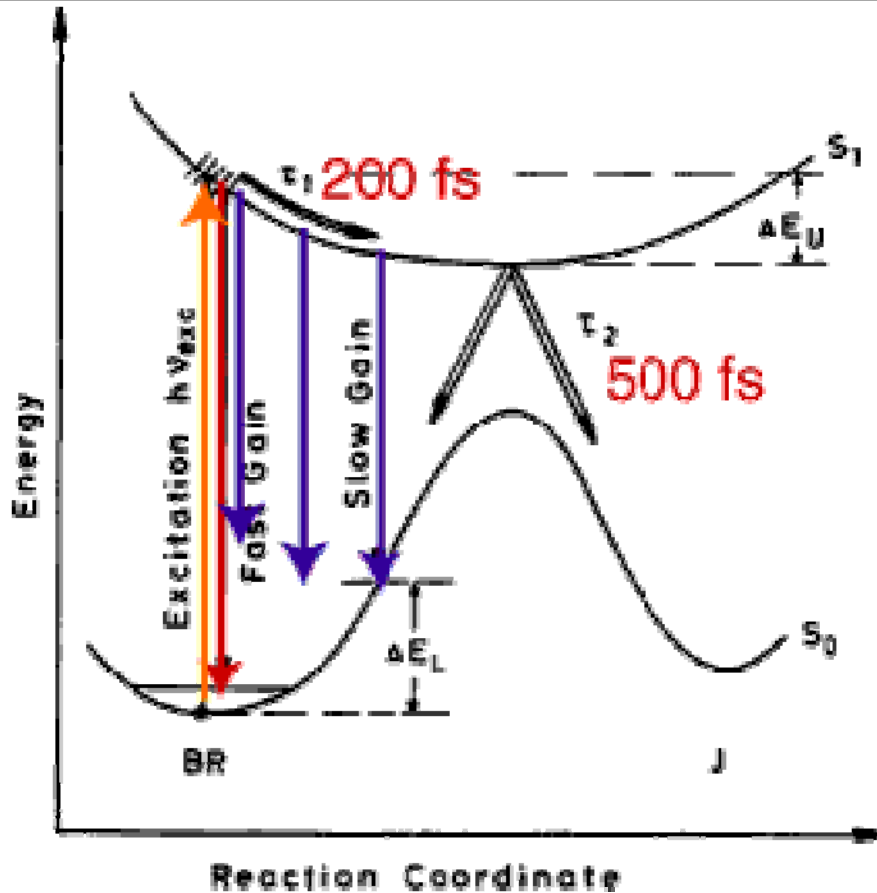
# Photochemical Reactions in Nature: Isomerization of Bacteriorhodopsin



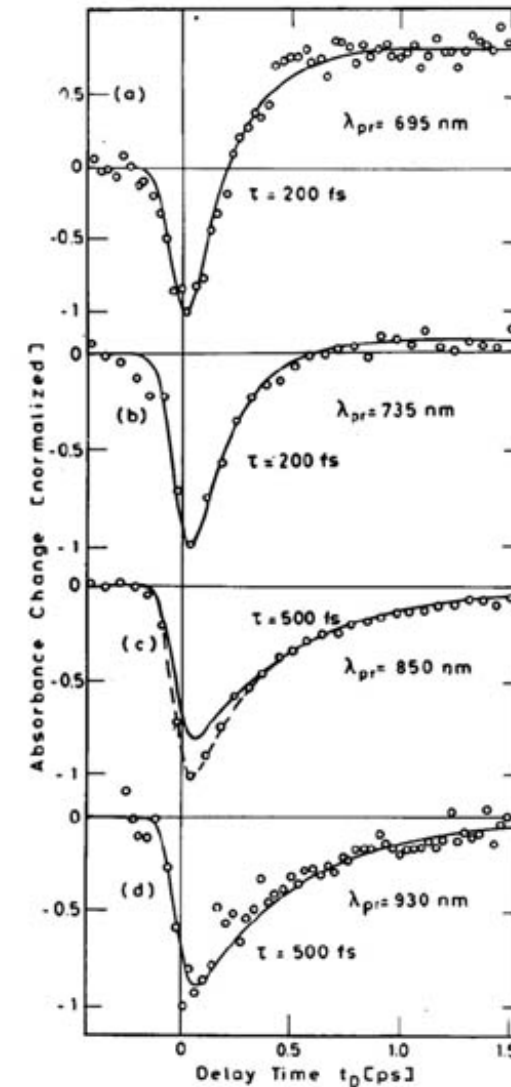
Dobler, W. Zinth, W. Kaiser, D. Oesterhelt *Excited-state reaction dynamics of Bacteriorhodopsin studied by femtosecond spectroscopy*. Chem. Phys. Lett. 144 (Feb. 1988) 215



# Photochemical Reactions in Nature: Isomerization of Bacteriorhodopsin



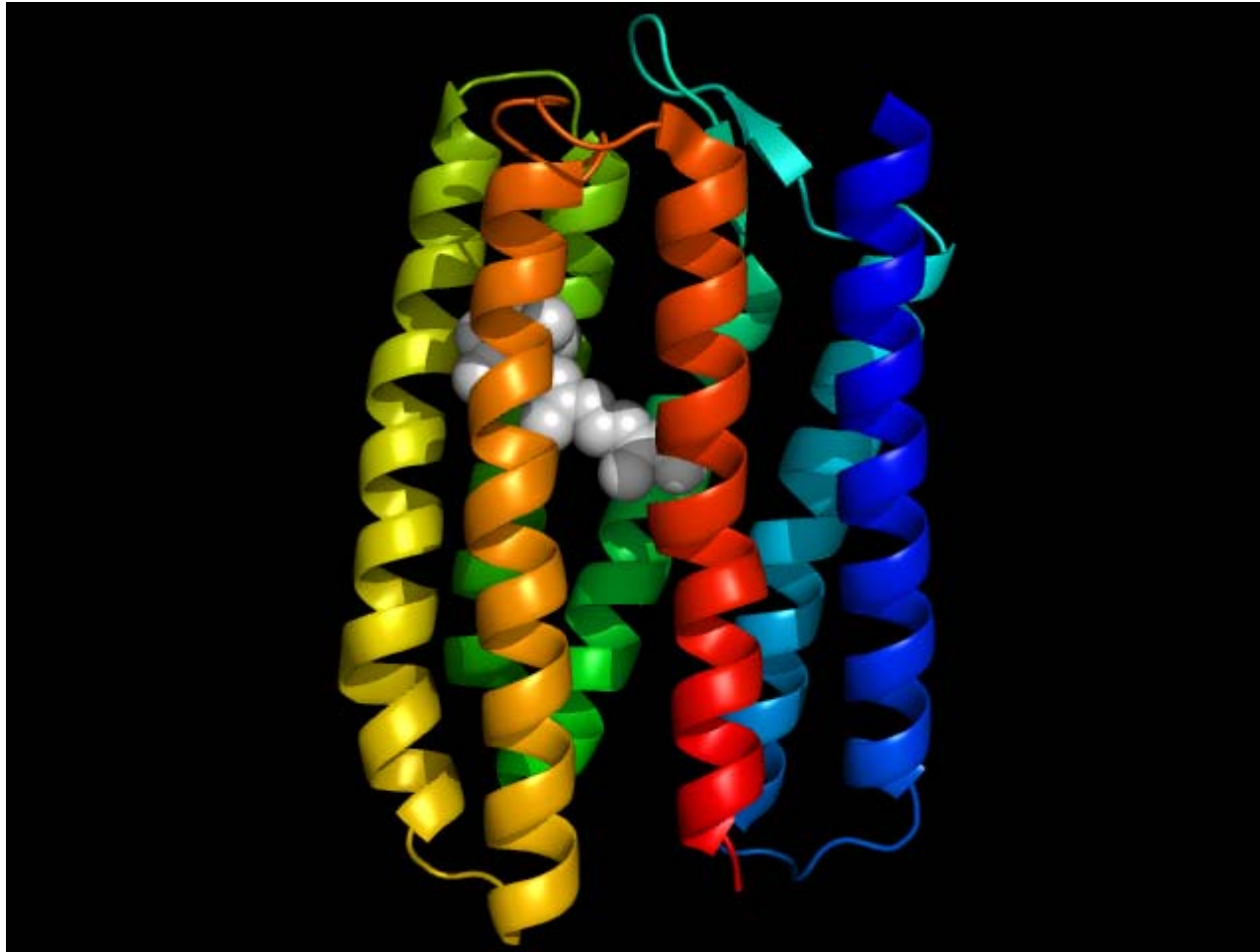
Dobler, W. Zinth, W. Kaiser, D. Oesterhelt  
*Excited-state reaction dynamics of Bacteriorhodopsin studied by femtosecond spectroscopy.* Chem. Phys. Lett. 144 (Feb. 1988) 215





# Vision: Isomerization in Rhodopsin

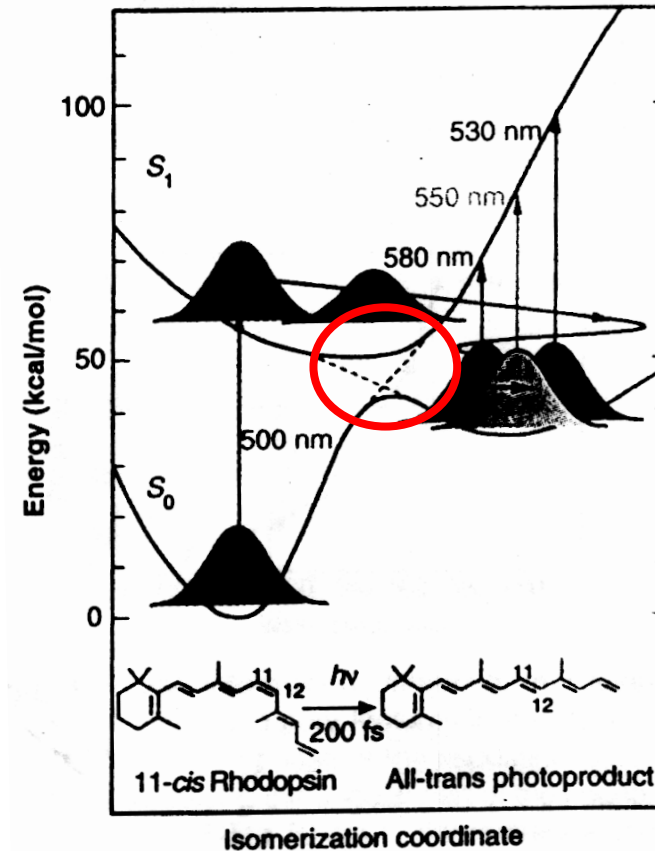
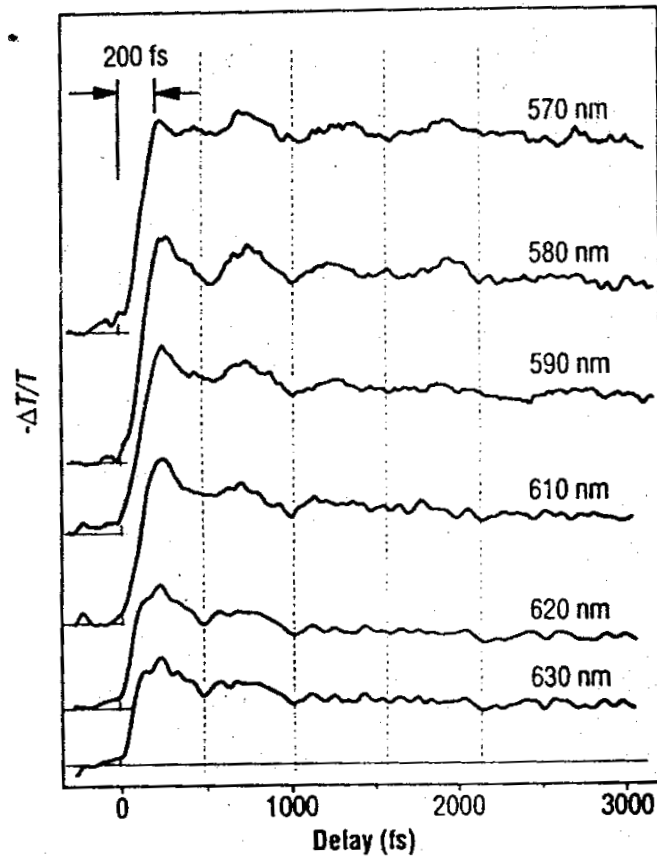
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movie



# Photochemical Reactions in Nature: Isomerization of Rhodopsin



Q. Wang, R. W. Schoenlein, L. A. Peteanu, R. A. Mathies, C. V. Shank,  
Science 266 (1994) 422



# Photochemical Reactions in Nature: Electron Transfer in Photosynthesis

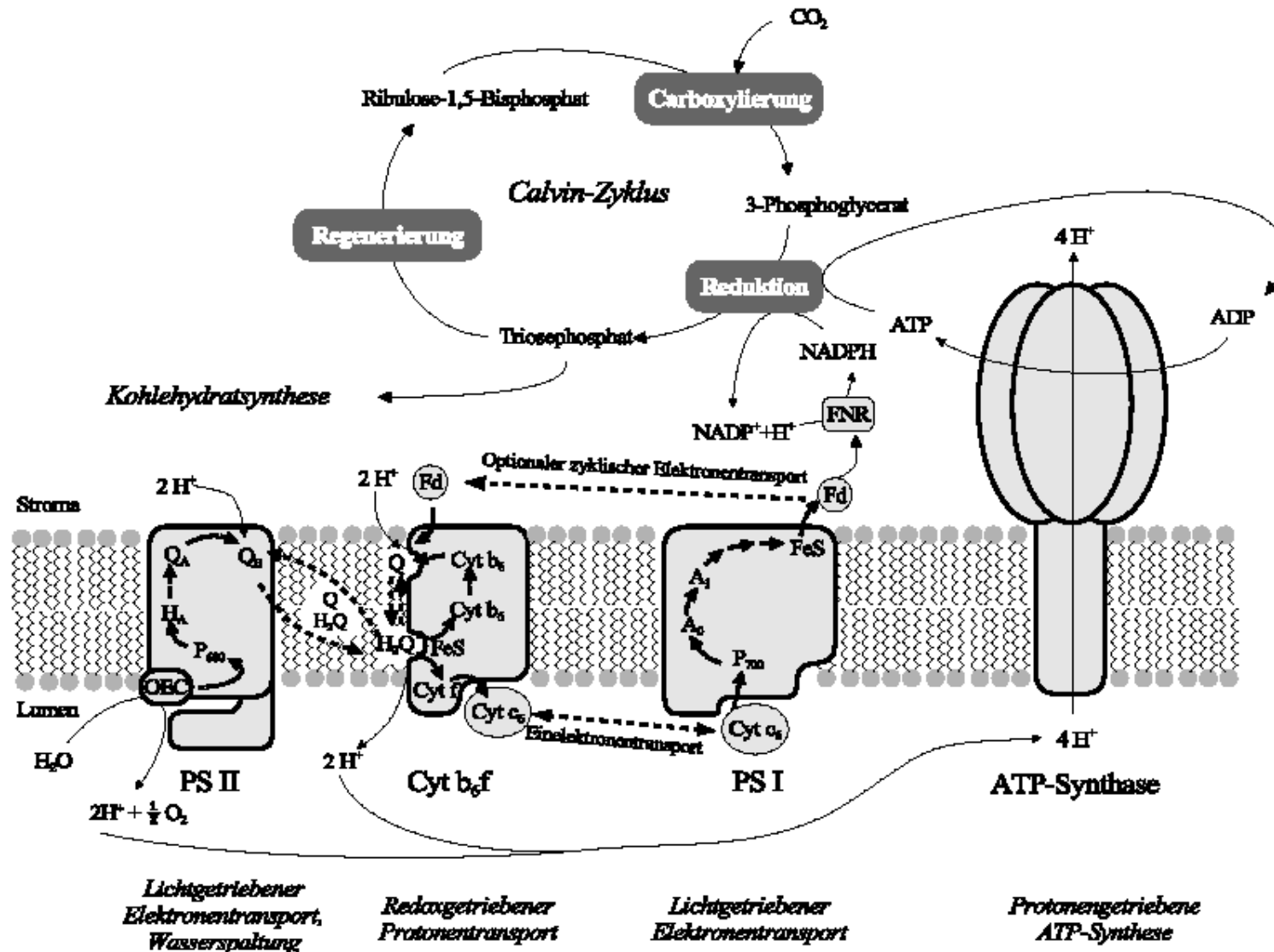
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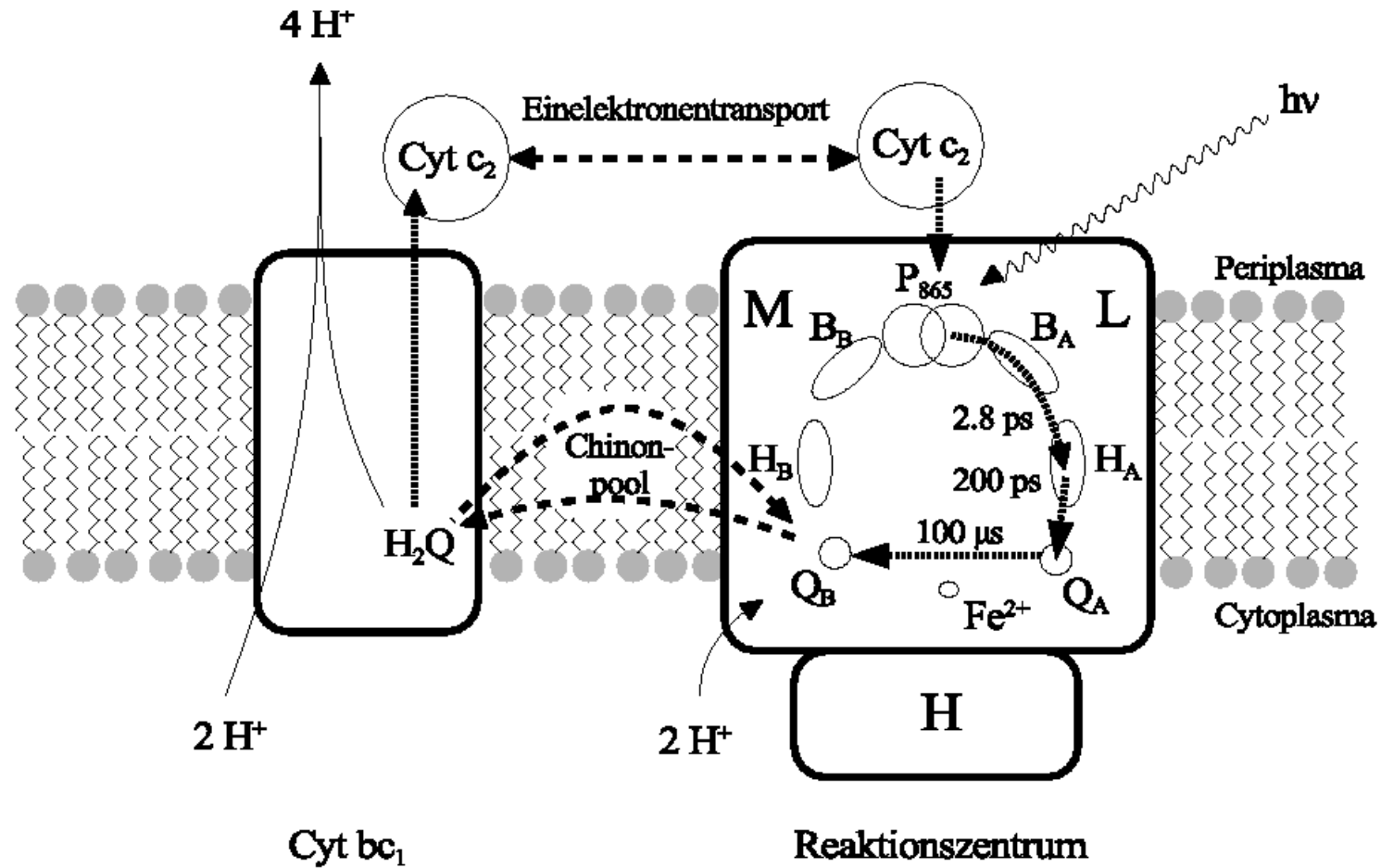


# Photochemical Reactions in Nature: Photosynthesis in Green Plants



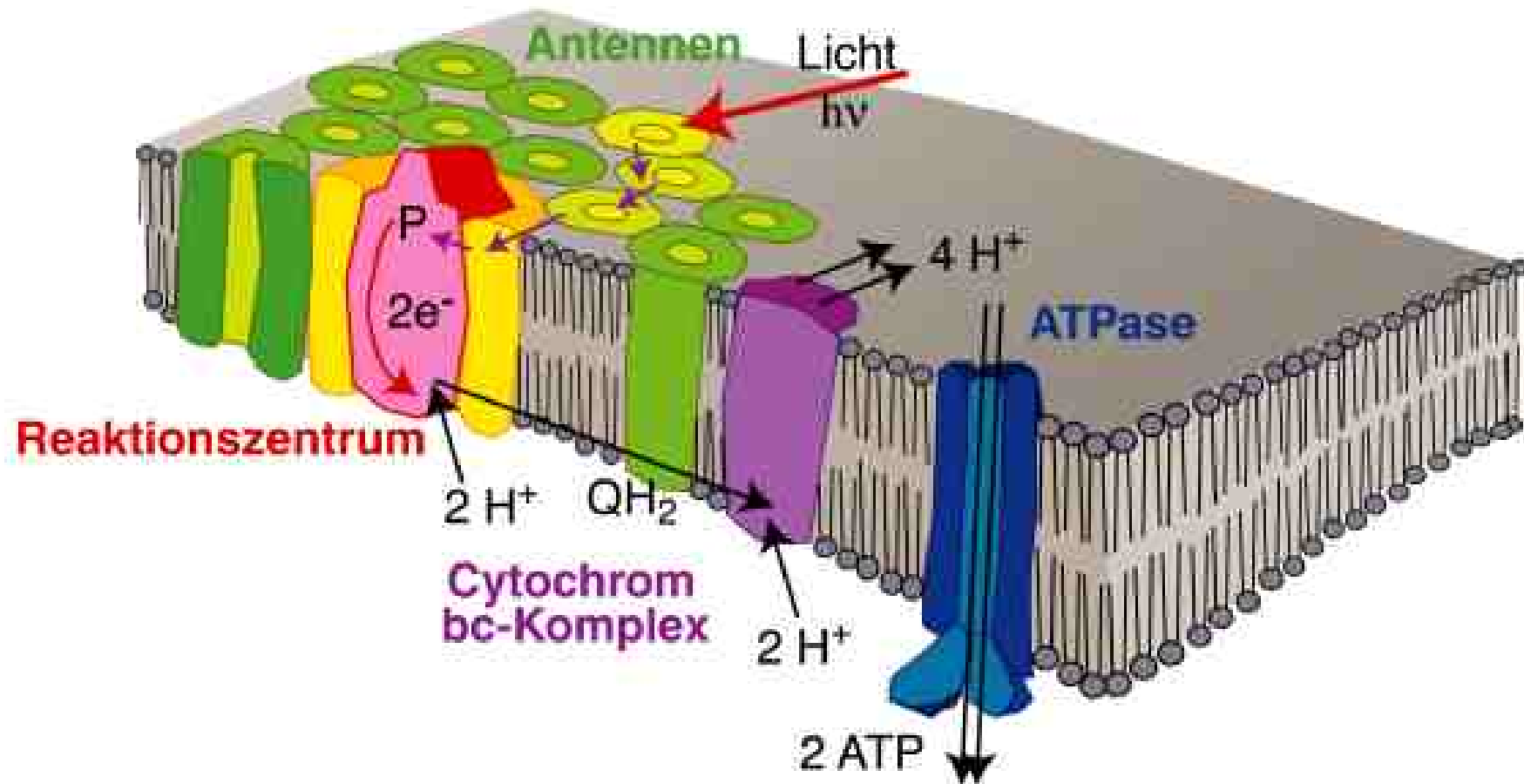


# Photochemical Reactions in Nature: Bacterial Photosynthesis





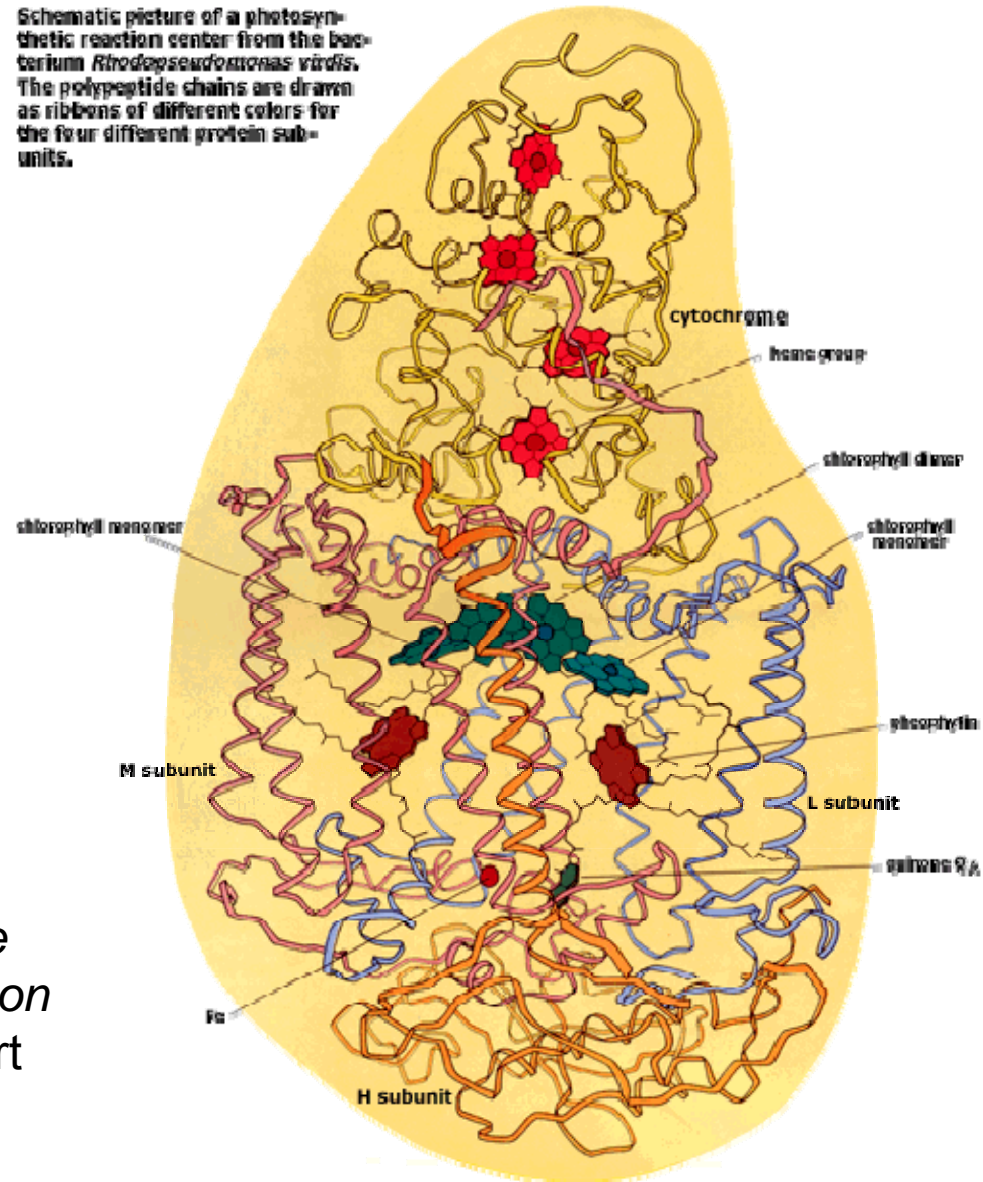
# Photochemical Reactions in Nature: Bacterial Photosynthesis





# Photochemical Reactions in Nature: Bacterial Photosynthesis

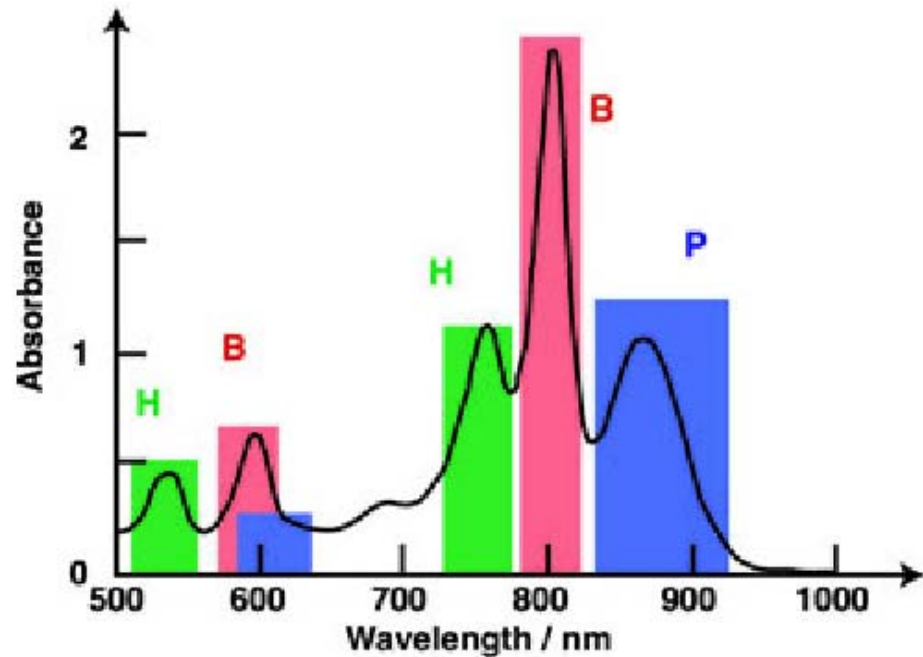
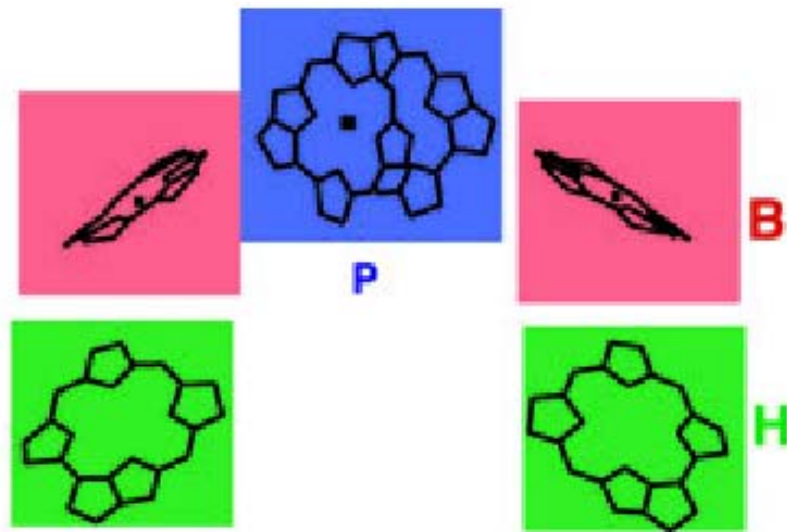
Schematic picture of a photosynthetic reaction center from the bacterium *Rhodospseudomonas viridis*. The polypeptide chains are drawn as ribbons of different colors for the four different protein subunits.



Nobel Prize in Chemistry 1988 *The structure of a photosynthetic reaction center*, Johann Deisenhofer, Robert Huber and Hartmut Michel

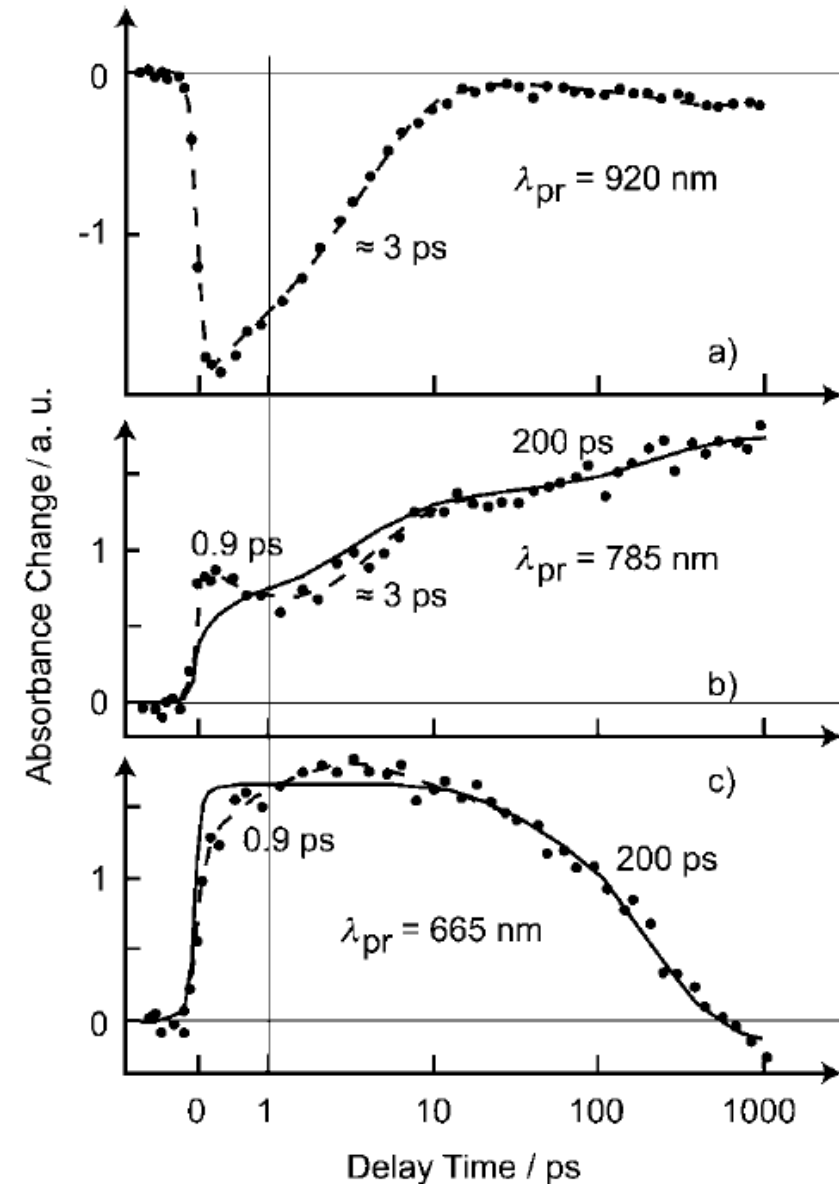
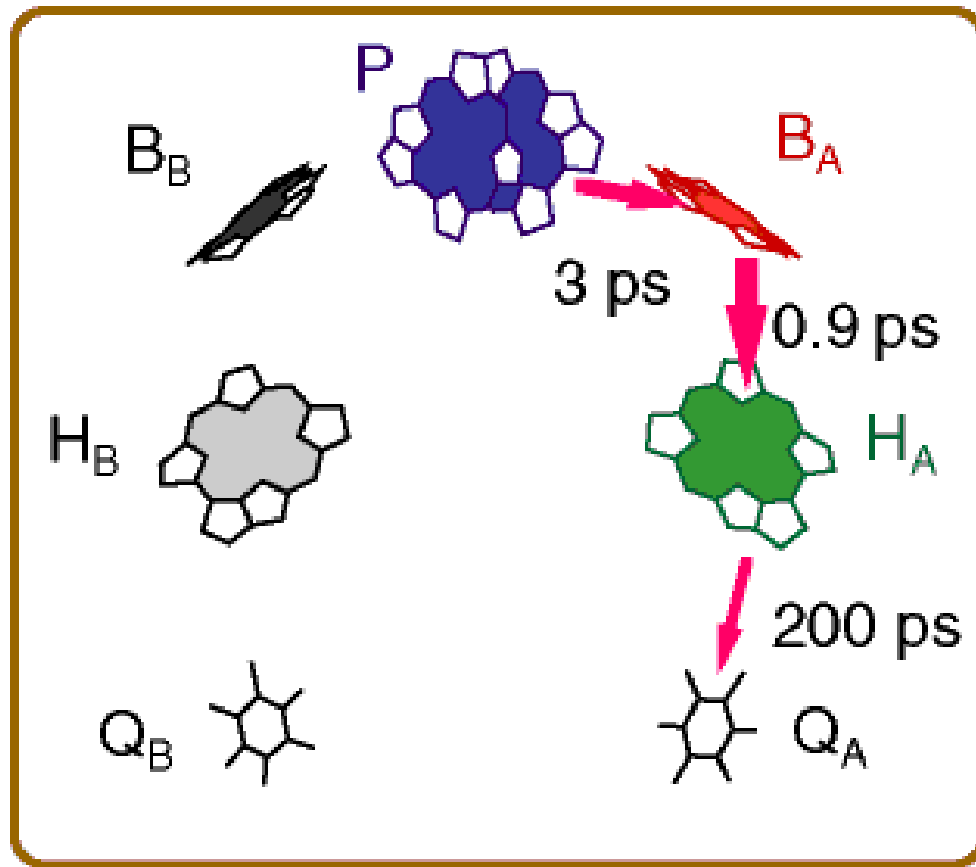


# Photochemical Reactions in Nature: Electron Transfer in Photosynthesis



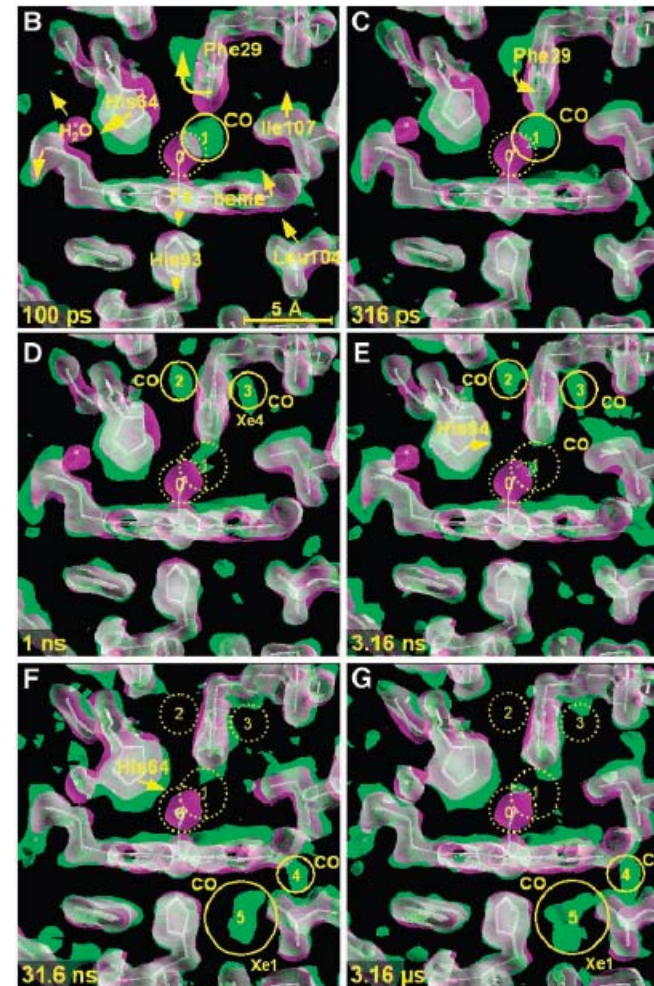
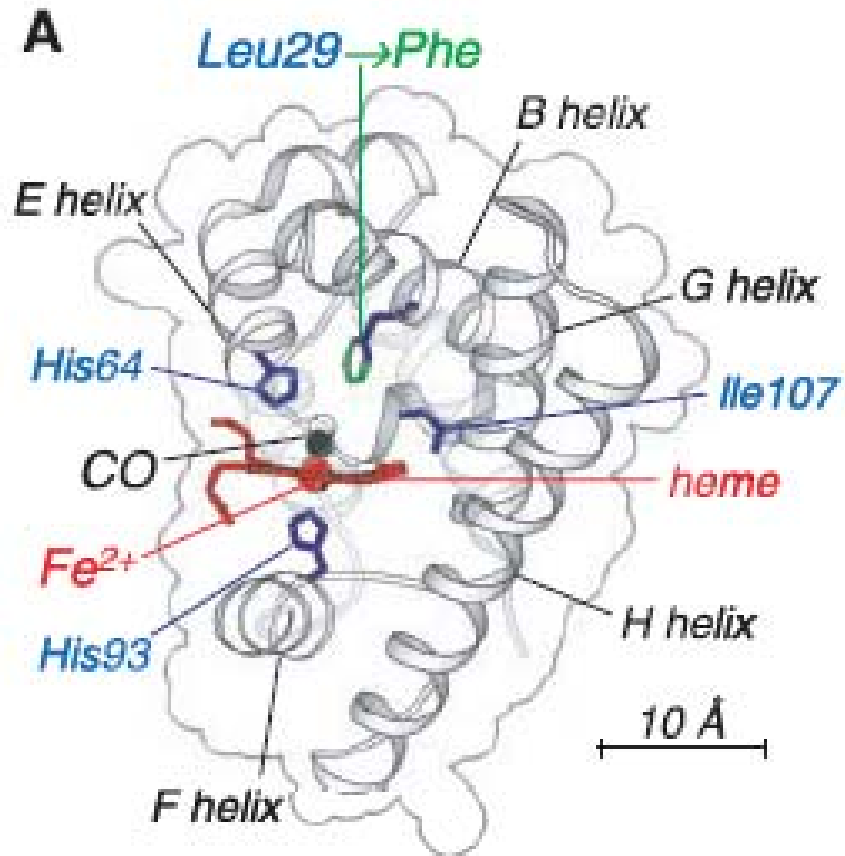


# Photochemical Reactions in Nature: Electron Transfer in Photosynthesis





# Photochemical Reactions in Nature: Myoglobin



Friedrich Schotte, Manho Lim, Timothy A. Jackson, Aleksandr V. Smirnov, Jayashree Soman, John S. Olson, George N. Phillips Jr., Michael Wulff, Philip A. Anfinrud *Watching a Protein as it Functions with 150-ps Time-Resolved X-ray Crystallography*, Science, 300 1944 (2003)



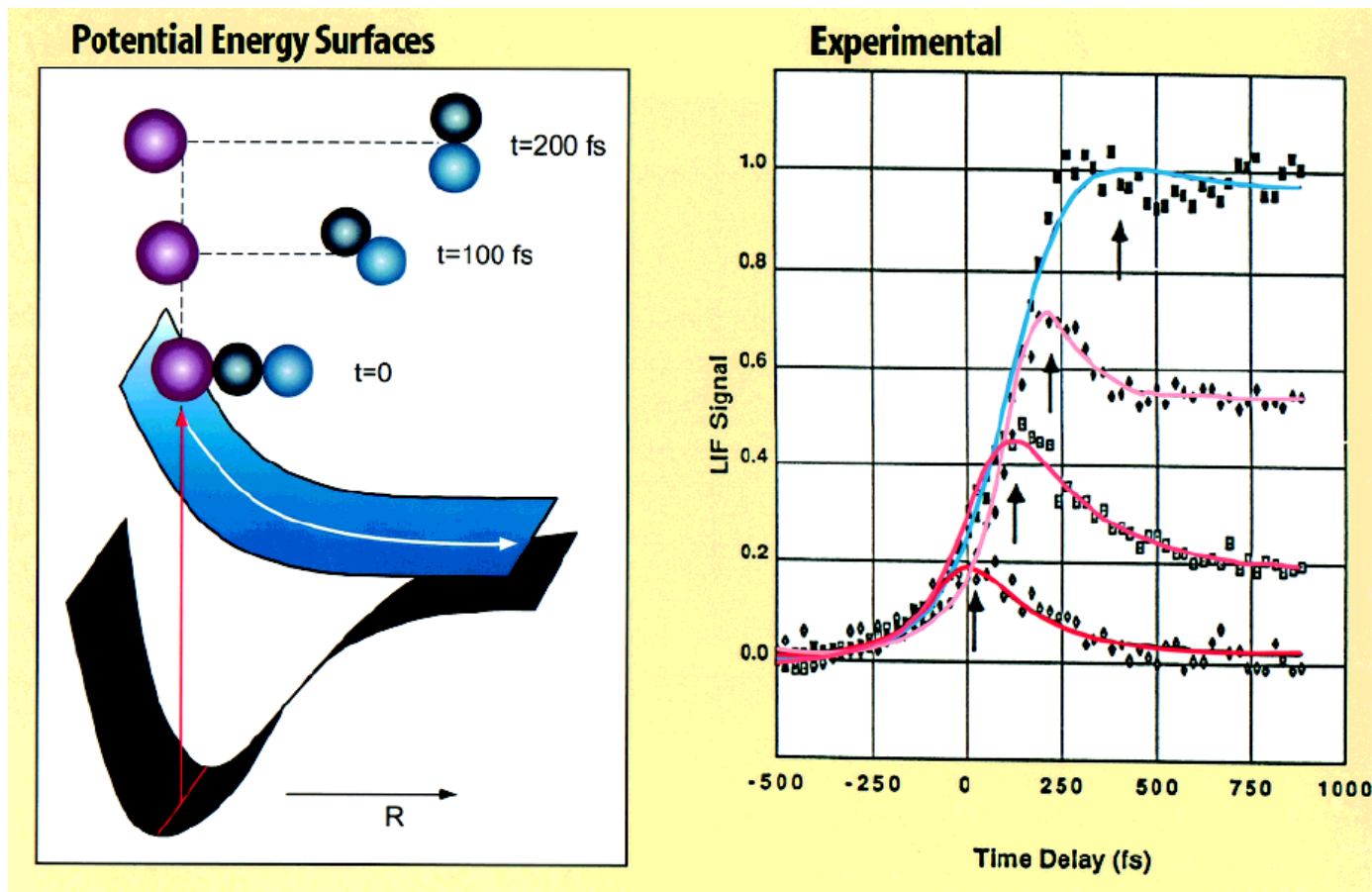
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# Prototype Photochemical Reactions in Chemistry





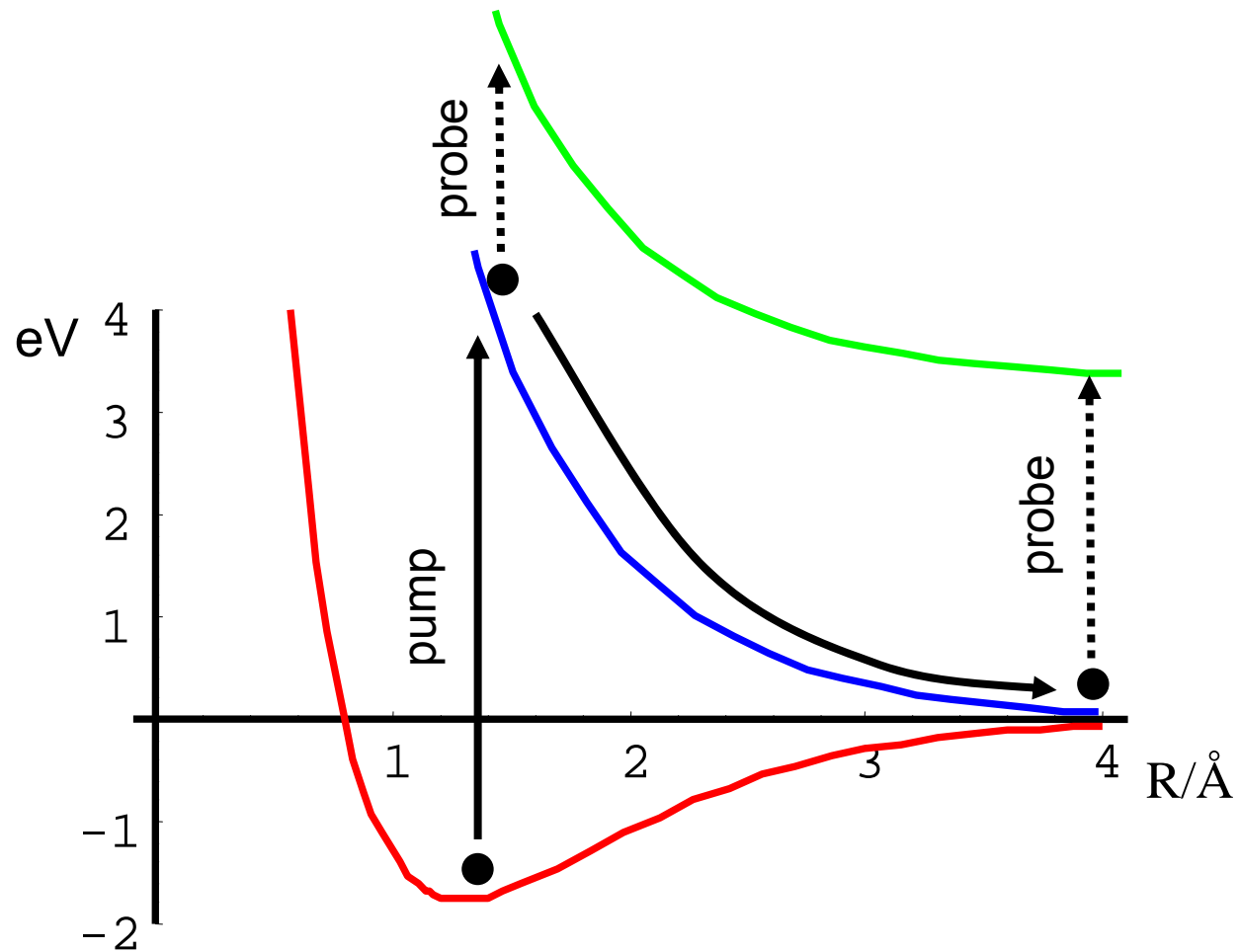
# Prototype Photochemical Reaction: ICN



M. Dantus, M. J. Rosker, A. H. Zewail, J. Chem. Phys. 87 (1987) 2395  
A. H. Zewail, J. Phys. Chem. A 104 (2000) 5660

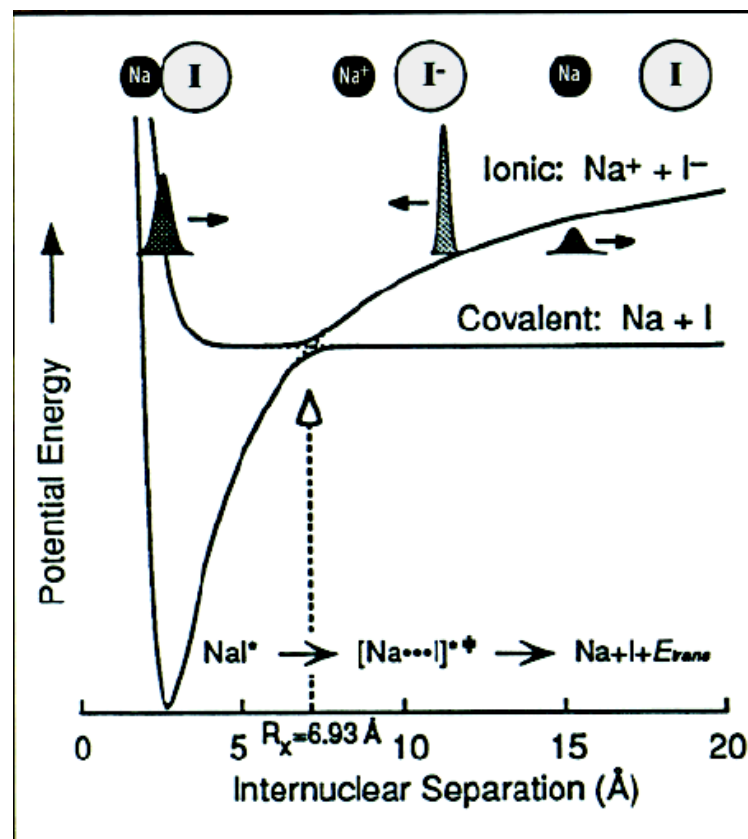
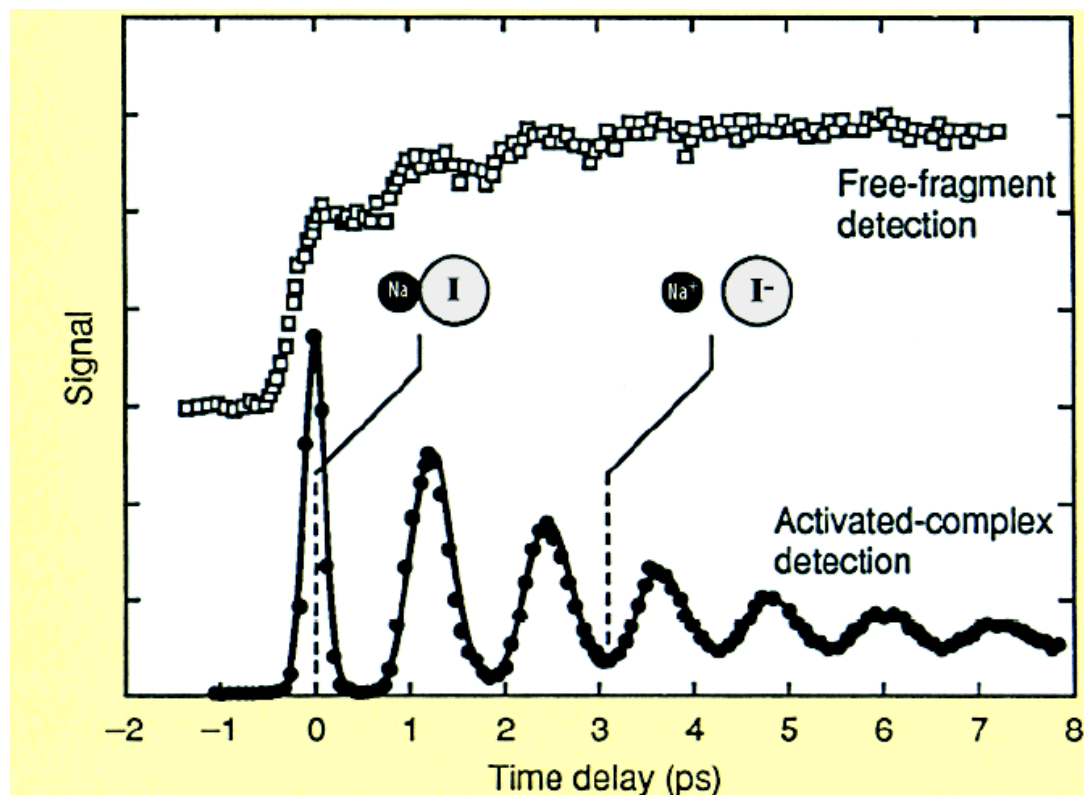


# Photochemie: $\text{H}_2^+$ -Molekül





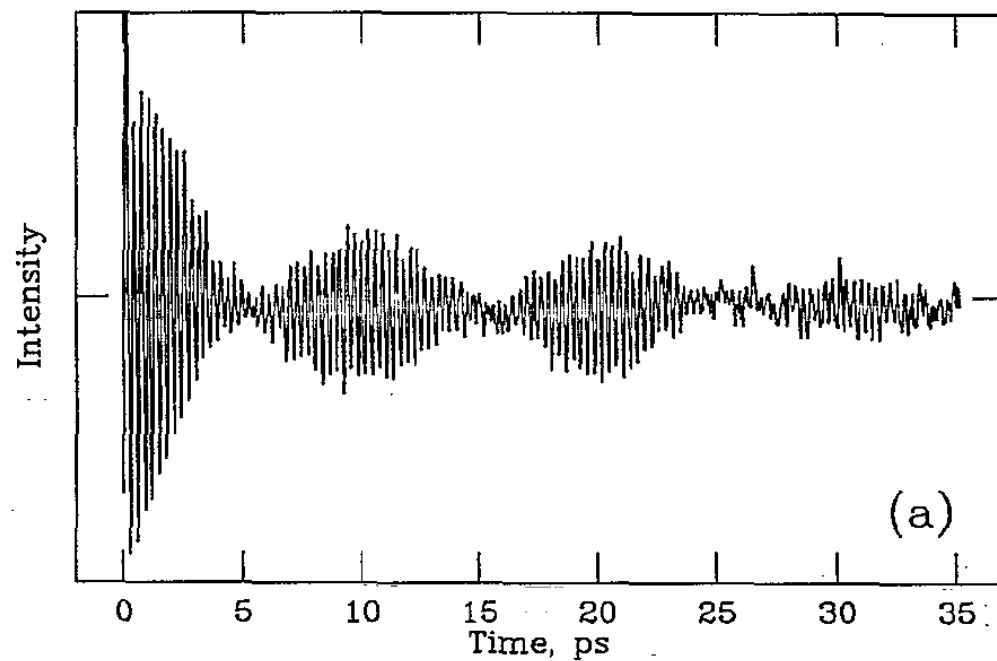
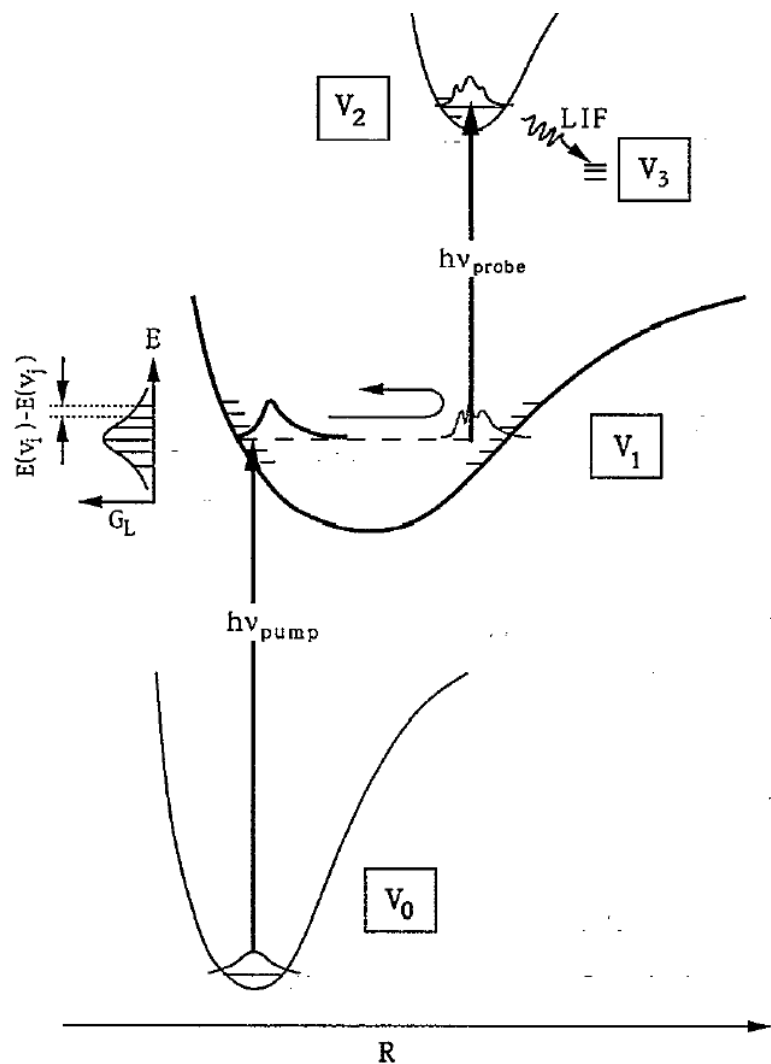
# Prototype Photochemical Reaction: NaI



T. S. Rose, M. J. Rosker, A. H. Zewail, J. Chem. Phys. 91 (1989) 7415  
A. H. Zewail, J. Phys. Chem. A 104 (2000) 5660

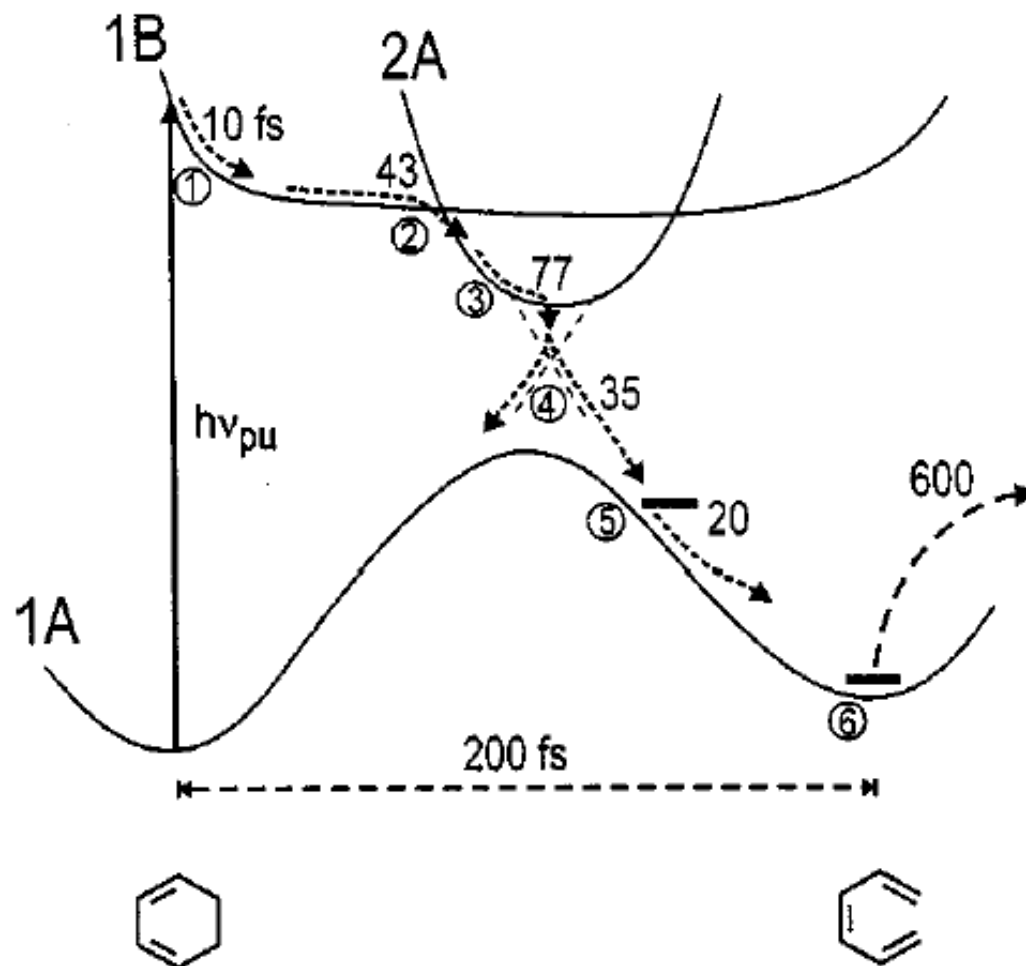


# Motion in Quantum Mechanics: I<sub>2</sub>





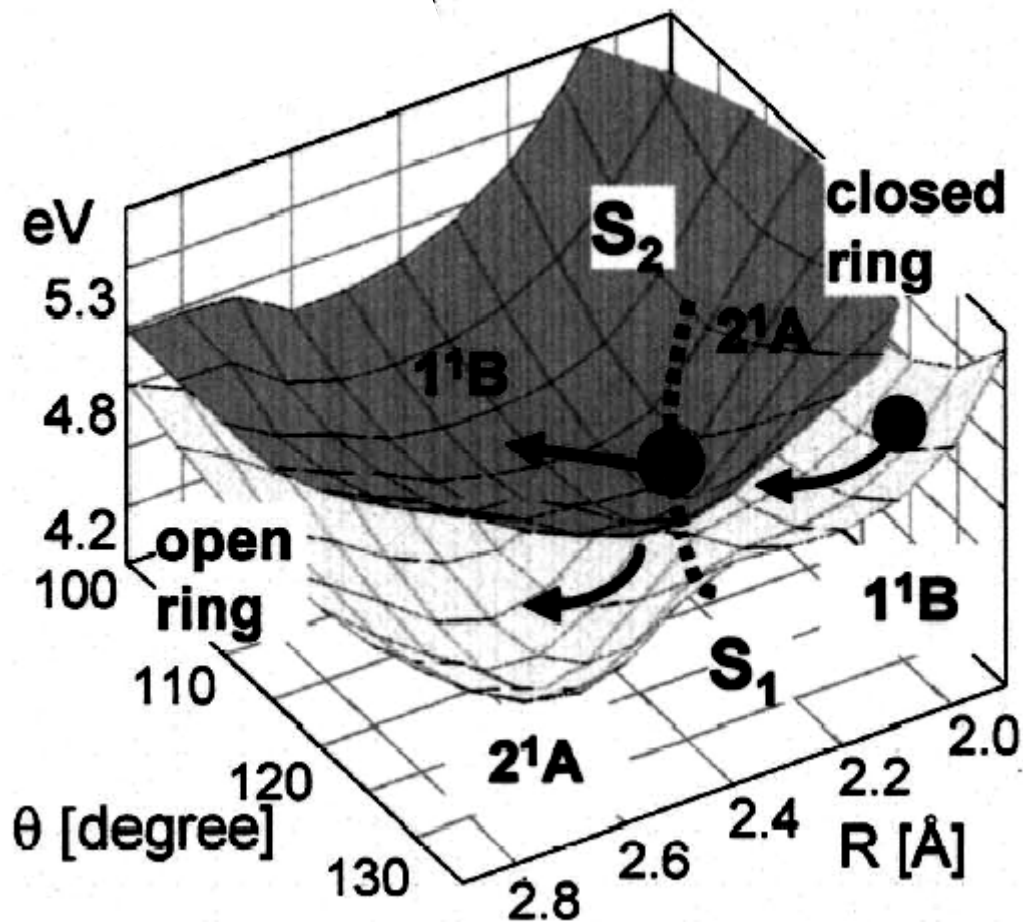
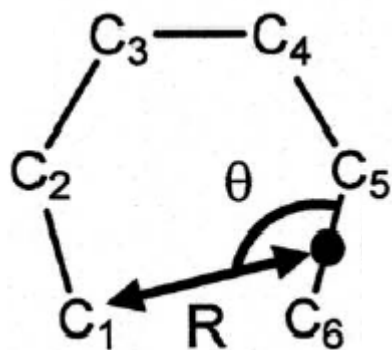
# Ring Opening of 1-3-Cyclohexadien



W. Fuß, W. E. Schmid, and S. A. Trushin, Time-resolved dissociative intense-laser field ionization for probing dynamics: Femtosecond photochemical ring opening of 1,3-cyclohexadiene, *J. Chem. Phys.* 112 (2000) 8347



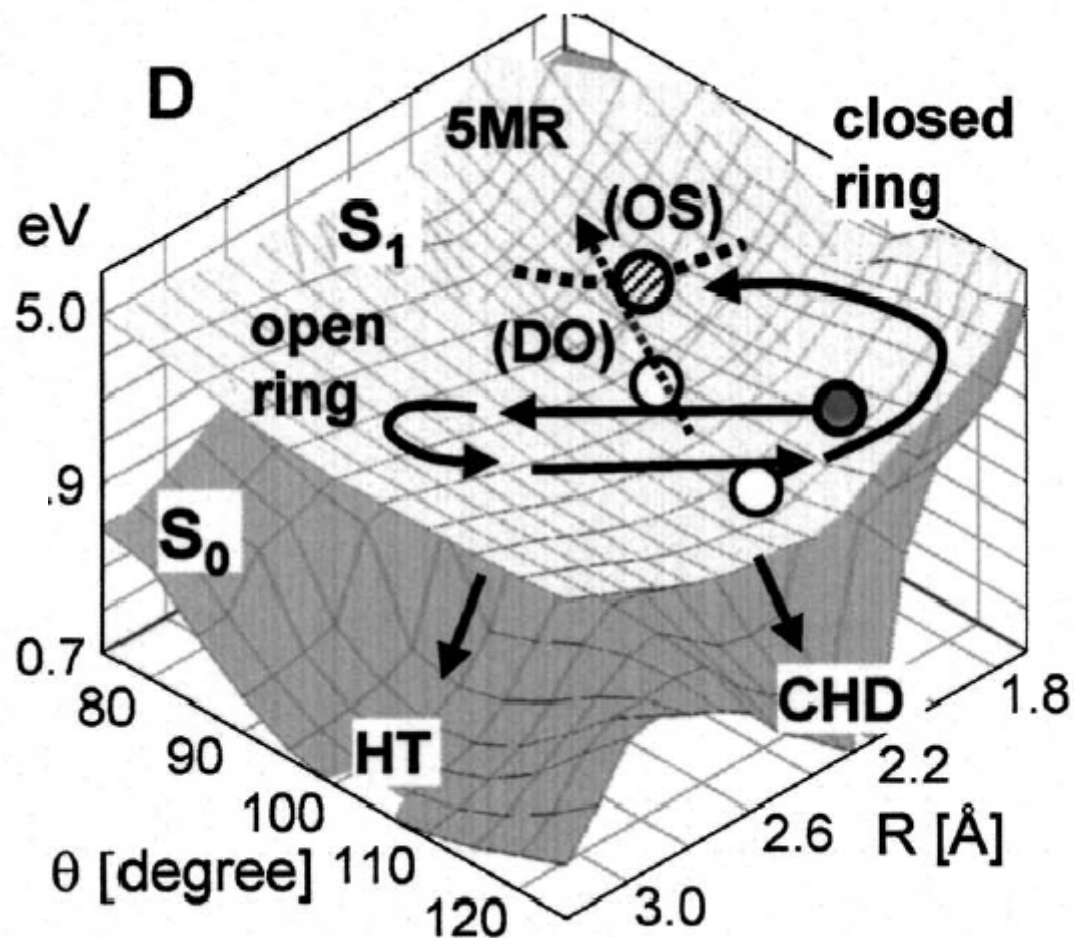
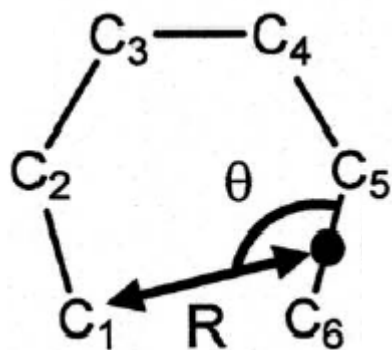
# Ring Opening of 1-3-Cyclohexadien



H. Tamuraa S. Nanbu T. Ishida H. Nakamura *Ab initio nonadiabatic quantum dynamics of cyclohexadiene/hexatriene ultrafast photoisomerization* J Chem. Phys. **124**, 084313 2006



# Ring Opening of 1-3-Cyclohexadien



H. Tamuraa S. Nanbu T. Ishida H. Nakamura *Ab initio nonadiabatic quantum dynamics of cyclohexadiene/hexatriene ultrafast photoisomerization* J Chem. Phys. **124**, 084313 2006



# Femtochemistry: Basic Concepts

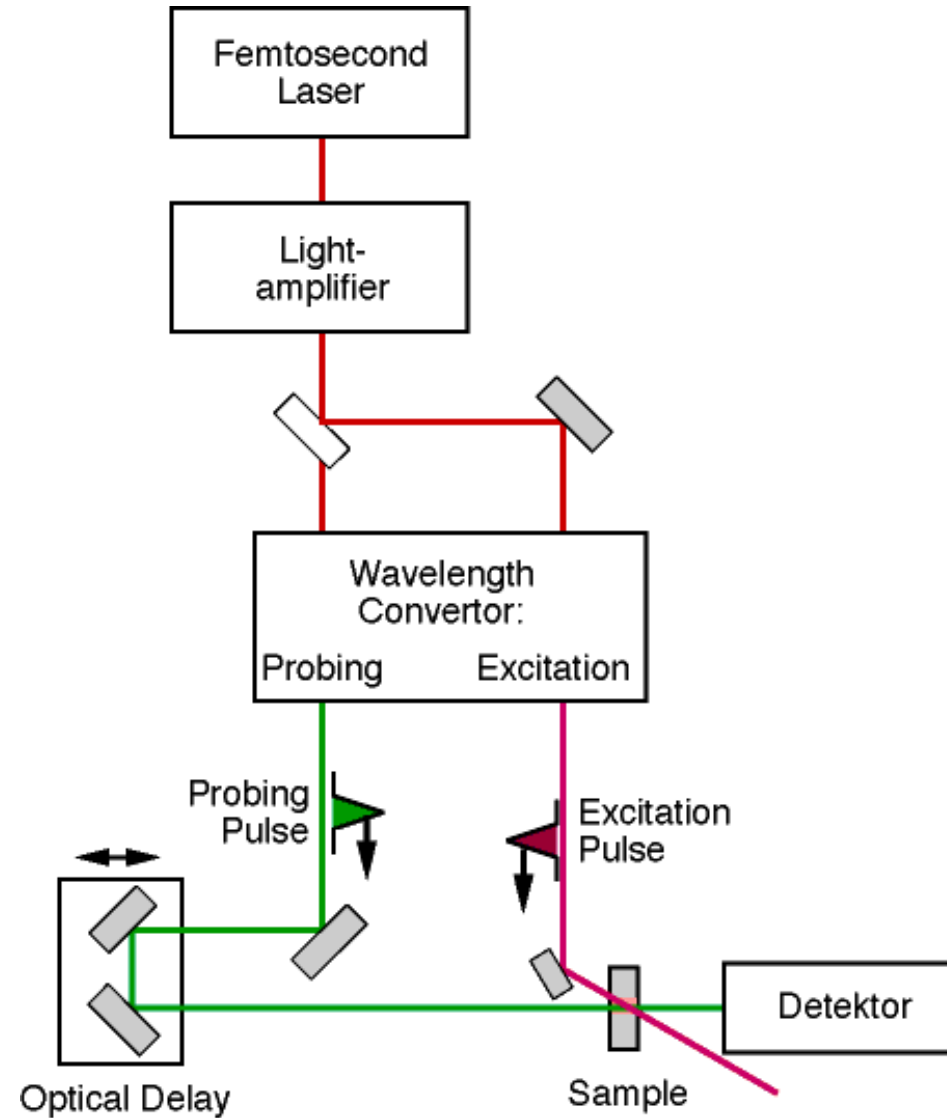
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- Examples of Photochemical Reactions
- **Experimental Methods**
- Motion in Quantum Mechanics: Wavepackets
- Franck-Condon Transition
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- Prototype Potential Energy Surfaces
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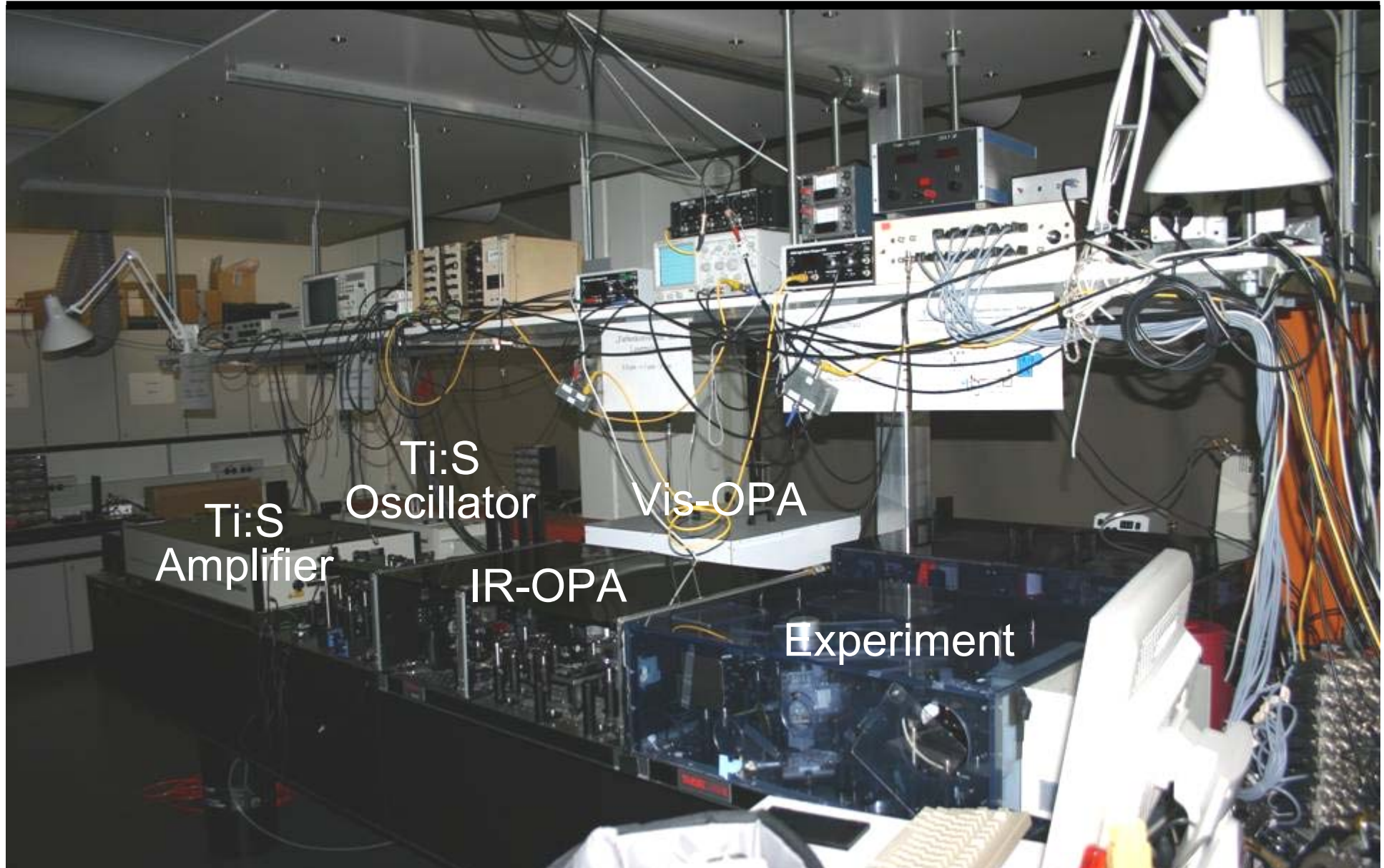


# Pump-Probe Spectroscopy





# The Laser Lab



Ti:S  
Amplifier

Ti:S  
Oscillator

IR-OPA

Vis-OPA

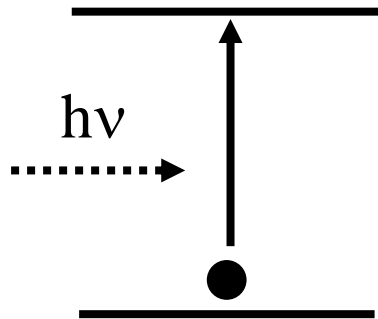
Experiment



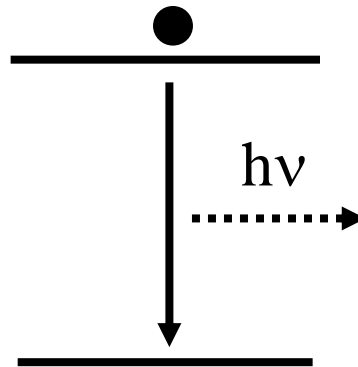
# Interaction of Light with Matter

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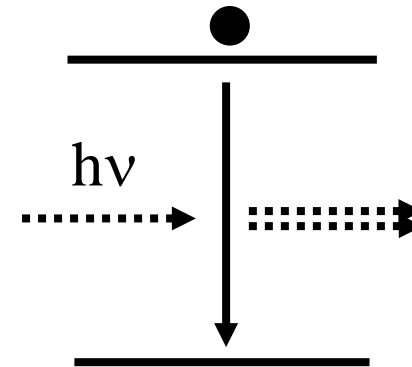
Absorption



spontaneous  
Emission



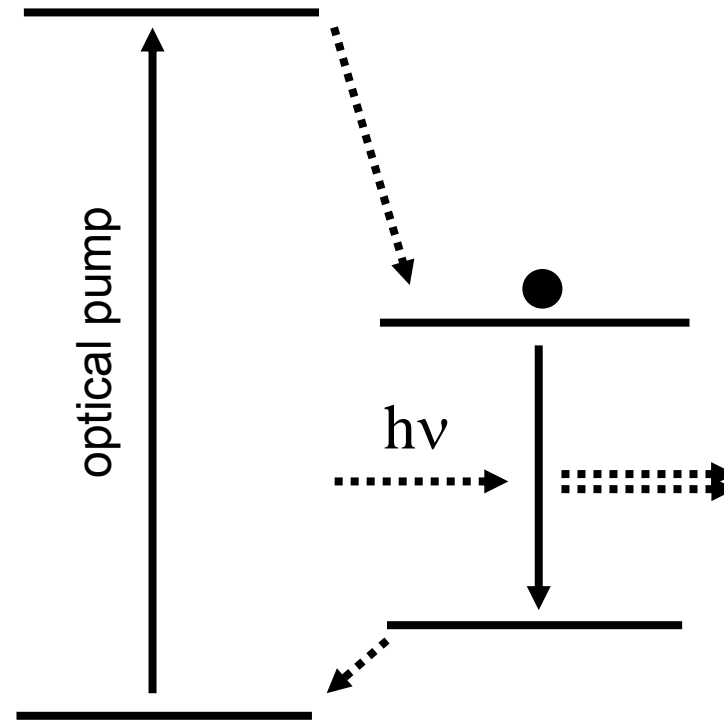
stimulated  
Emission





# 4-Level System

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# Laser

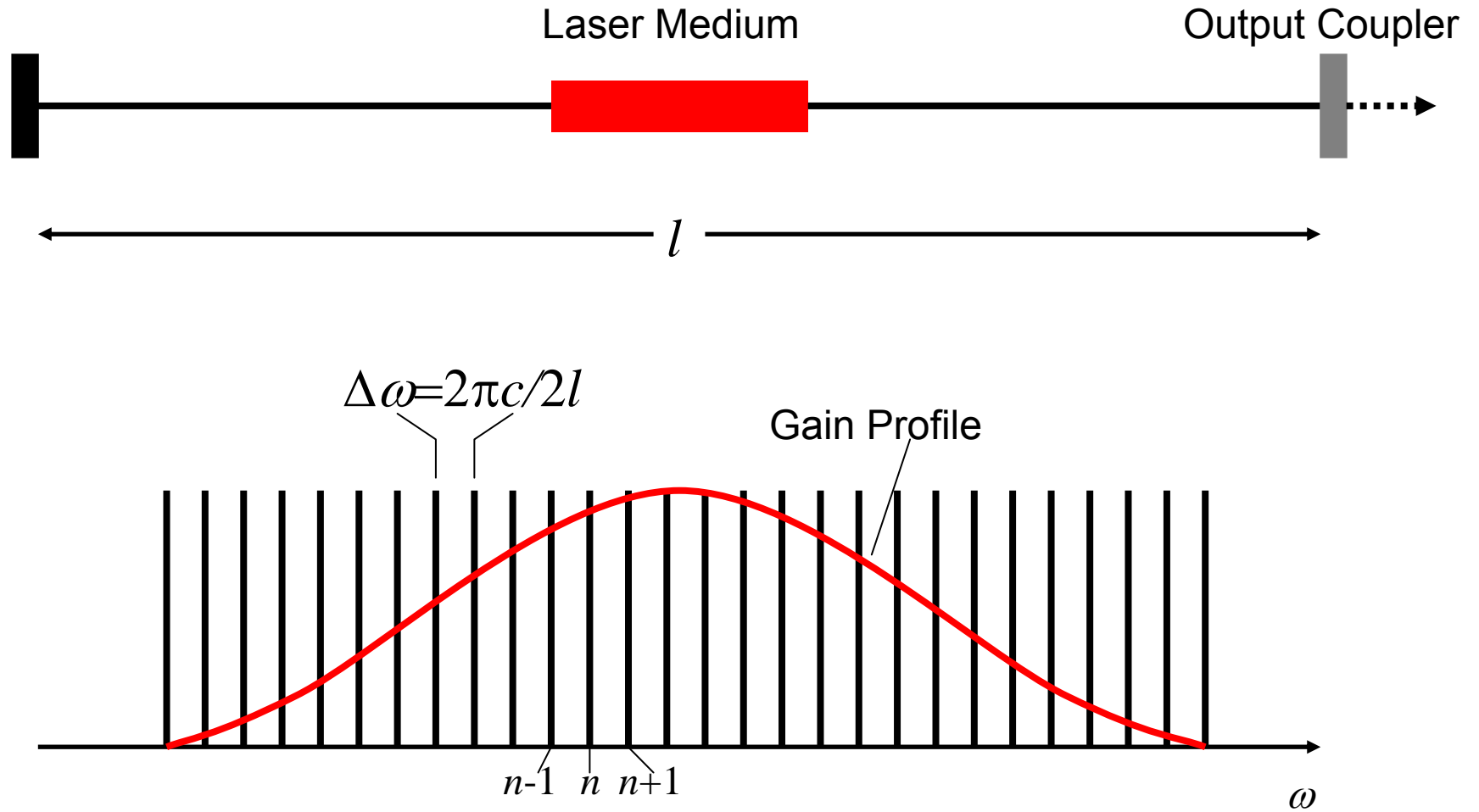


## Short Pulses:

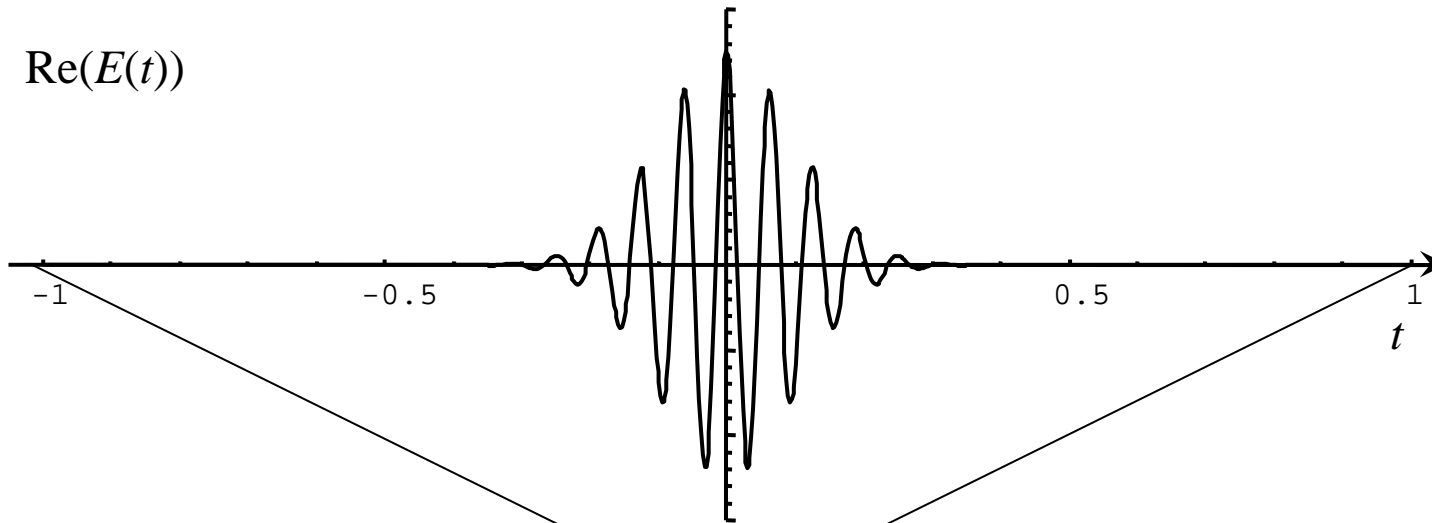
- Broad Gain Medium (organic Dyes, Ti:S)
- Mode Locking
- Dispersion Control



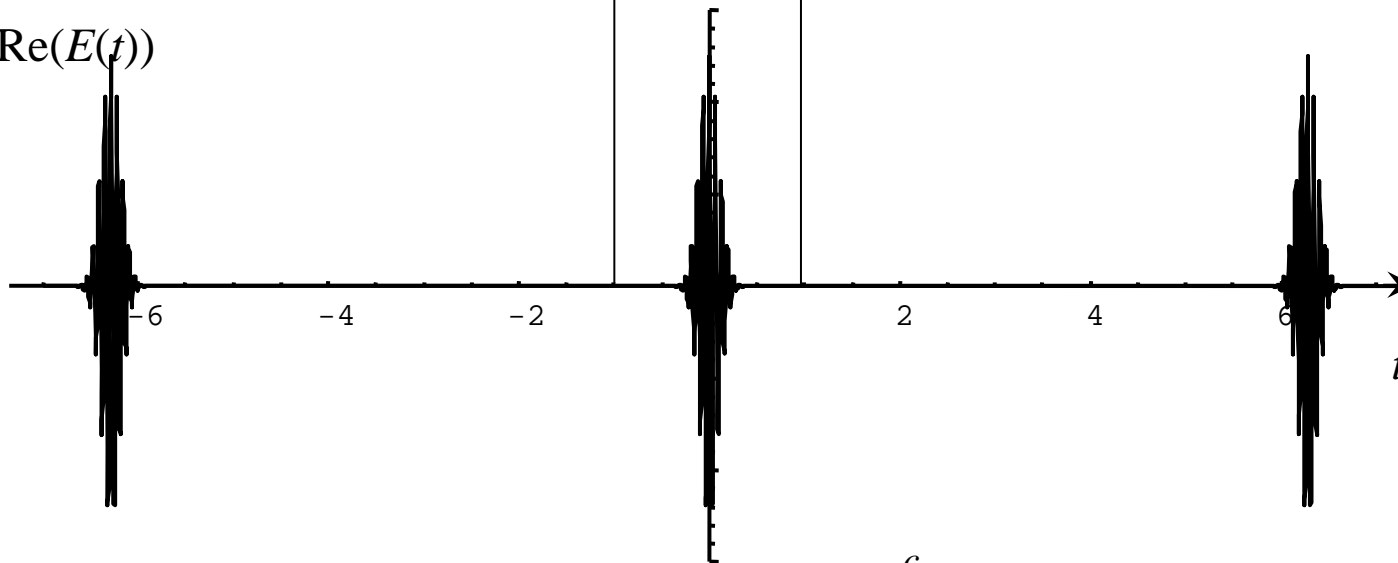
# Laser



$\text{Re}(E(t))$



$\text{Re}(E(t))$

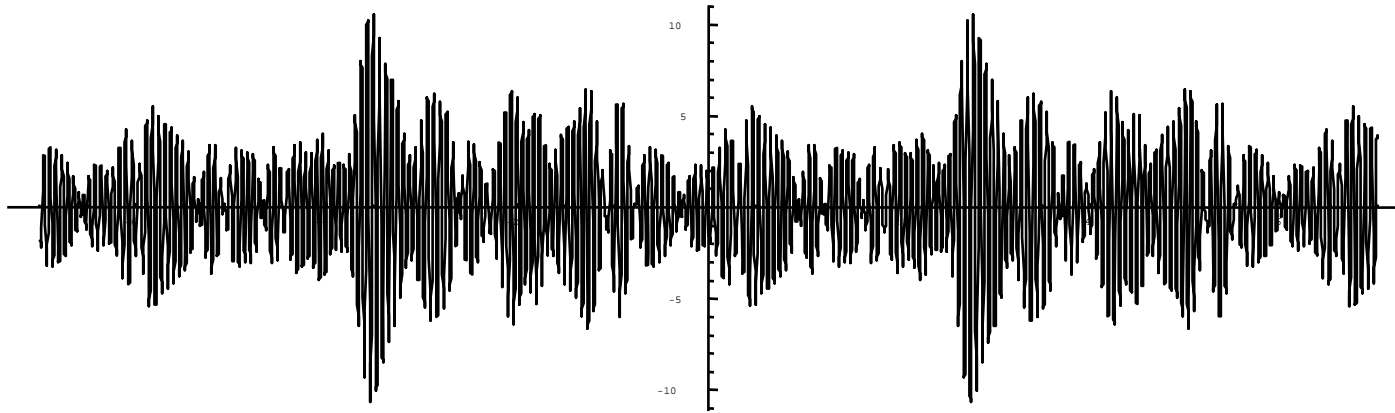


$$E(t) = \sum_n E_n e^{i2\pi n \frac{c}{2l} t}$$



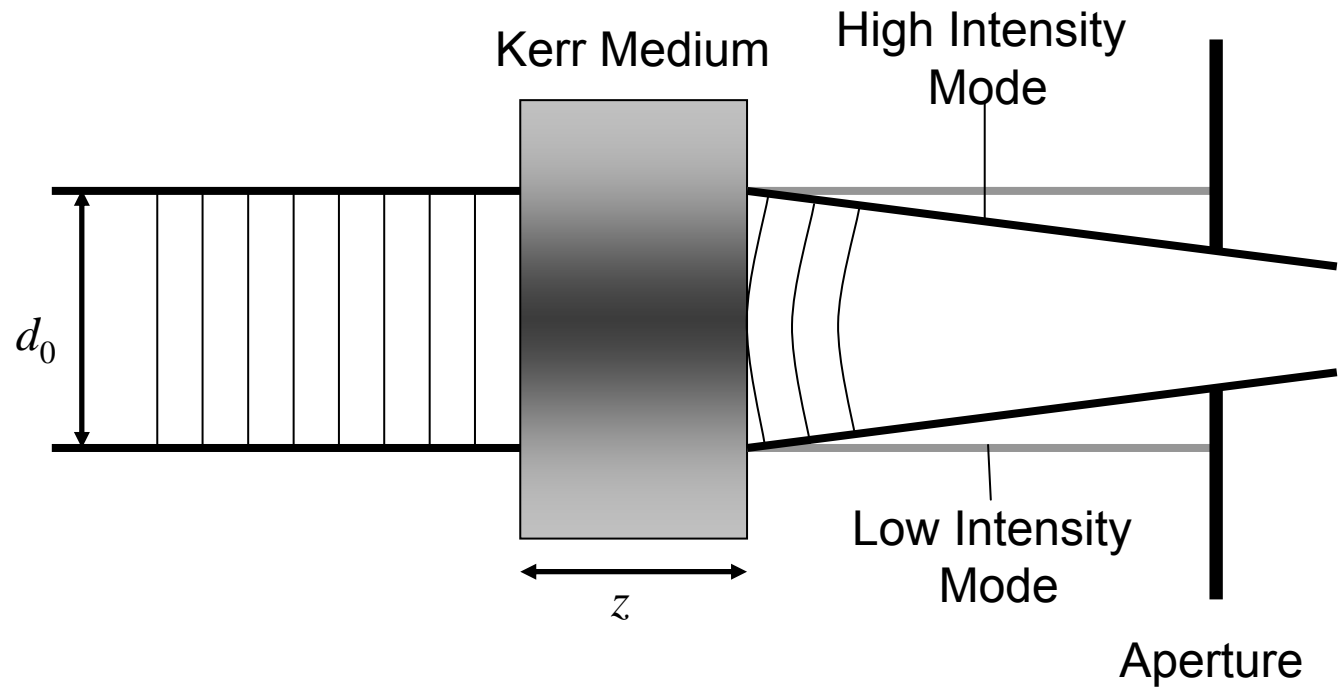
# Random Phase

$E(t)$



$$E(t) = \sum_n E_n e^{i\varphi_n} e^{i2\pi\frac{c}{2l}t}$$





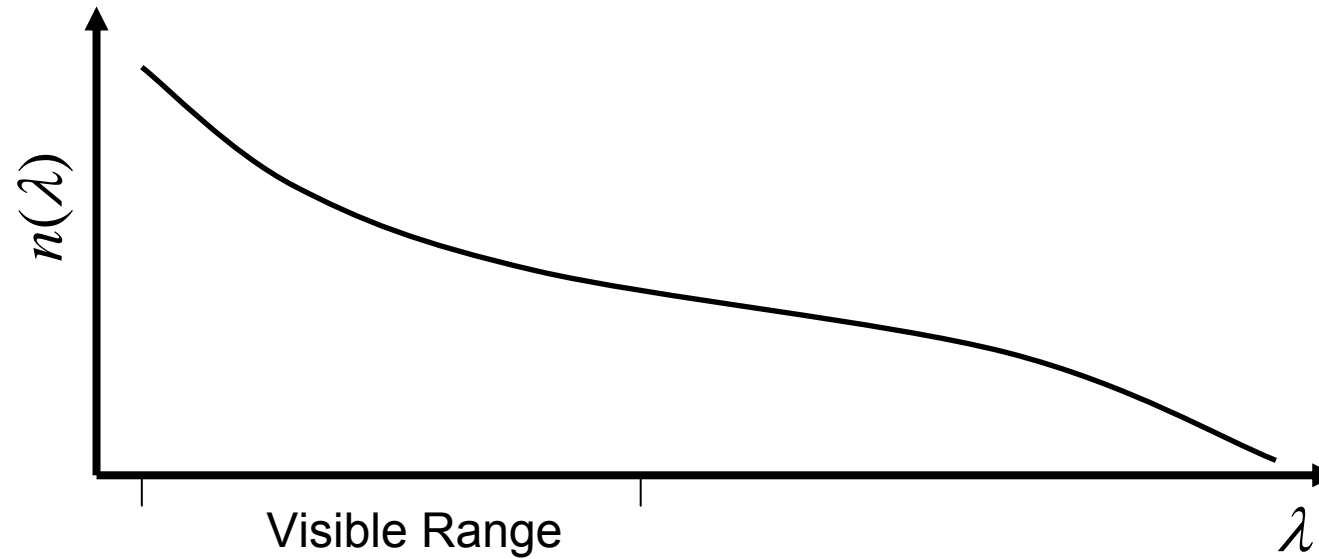
Kerr Effect:

$$n(I) = n_0 + I \times n_2$$



# Dispersion

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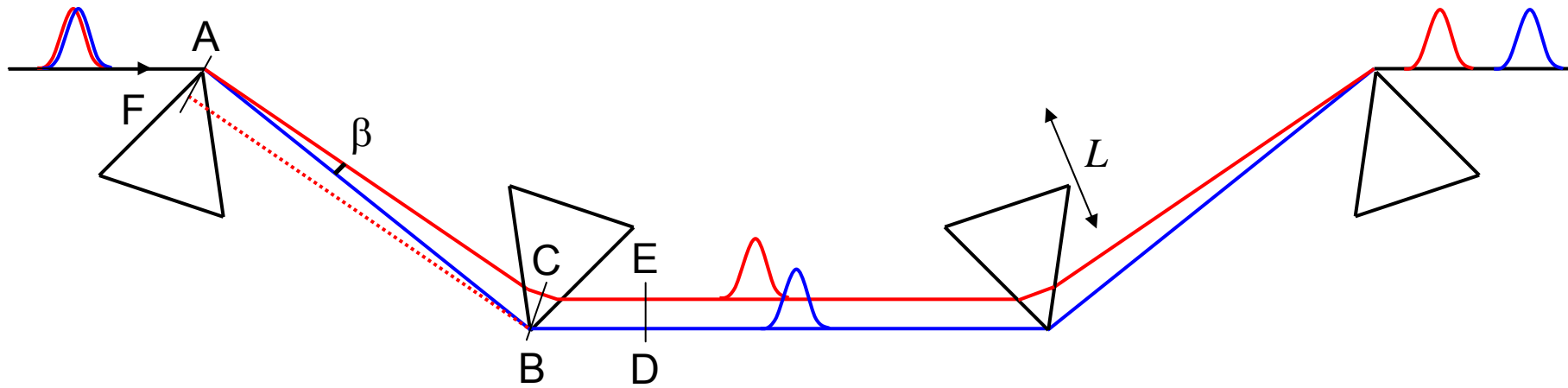


$$v_{ph} = \frac{c}{n(\lambda)}$$

$$v_{gr} = \frac{c}{n(\lambda)} - \frac{\lambda}{c} \frac{dn}{d\lambda}$$

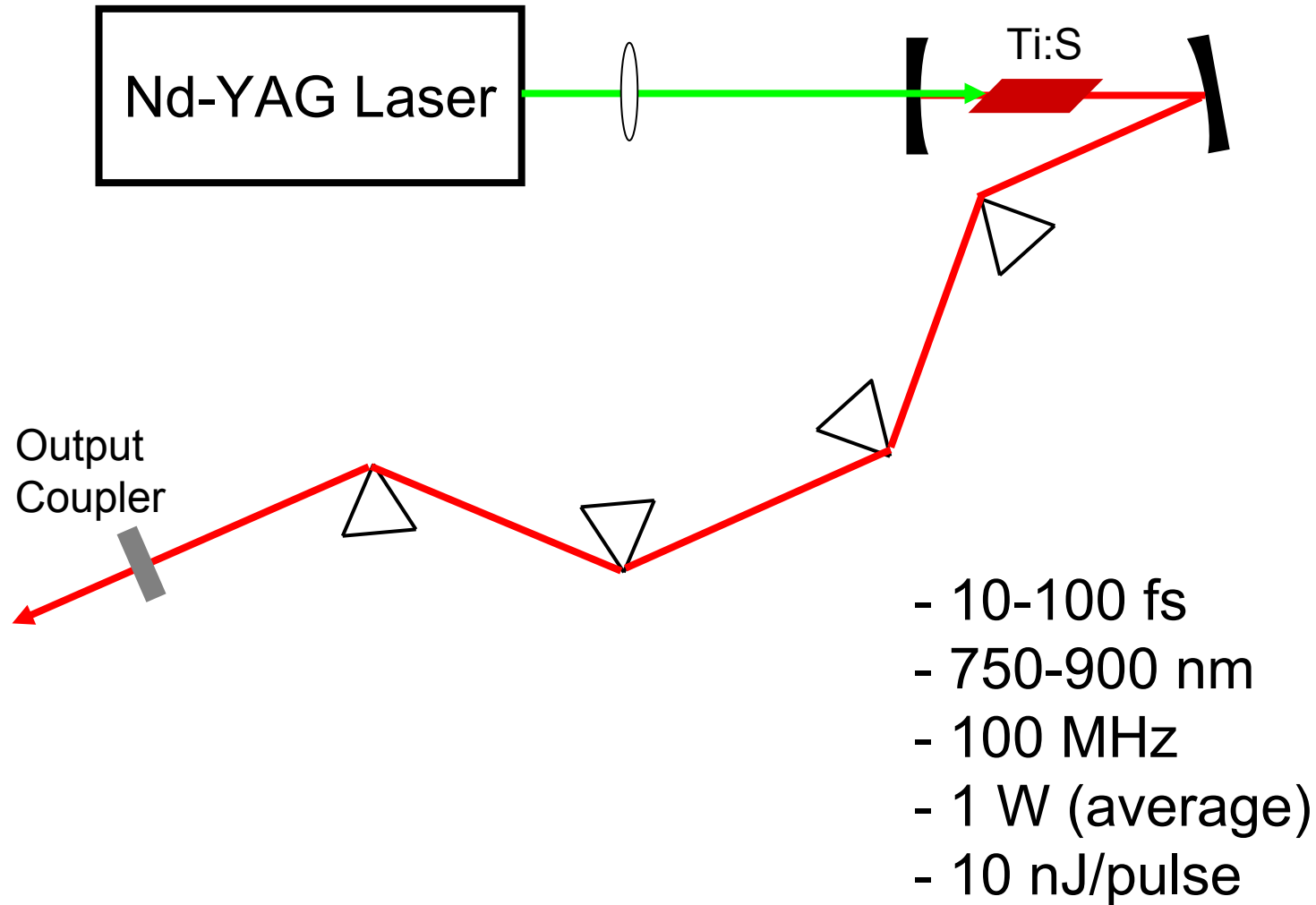


# Prism-Compressor





# Ti:S Laser





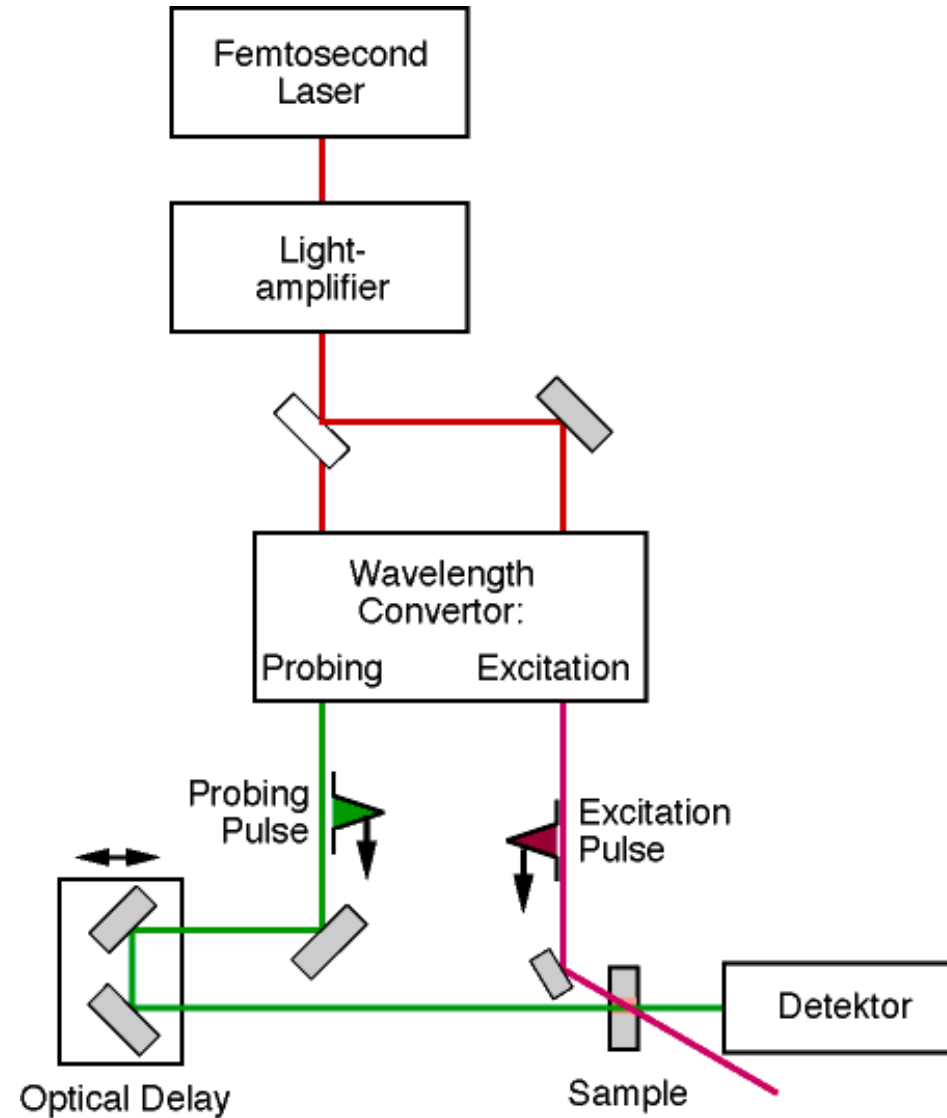
# Ti:S Laser

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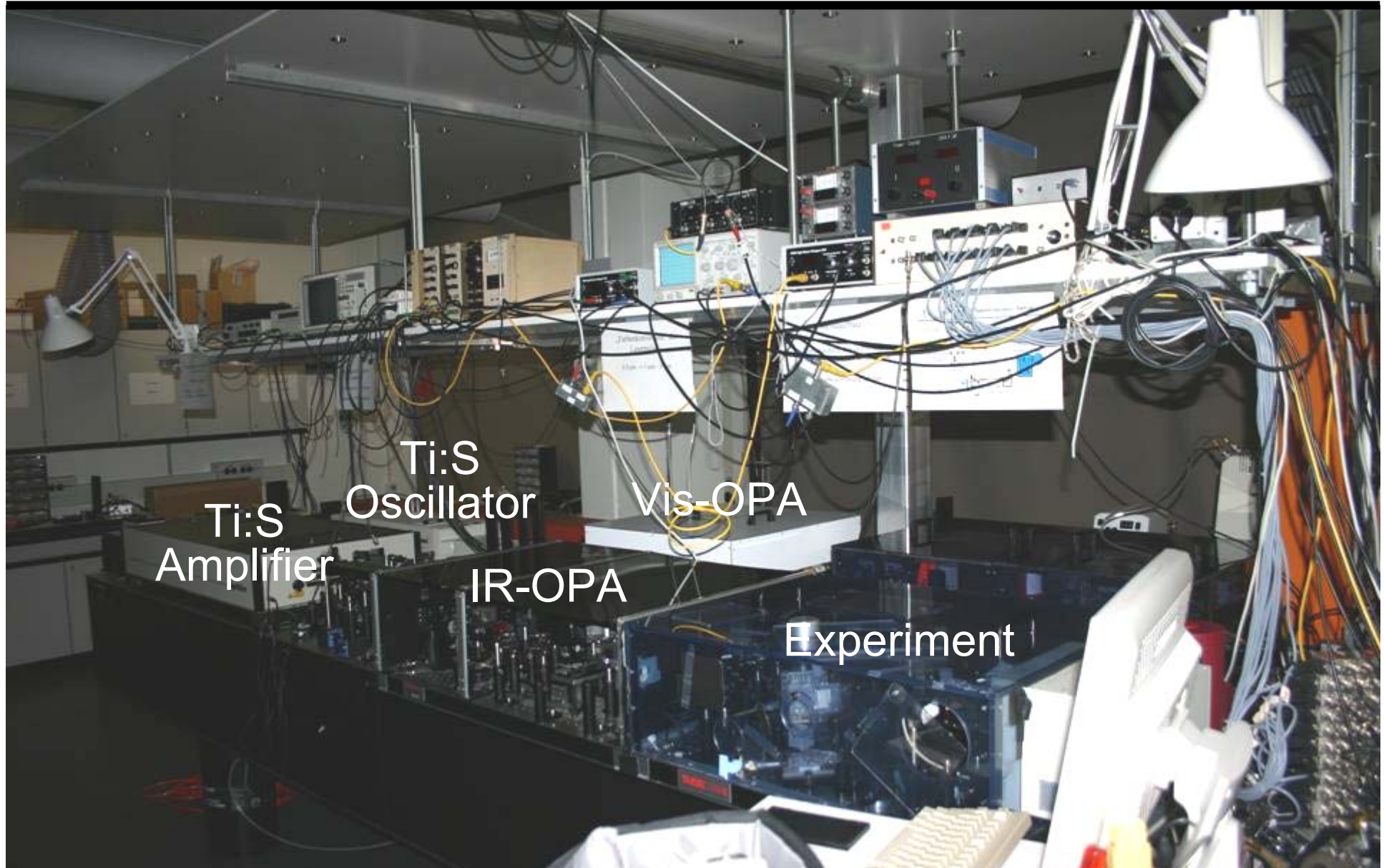


# Pump-Probe Spectroscopy



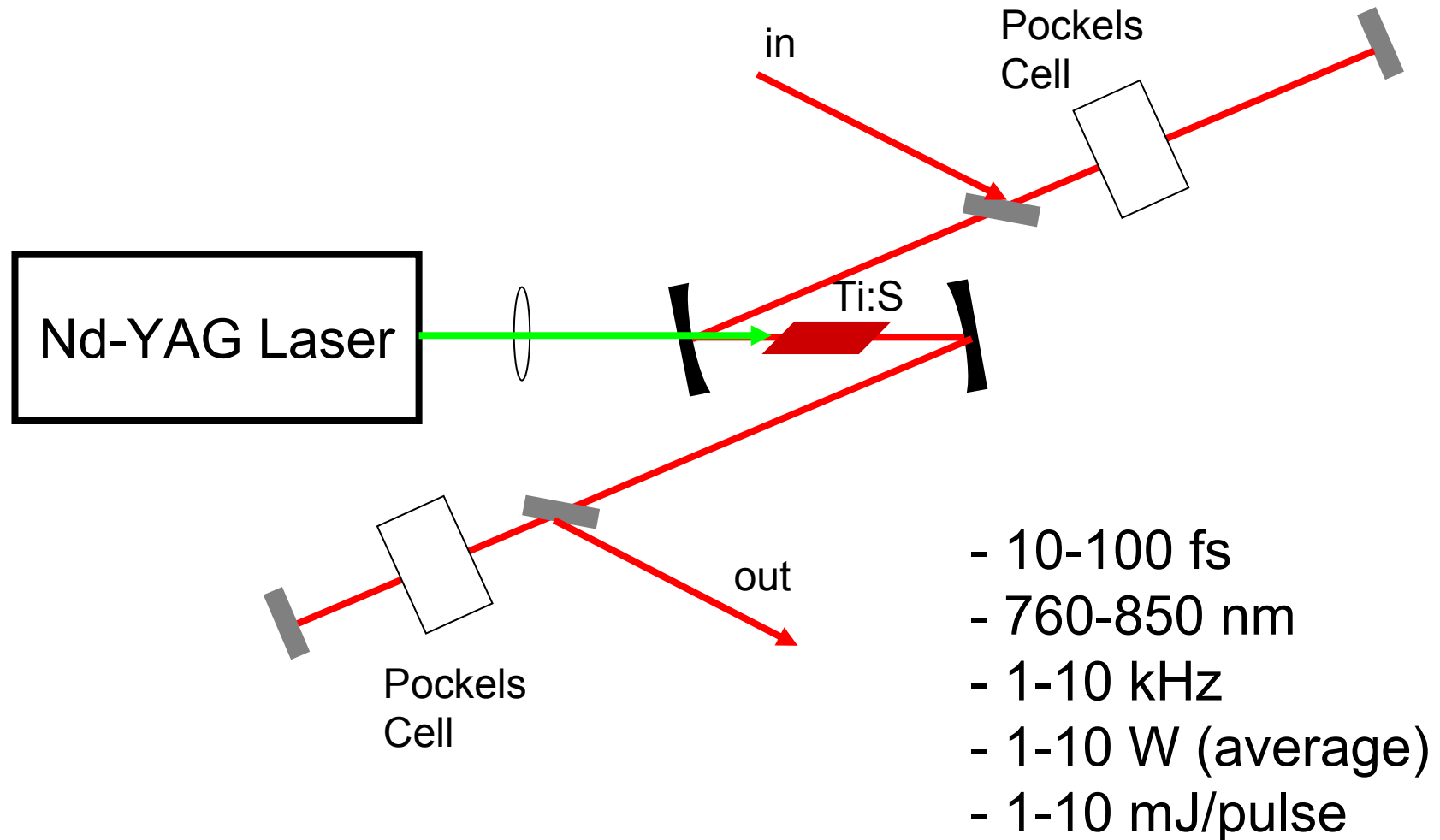


# The Laser Lab





# Regenerative Amplifier

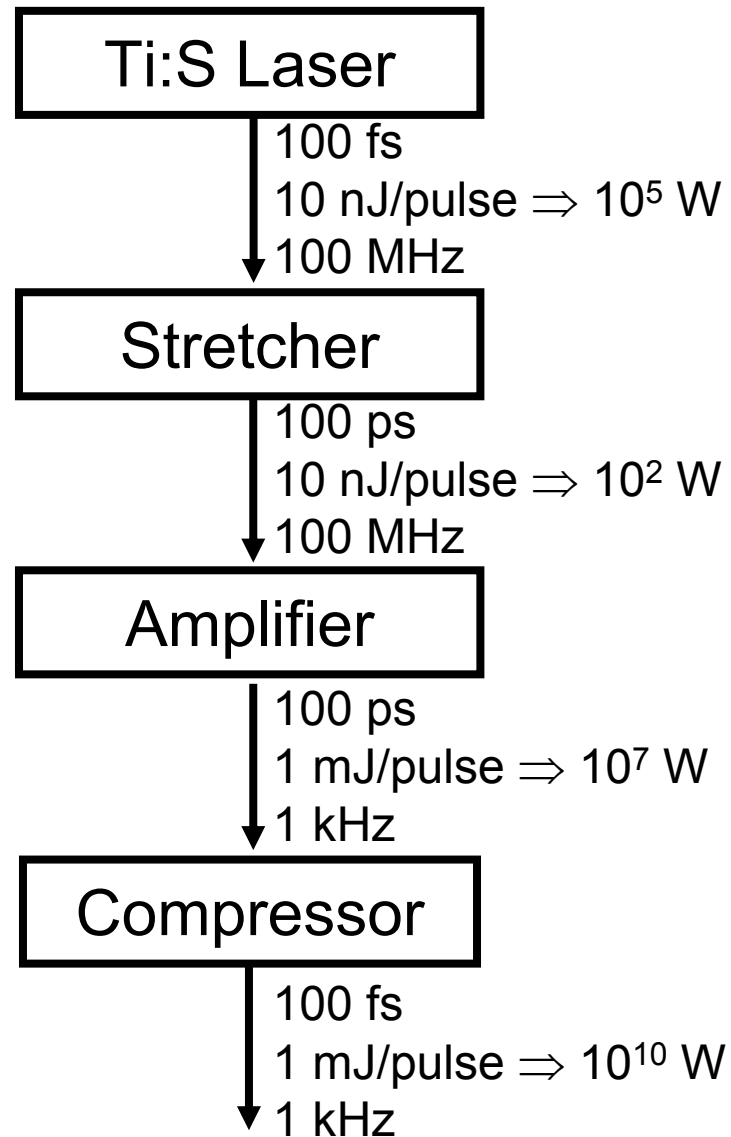






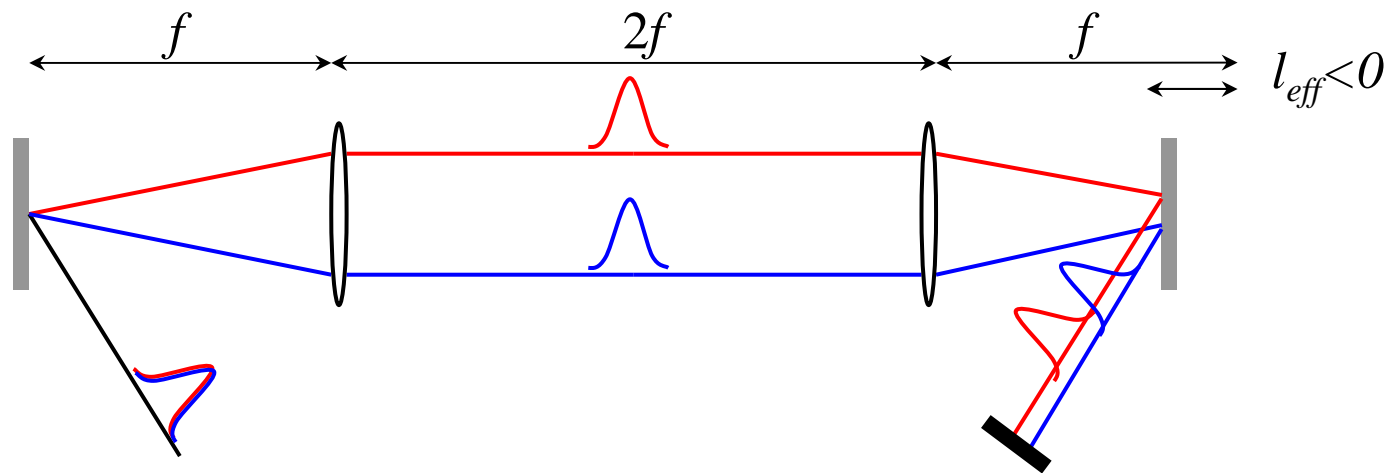
# Chirped Pulse Amplification

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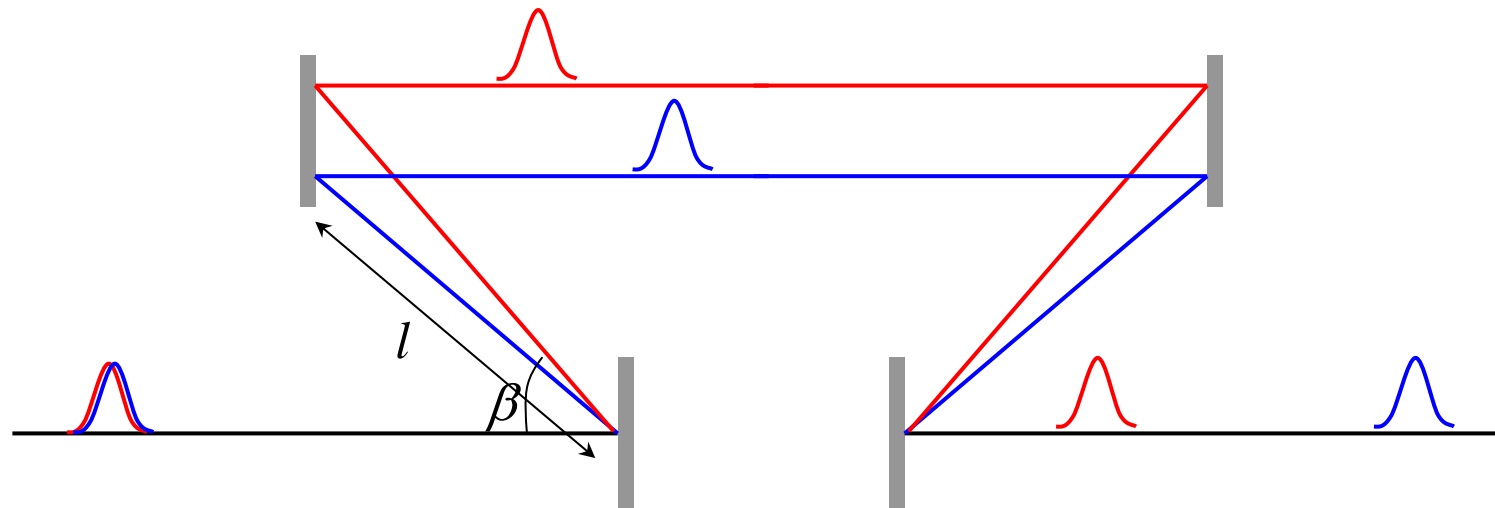


# Grating-Stretcher





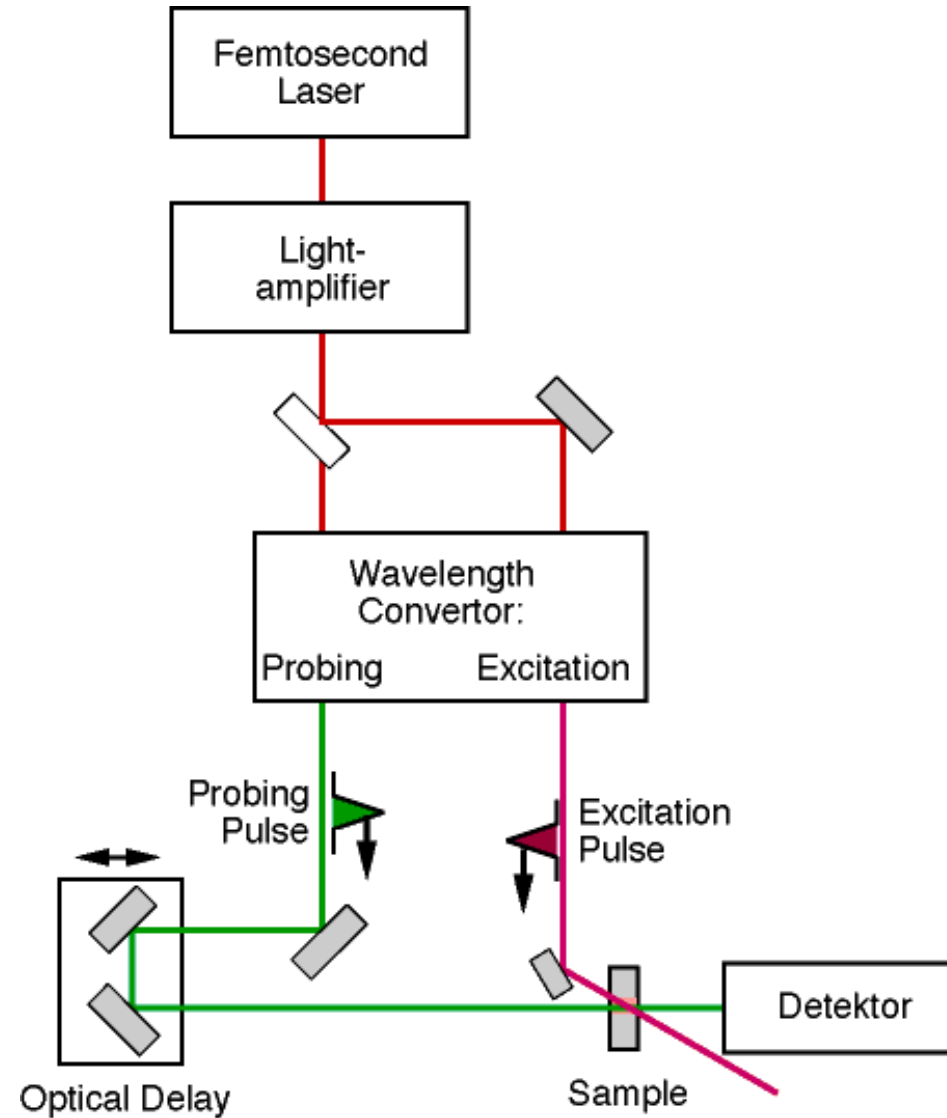
# Grating-Compressor





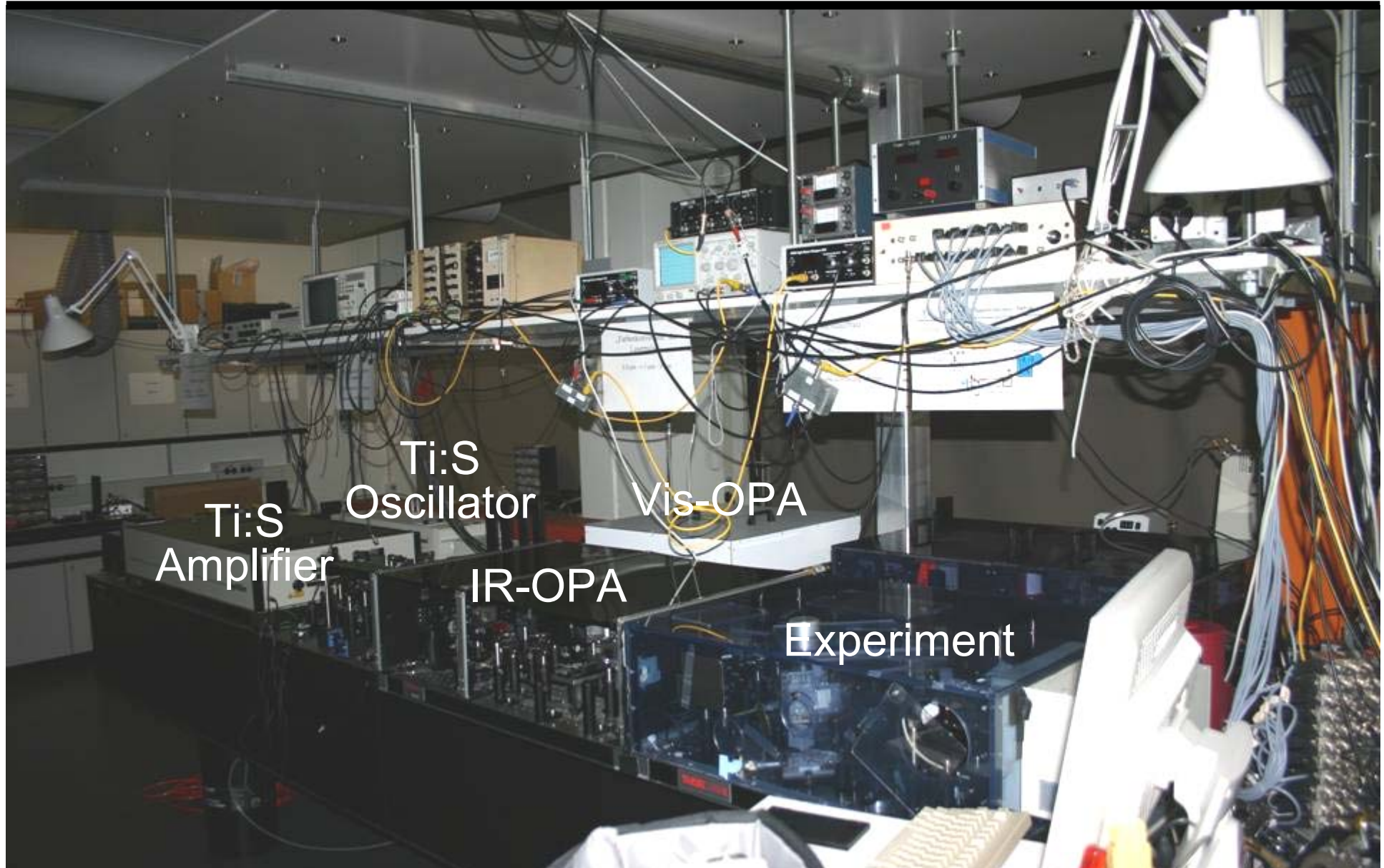


# Pump-Probe Spectroscopy





# The Laser Lab



Ti:S  
Amplifier

Ti:S  
Oscillator

IR-OPA

Vis-OPA

Experiment



# Nonlinear Optics

---

$$P = \chi_1 \cdot E$$

$$E = E_0 \cos \omega t$$

$$P^{(1)} = \chi_1 \cdot E_0 \cdot \cos(\omega t)$$

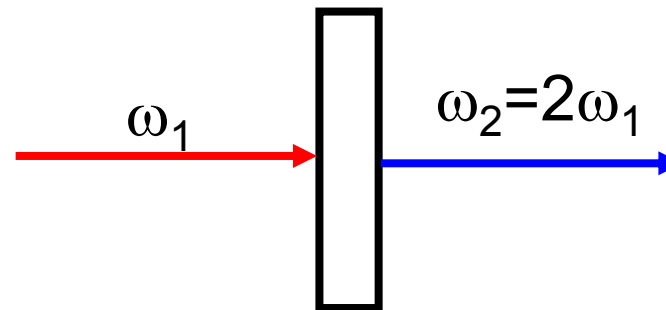
$$P^{(2)} = \chi_2 \cdot E_0^2 \cdot (1 + \cos(2\omega t))$$



# Second Harmonic Generation

---

Nonlinear Crystal







# Nonlinear Optics

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$$P = \chi_1 \cdot E + \chi_2 \cdot E \cdot E + \dots$$

$$E = E_0 \cos \omega_1 t + E_0 \cos \omega_2 t$$

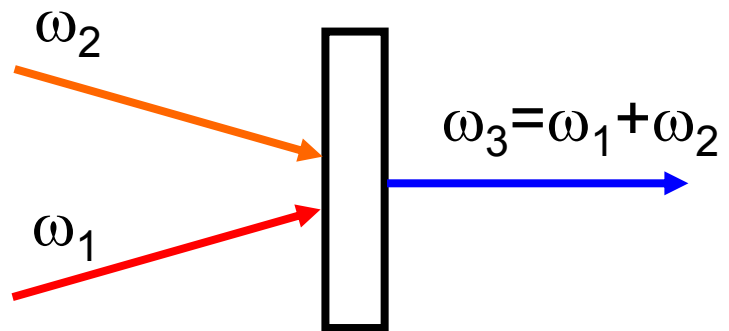
$$P^{(2)} = \chi_2 \cdot E_0^2 \cdot (\cos(\omega_1 + \omega_2)t + \cos(\omega_1 - \omega_2)t)$$



# Sum Frequency Generation

---

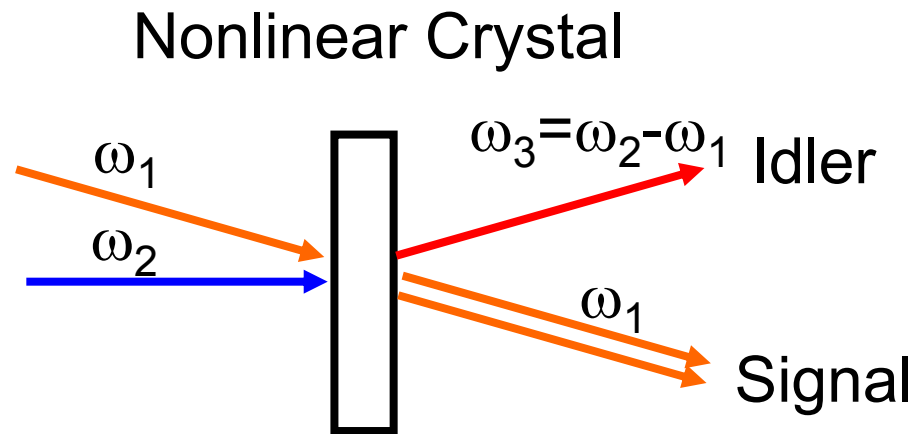
Nonlinear Crystal





# Difference Frequency Mixing

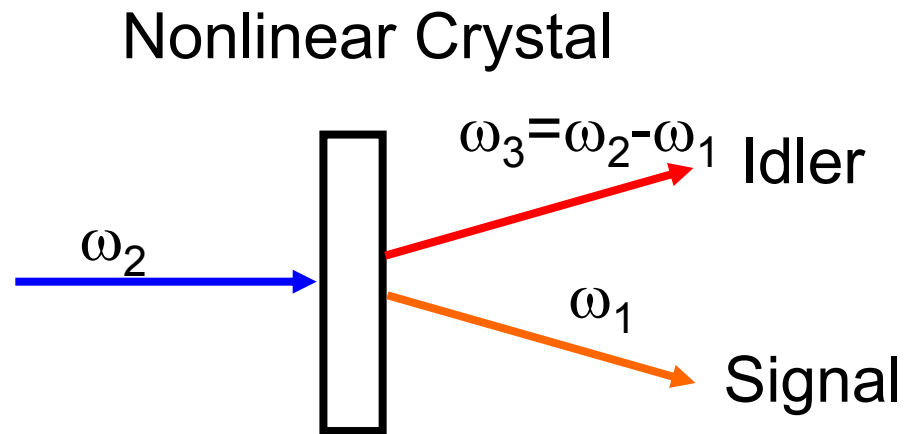
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# Optical Parametrical Process

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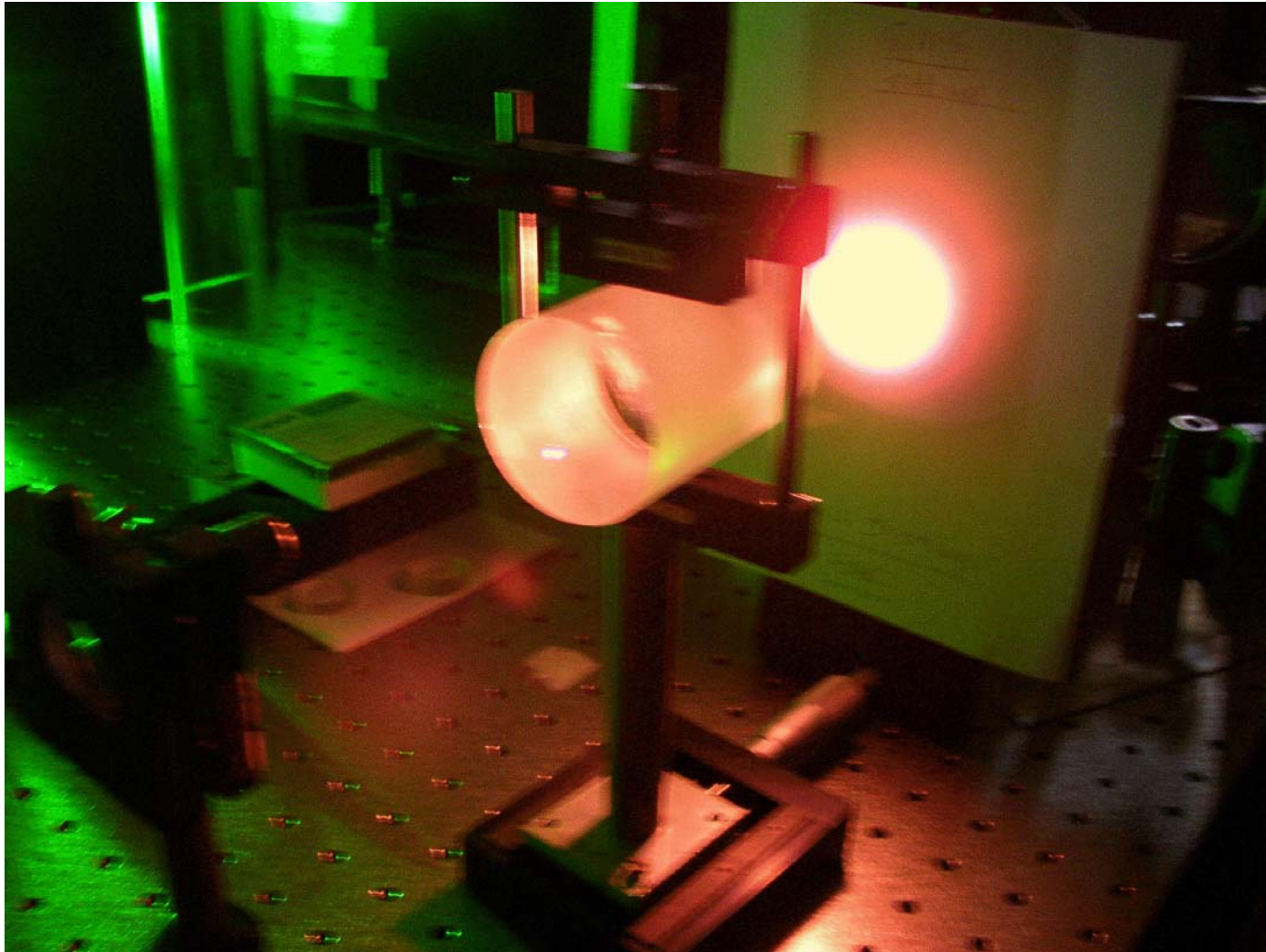






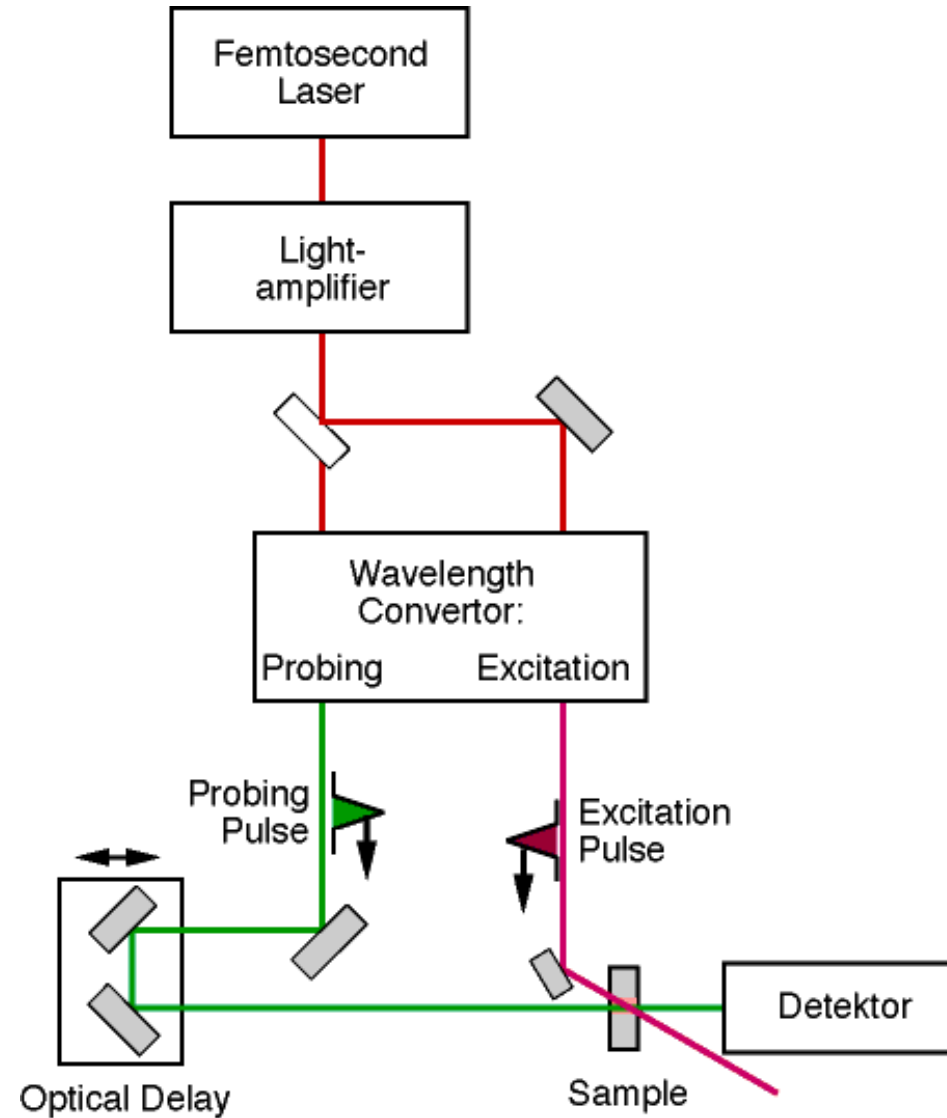
# White-light Generation

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# Pump-Probe Spectroscopy





# Femtochemistry: Basic Concepts

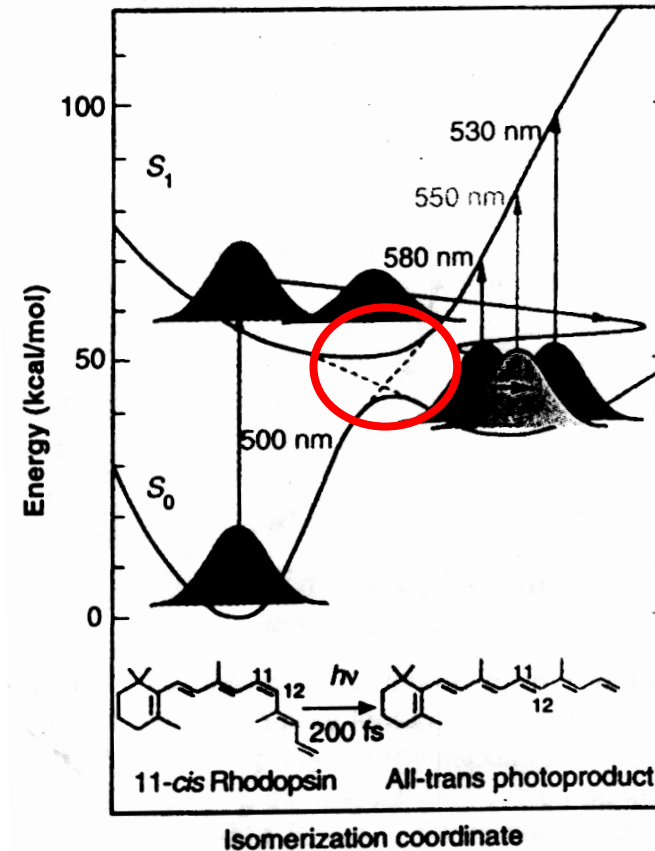
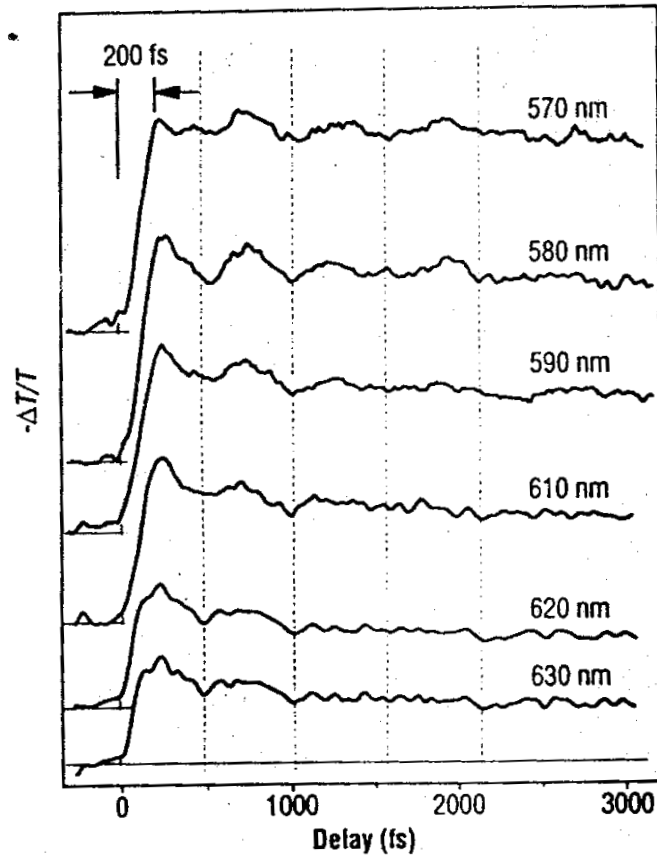
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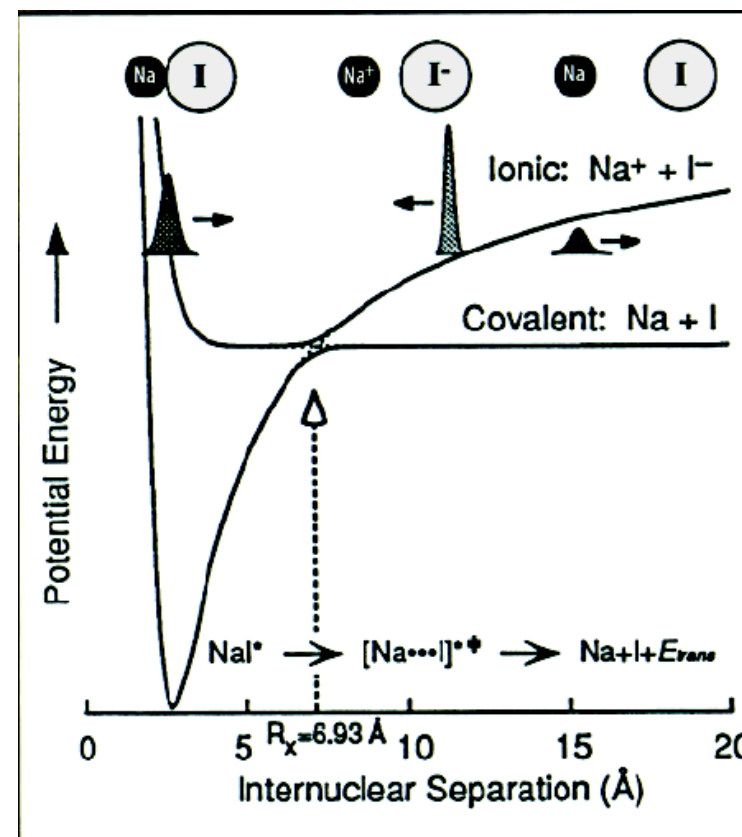
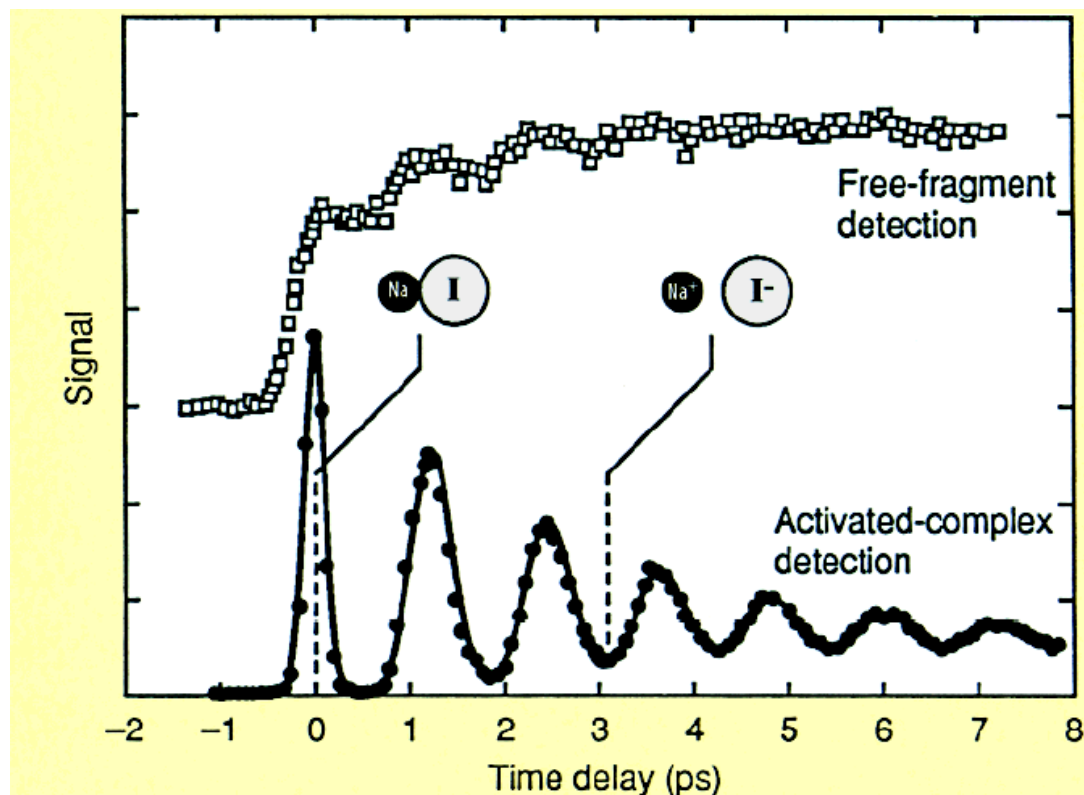
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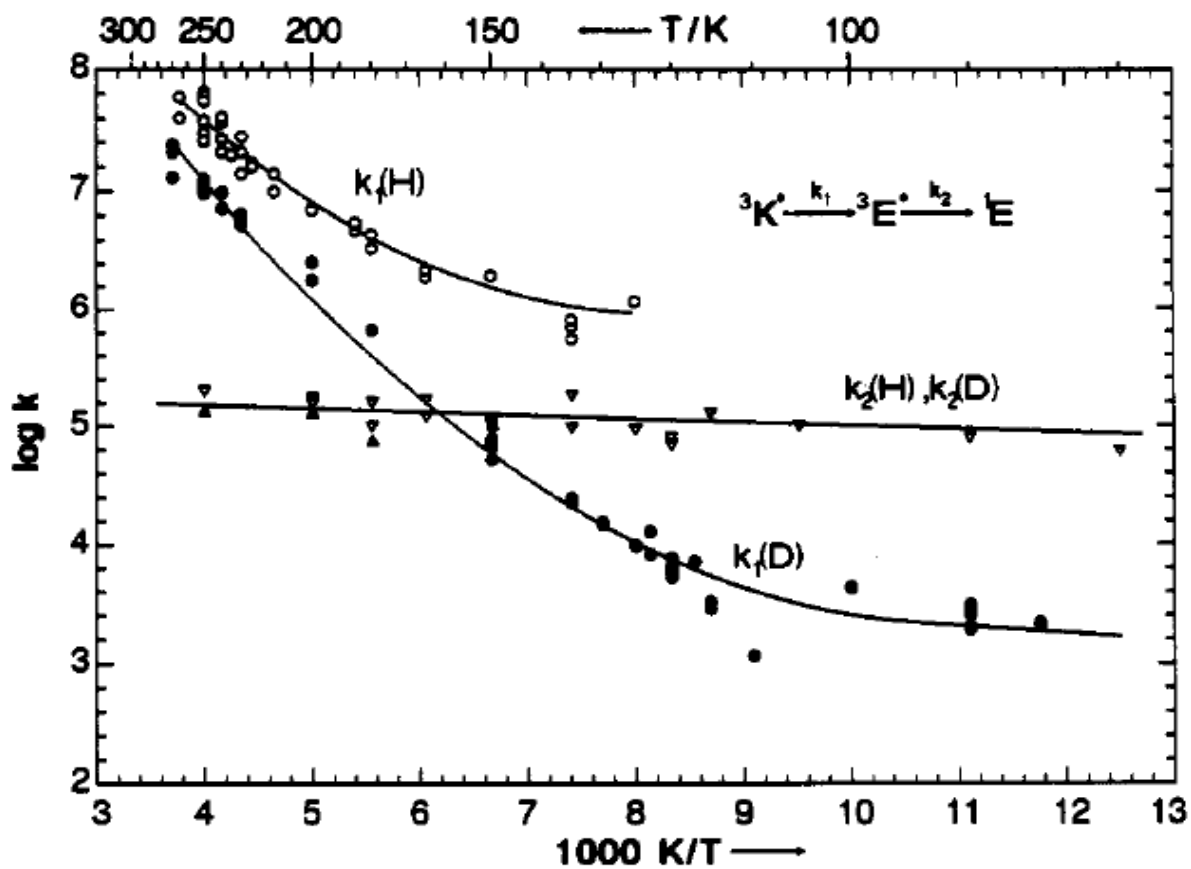
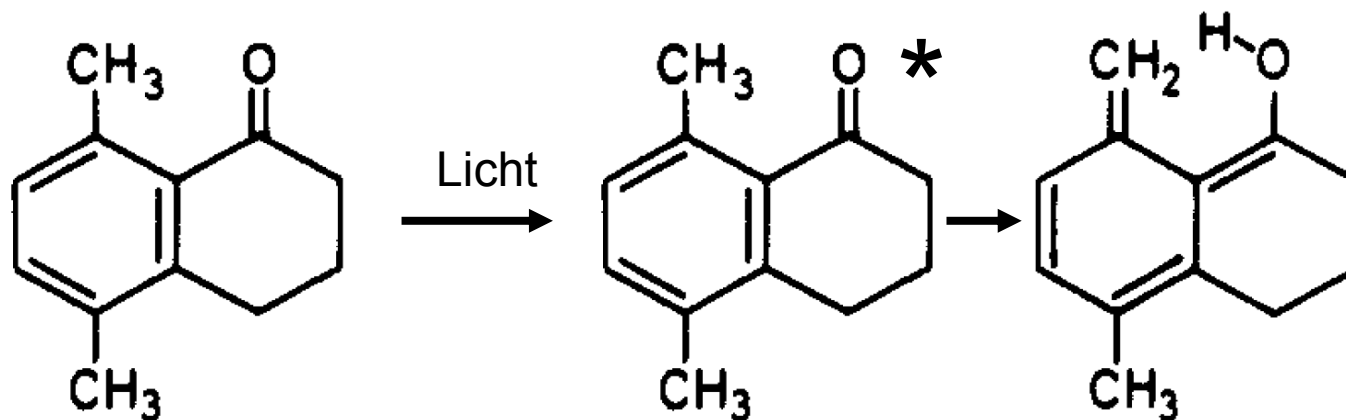
Q. Wang, R. W. Schoenlein, L. A. Peteanu, R. A. Mathies, C. V. Shank,  
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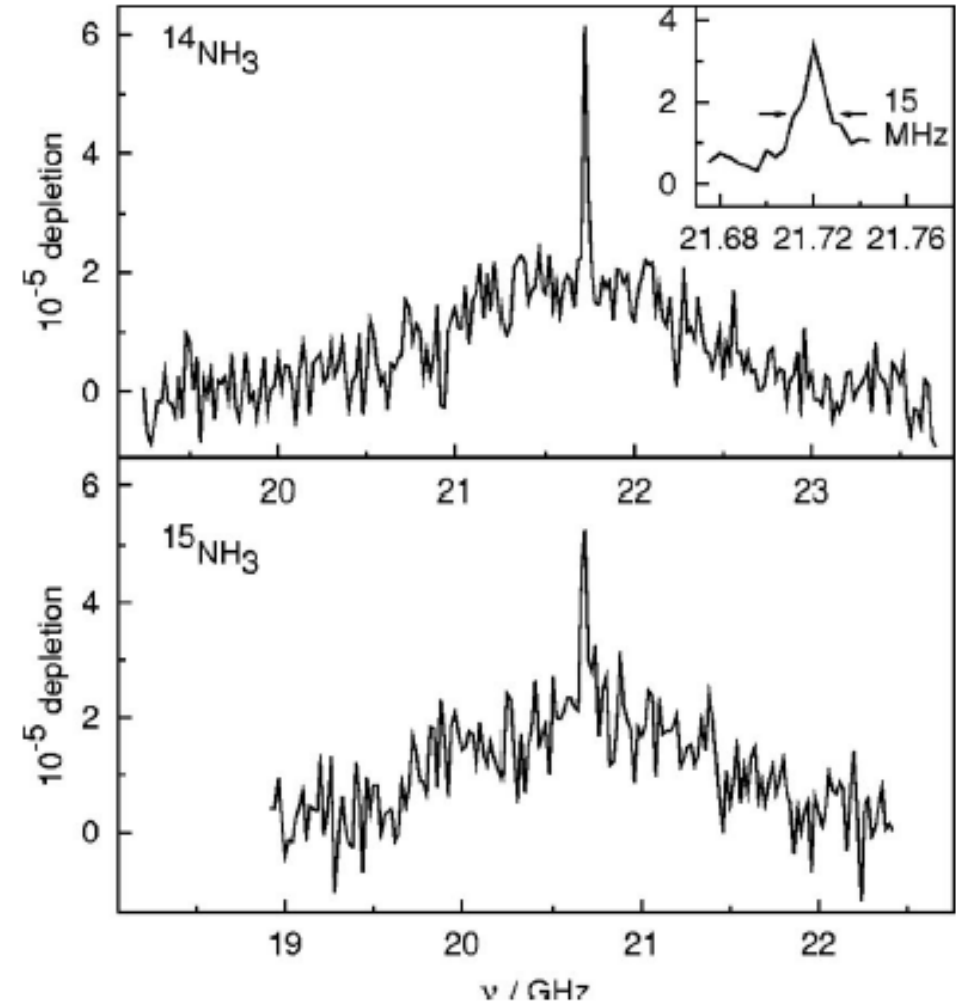
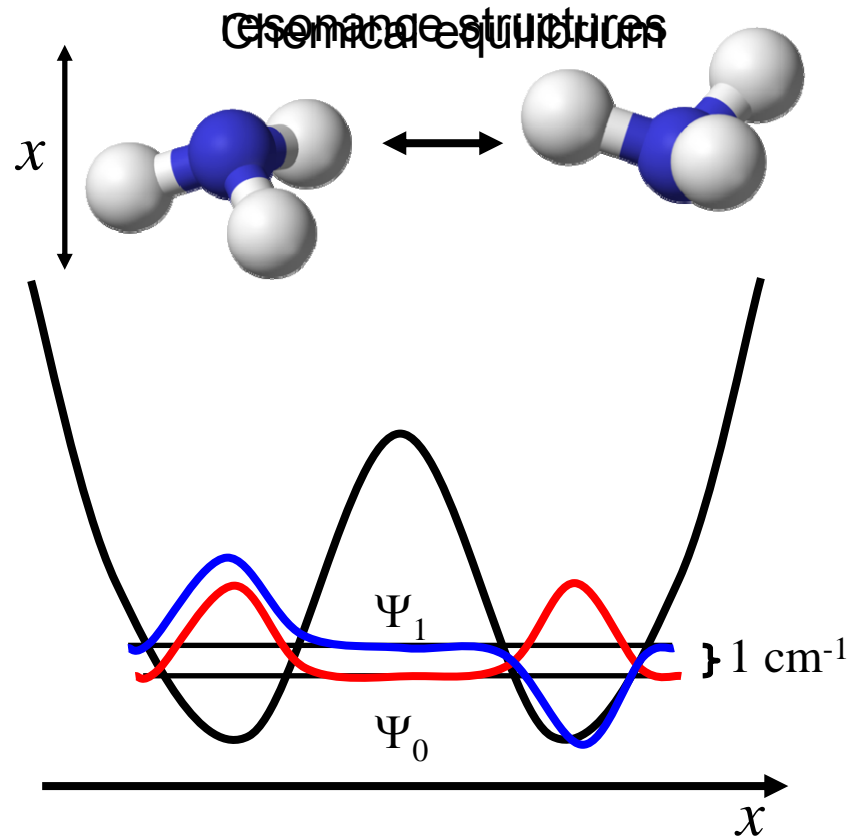
# Prototype Photochemical Reaction: NaI



T. S. Rose, M. J. Rosker, A. H. Zewail, J. Chem. Phys. 91 (1989) 7415  
A. H. Zewail, J. Phys. Chem. A 104 (2000) 5660



# Inversion Tunneling in Ammonia (in He droplets)



# Time-propagating Wavepackets

- in an eigenstate basis:

$$\Psi(t) = \sum \langle \Psi(t=0) | \varphi_i \rangle \varphi_i e^{-i \frac{E_i}{\hbar} t}$$

- direct propagation

$$\Psi(t) = e^{-i \frac{\hat{H}}{\hbar} t} \Psi(t=0)$$

with

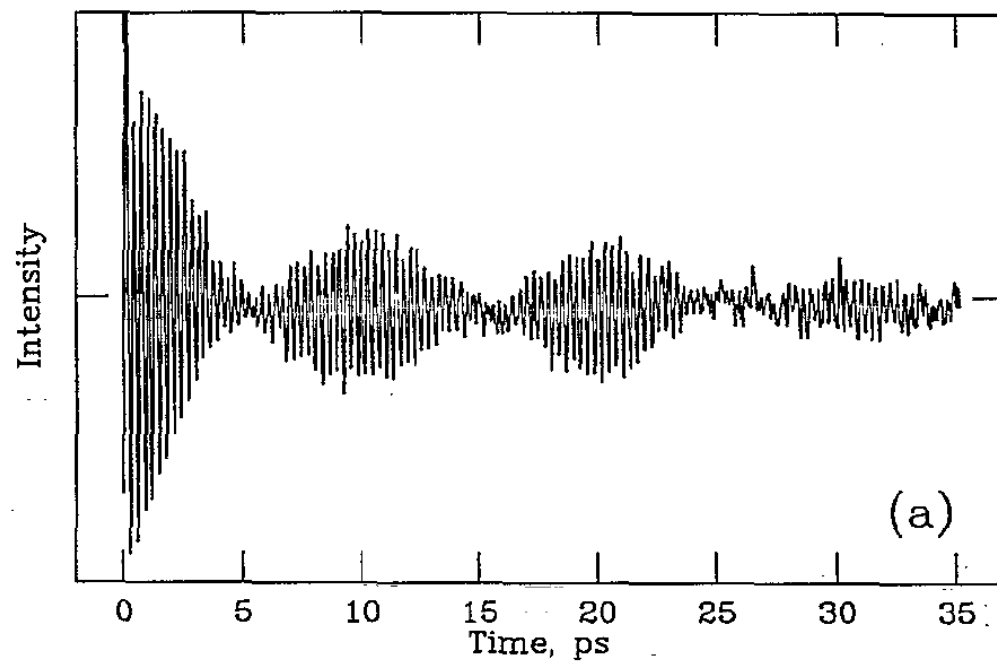
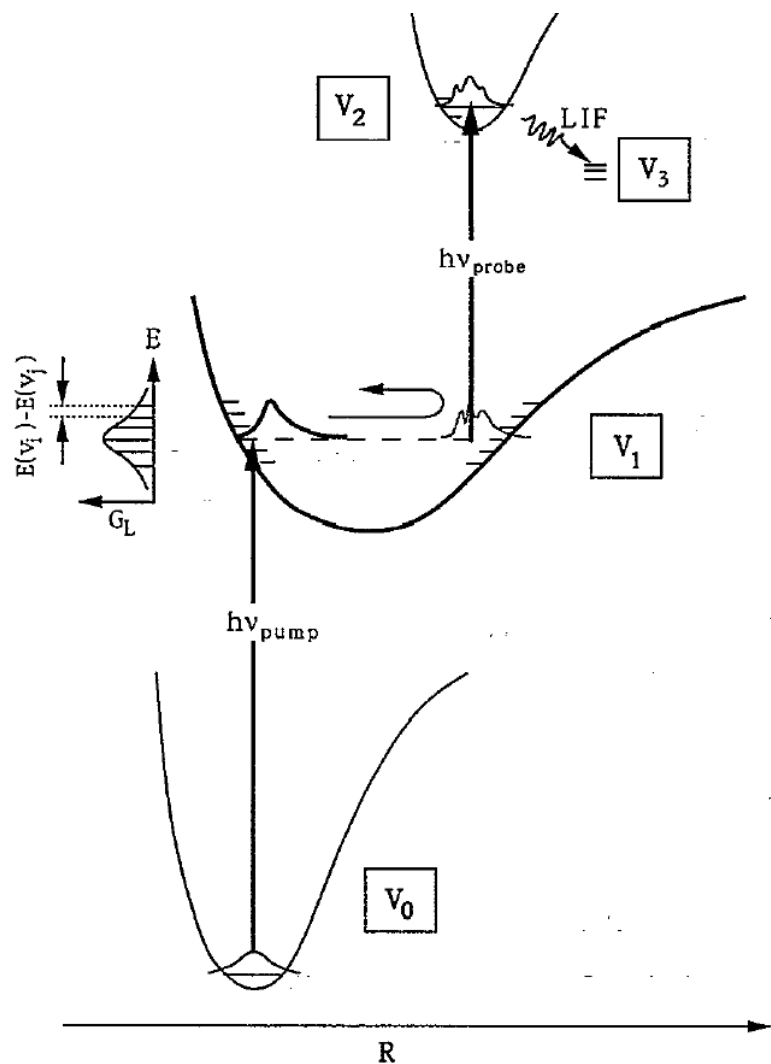
$$e^{-i \frac{\hat{H}}{\hbar} t} \equiv 1 - i \frac{\hat{H}}{\hbar} t - \frac{\hat{H}^2}{\hbar^2} t^2 + \dots$$

- simple numerical scheme by discretizing time

$$\Psi(t + \Delta t) = \Psi(t - \Delta t) - 2i \frac{\hat{H}}{\hbar} \Psi(t) \cdot \Delta t$$



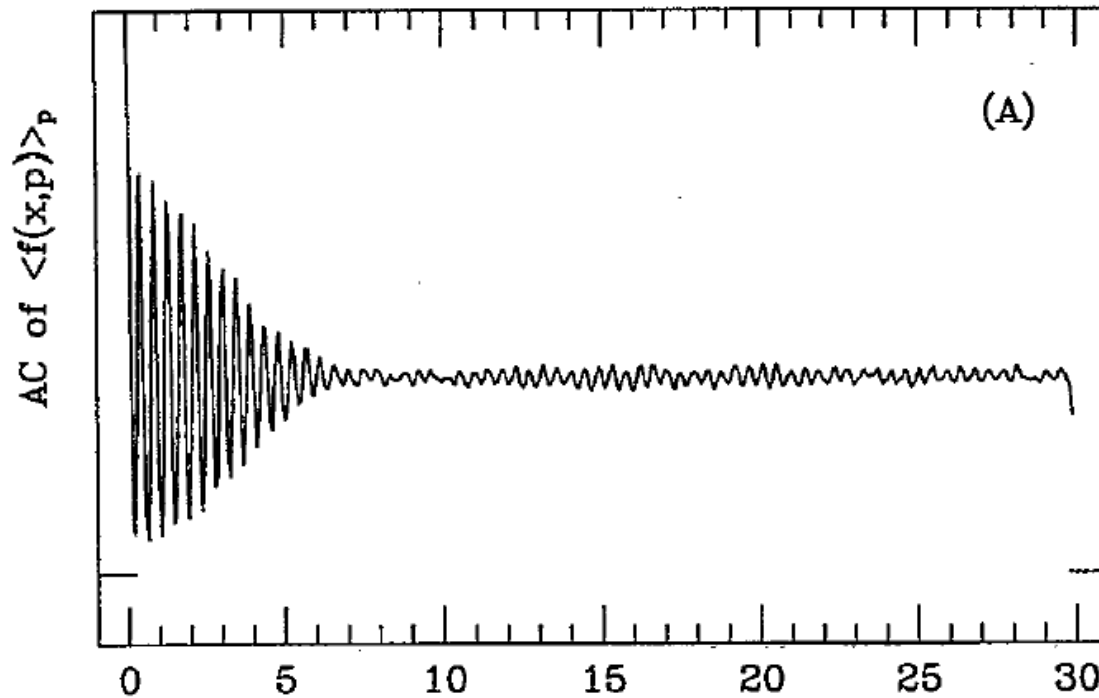
# Motion in Quantum Mechanics: I<sub>2</sub>





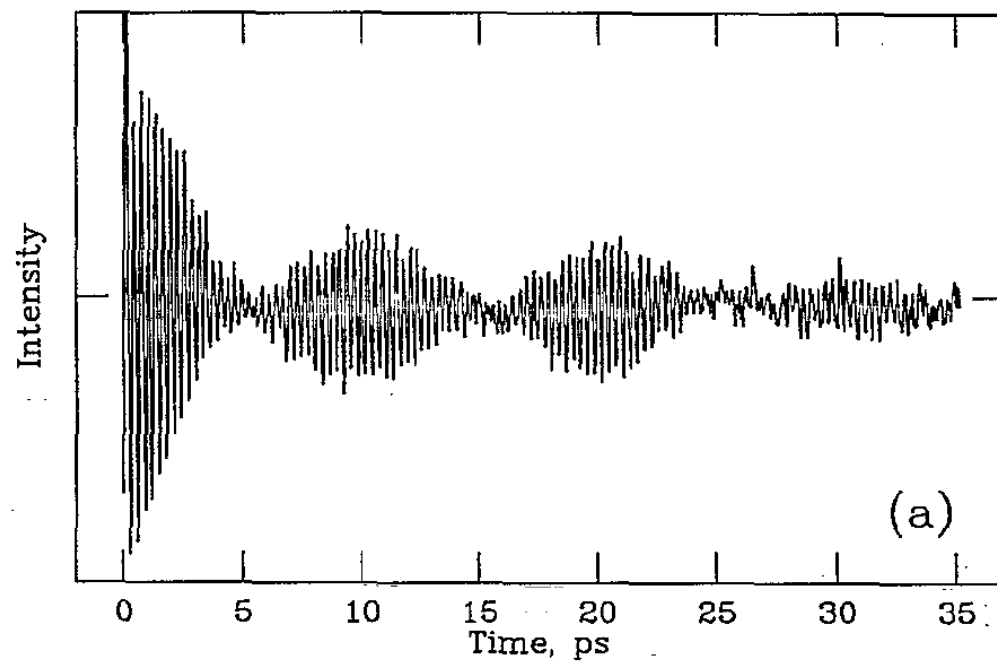
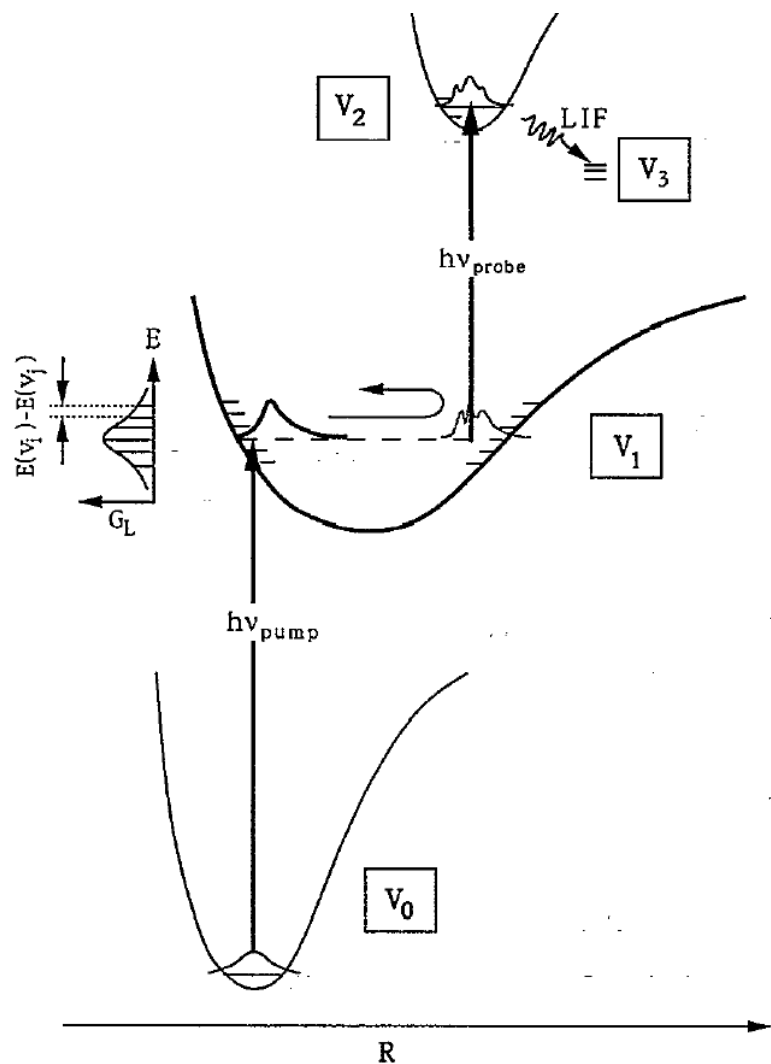
# Wavepackets: I<sub>2</sub>

## Classical Wavepacket





# Motion in Quantum Mechanics: I<sub>2</sub>







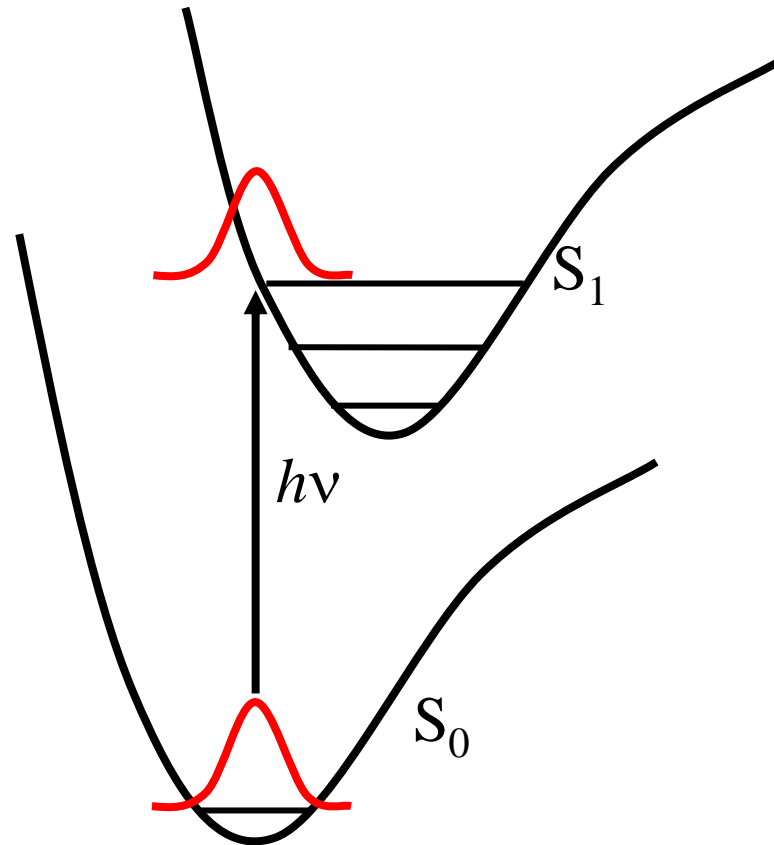
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# Vertical Franck Condon Transition



$$\Psi(t = 0) = \sum_i \langle \phi_0^{(S_0)} | \phi_i^{(S_1)} \rangle \phi_i^{(S_1)}$$

$$\Psi(t = 0) = \phi_0^{(S_0)}$$



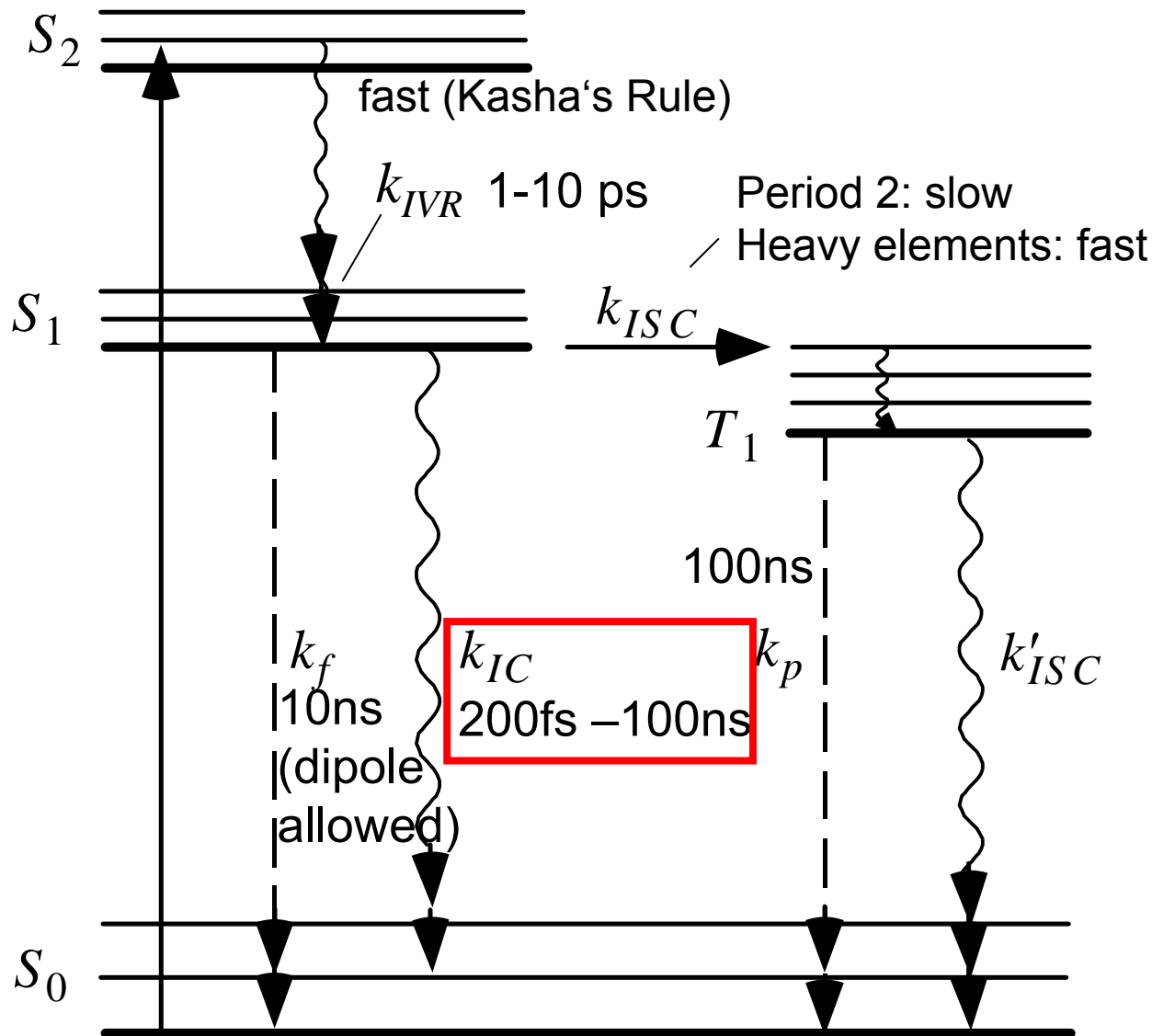
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# Jablonski Diagram



- $k_{IVR}$ : Intramolecular Vibrational Energy Relaxation
- $k_f$ : Fluorescence
- $k_p$ : Phosphorescence
- $k_{IC}$ : Internal conversion (non-radiative decay)
- $k_{ISC}$ : Intersystem Crossing



# Fermi Golden Rule: Derivation

$$\underline{\Phi_i} \xrightarrow{k?} \underline{\Phi_f}$$

$$H = \begin{pmatrix} E_i & V \\ V & E_f \end{pmatrix} \quad \text{with} \quad V = \langle \Phi_i | \hat{V} | \Phi_f \rangle$$

propagating the time-dependent SEQ:

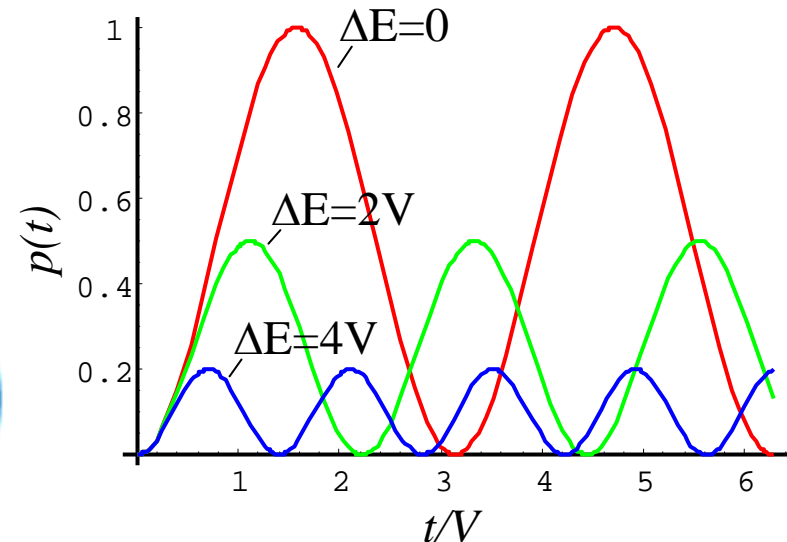
$$p(t) \equiv |\langle \Psi(t) | \Phi_i \rangle|^2 = c_f^2 = \sin^2 \left( \frac{V}{\hbar} t \right)$$

same for non-resonant states:

$$p(t) = \frac{4V^2}{\Delta E^2 + 4V^2} \sin^2 \left( \frac{\sqrt{\Delta E^2 + 4V^2}}{2\hbar} t \right)$$

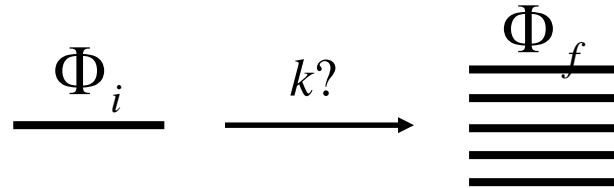
with  $V \ll \Delta E$

$$p(t) = \frac{4V^2}{\Delta E^2} \sin^2 \left( \frac{\Delta E}{2\hbar} t \right)$$





# Fermi Golden Rule: Derivation

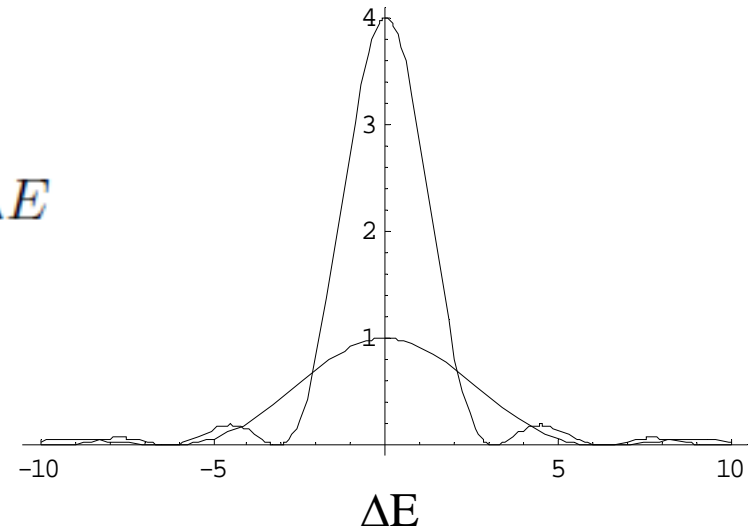


relaxation into a continuum of states:

$$P(t) = \int_{-\infty}^{\infty} p(t) \rho(E) d\Delta E$$

$$P(t) = \rho(E) V^2 \int_{-\infty}^{\infty} \frac{4 \sin^2 \Delta E / (2\hbar)t}{\Delta E^2} d\Delta E$$

$$P(t) = \frac{2\pi}{\hbar} \rho(E) V^2 t$$





# Fermi Golden Rule

---

$$k_{if} = \frac{2\pi}{\hbar} V_{if}^2 \delta(\Delta E)$$

or

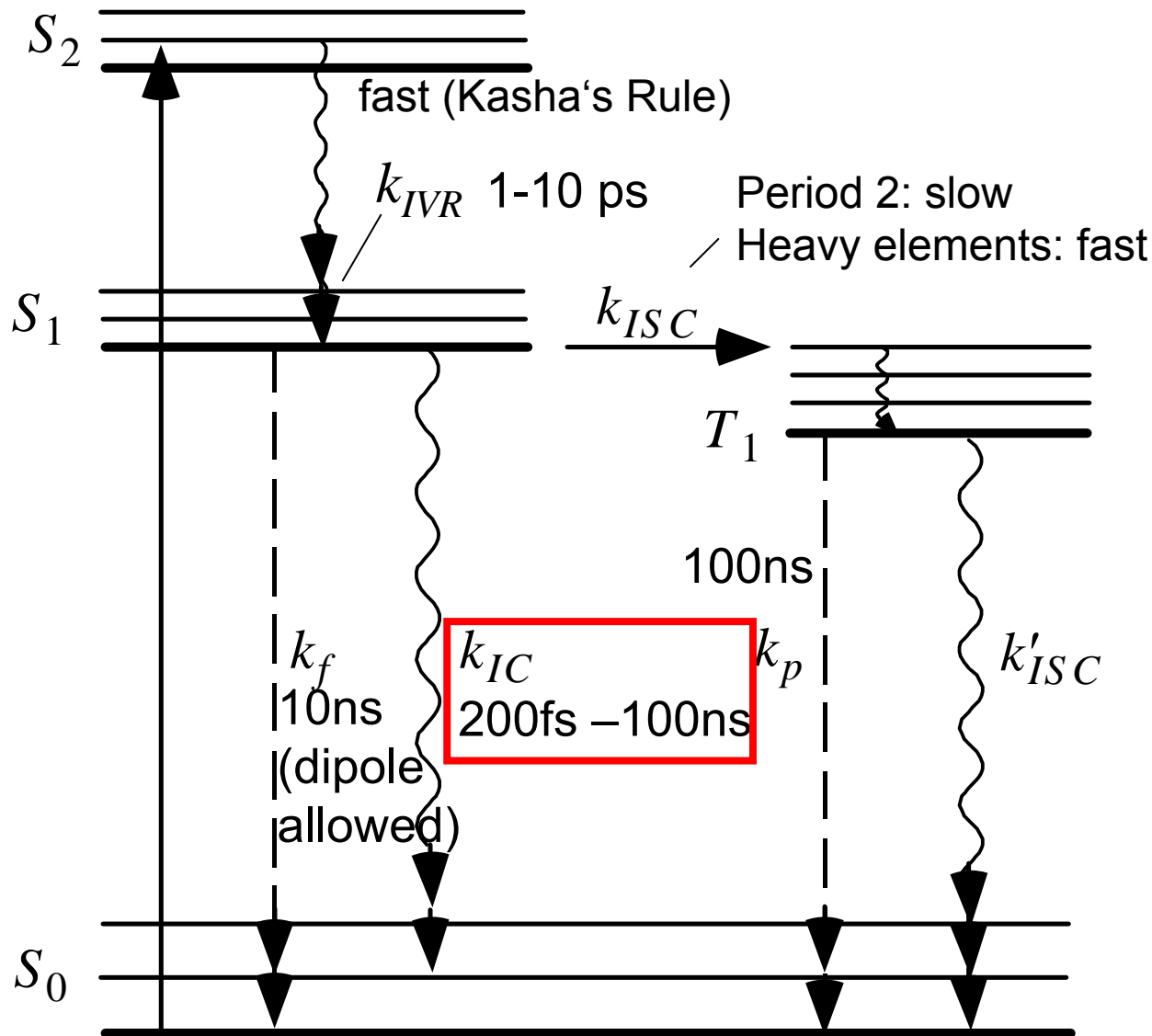
$$k_{if} = \frac{2\pi}{\hbar} V_{if}^2 \rho(E)$$

with

$$V_{if} = \langle \Phi_i | V | \Phi_f \rangle$$



# Jablonski Diagram

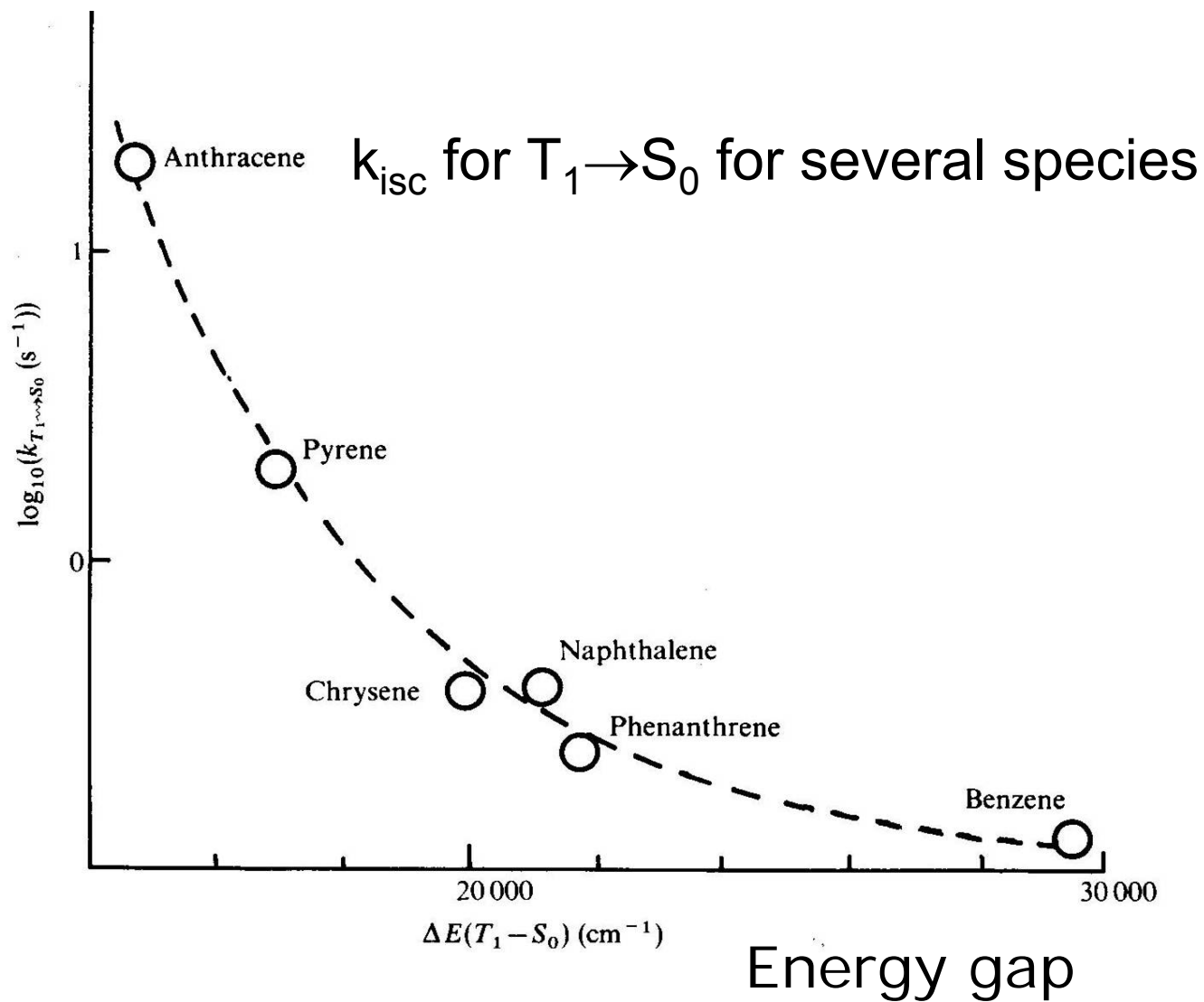


- $k_{IVR}$ : Intramolecular Vibrational Energy Relaxation
- $k_f$ : Fluorescence
- $k_p$ : Phosphorescence
- $k_{IC}$ : Internal conversion (non-radiative decay)
- $k_{ISC}$ : Intersystem Crossing





# Energy Gap Law





# Internal Conversion or Non-Radiative Decay

---

$$k_{if} = \frac{2\pi}{\hbar} V_{if}^2 \delta(\Delta E)$$

$$V_{if} = \langle \Phi_i | V | \Phi_f \rangle$$

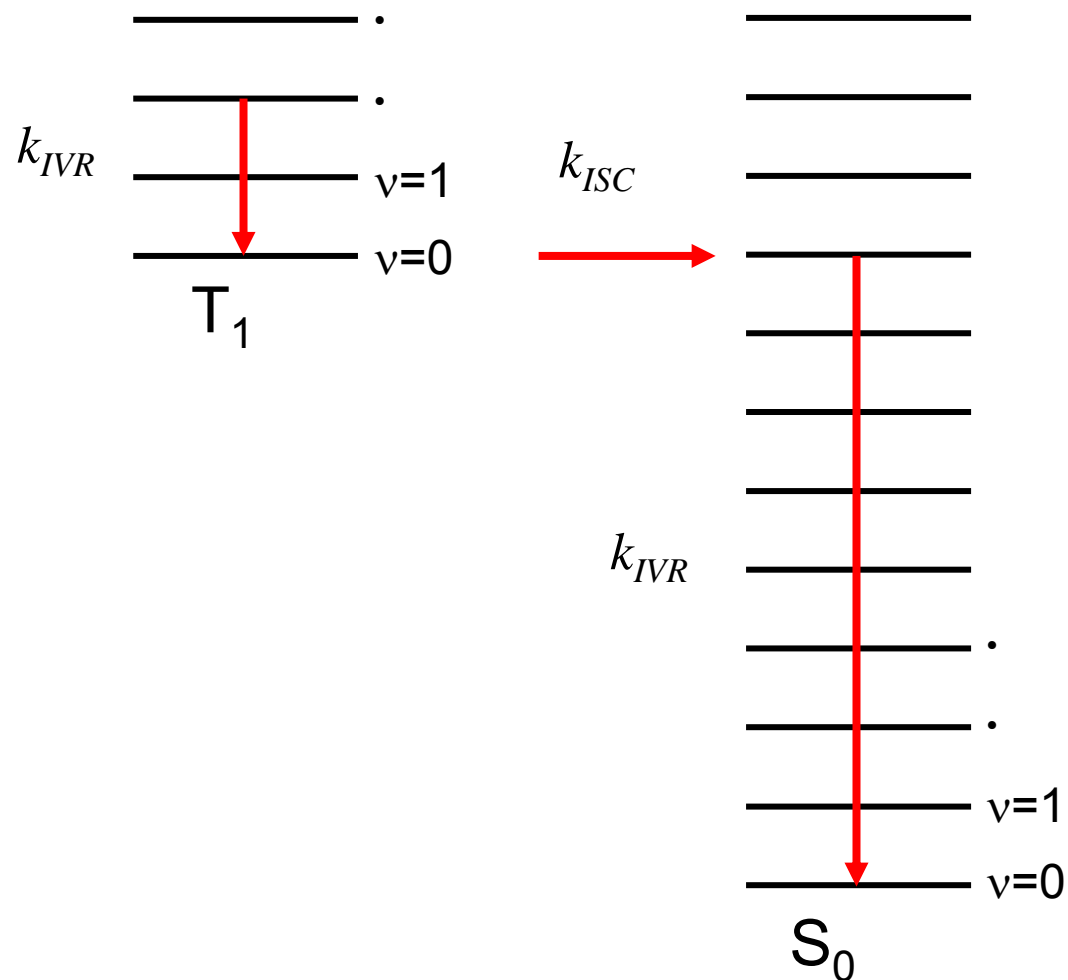
$$\Phi(R, r) = \underbrace{\Psi_{el}(r; R)}_{\text{electronic}} \underbrace{\chi_{nuc}(R)}_{\text{nuclear}}$$

$$V_{if} = \langle \Psi_i | V_{el} | \Psi_f \rangle \langle \chi_i | \chi_f \rangle$$

Franck-Condon Factor

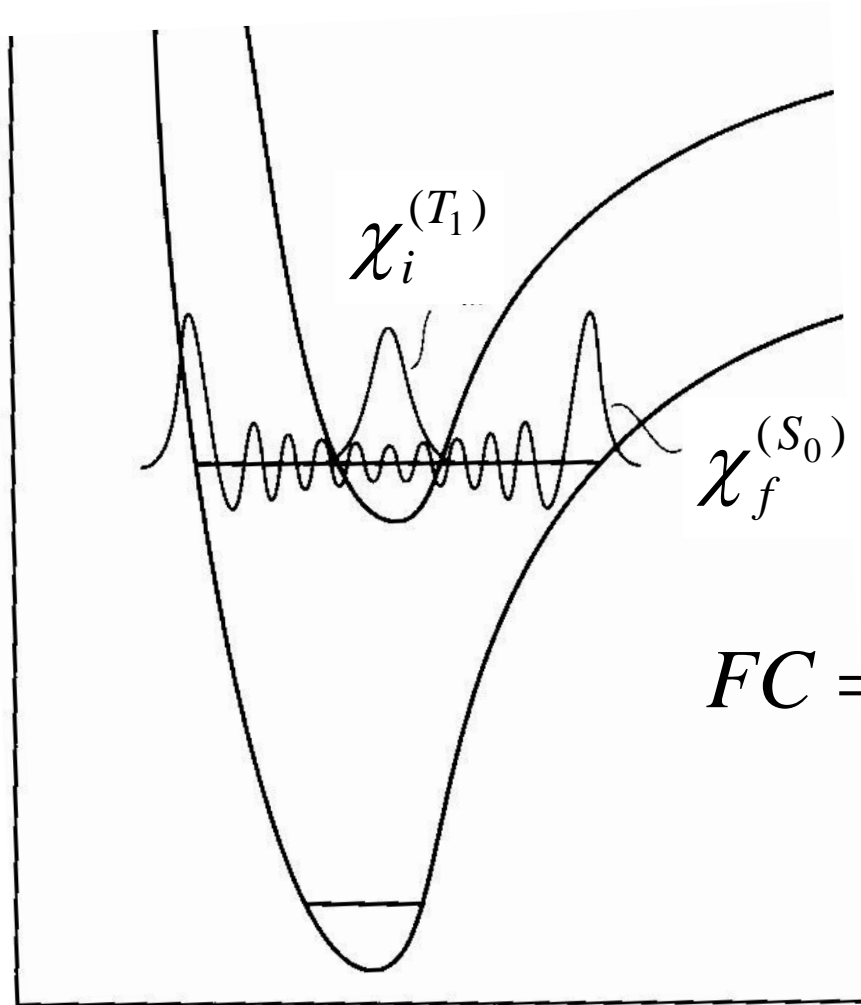


# Internal Conversion or Non-Radiative Decay





# Internal Conversion or Non-Radiative Decay

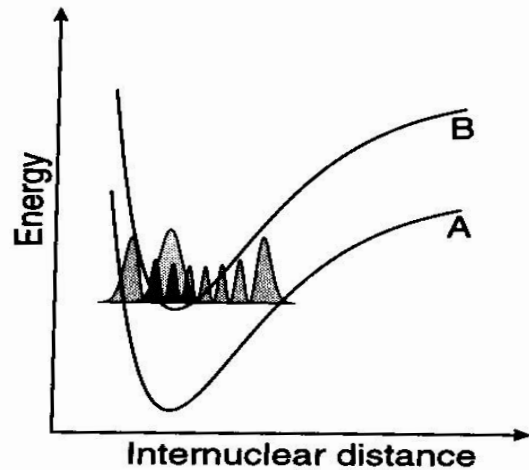


$$FC = \left\langle \chi_i^{(T_1)} \left| \chi_f^{(S_0)} \right. \right\rangle$$



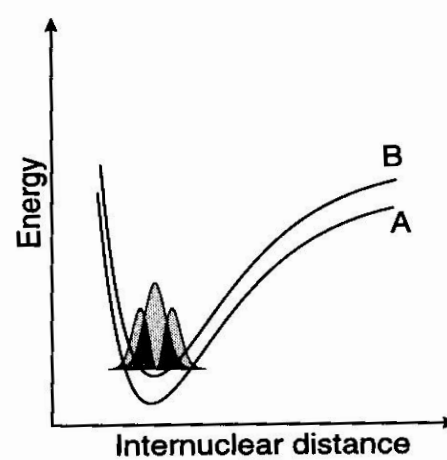
# Internal Conversion or Non-Radiative Decay

Poor overlap

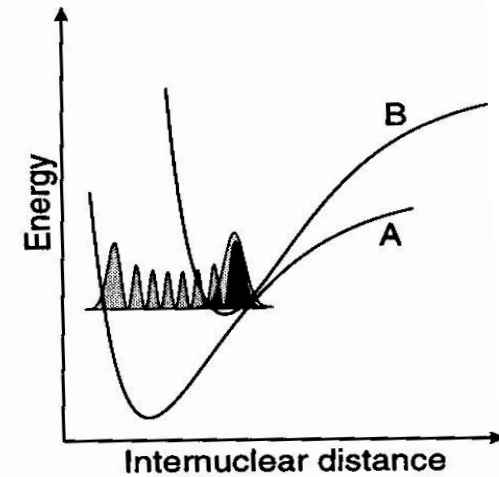


(a) Similar geometry, with large energy separation.

Better overlap



(b) Similar geometry, with small energy separation.



(c) Different geometry, with large energy separation.



# Energy Gap Law

Rates of  $T_1 - S_0$  intersystem crossing

M	$10^{-4} k''_{ISC}/s^{-1}$	$\tau_p/s$
Benzene	17.6	4.75
Benzene-d <sub>1</sub>	16.0	5.15
Benzene-d <sub>5</sub>	7.1	9.50
Benzene-d <sub>6</sub>	3.7	14.1

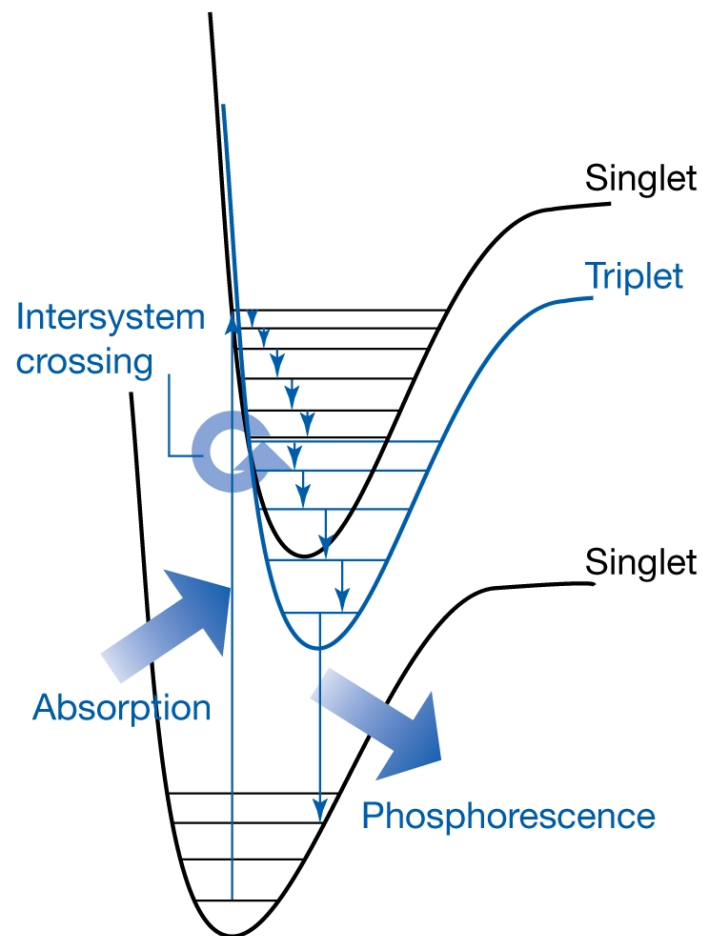
The vibrational frequency of deuterium substituted compounds is lower than unsubstituted

Thus higher quantum numbers (more nodes) involved in final state for same energy gap – poorer overlap.



# Energy Gap Law

- Rate of intramolecular energy transfer decreases with increasing energy gap
- Usually  $S_1-T_1 < T_1-S_0 < S_1-S_0$
- Thus this factor tends to make ISC faster than IC

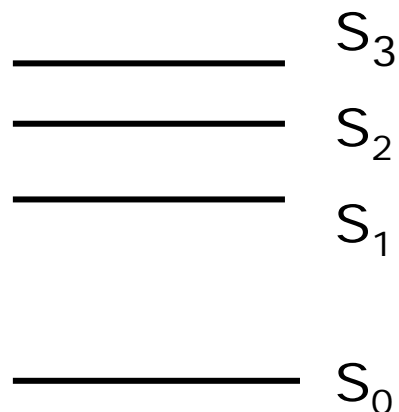




# Kasha's Rule

---

- Emission from the lowest excited state  $S_1$ .
- Consequence of energy gap law (FC factor)
- In general  $E(S_2) - E(S_1) \ll E(S_1) - E(S_0)$



Thus fast internal  
conversion  
between higher  
singlet states





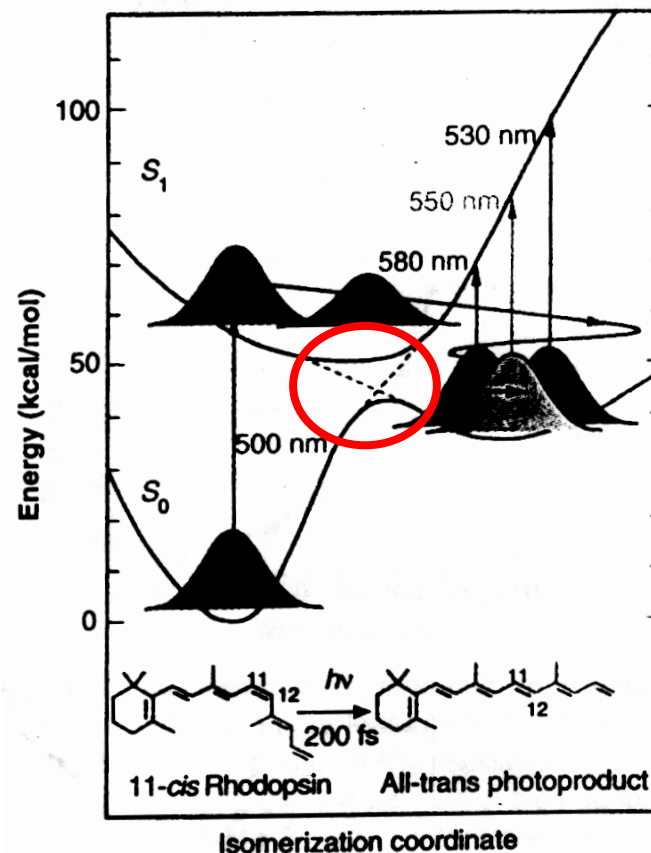
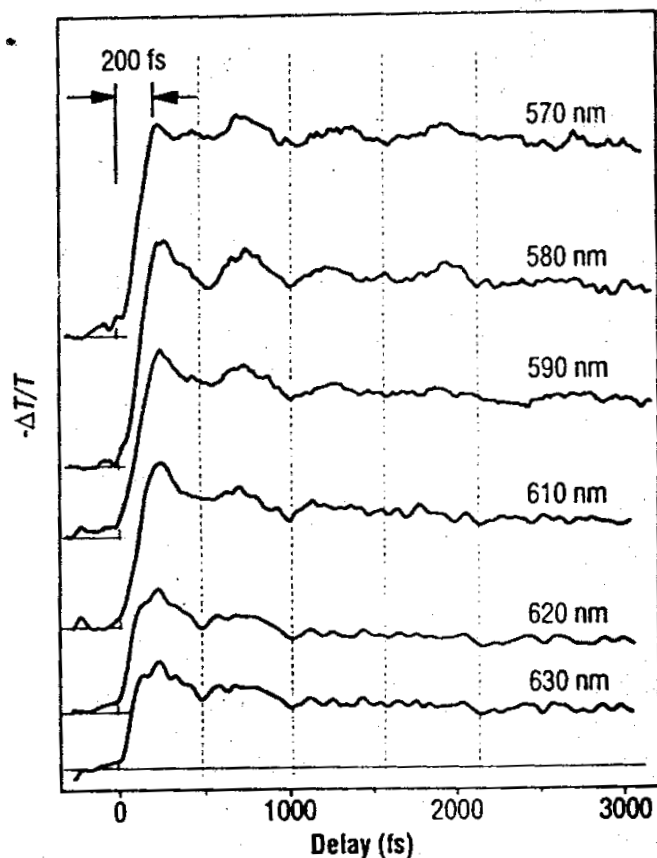
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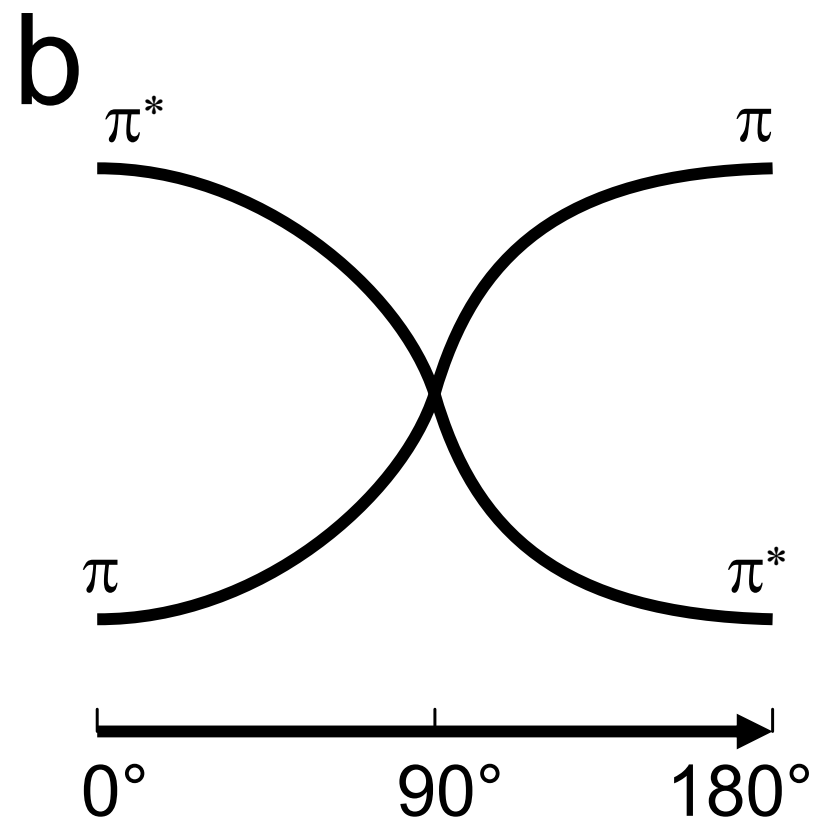
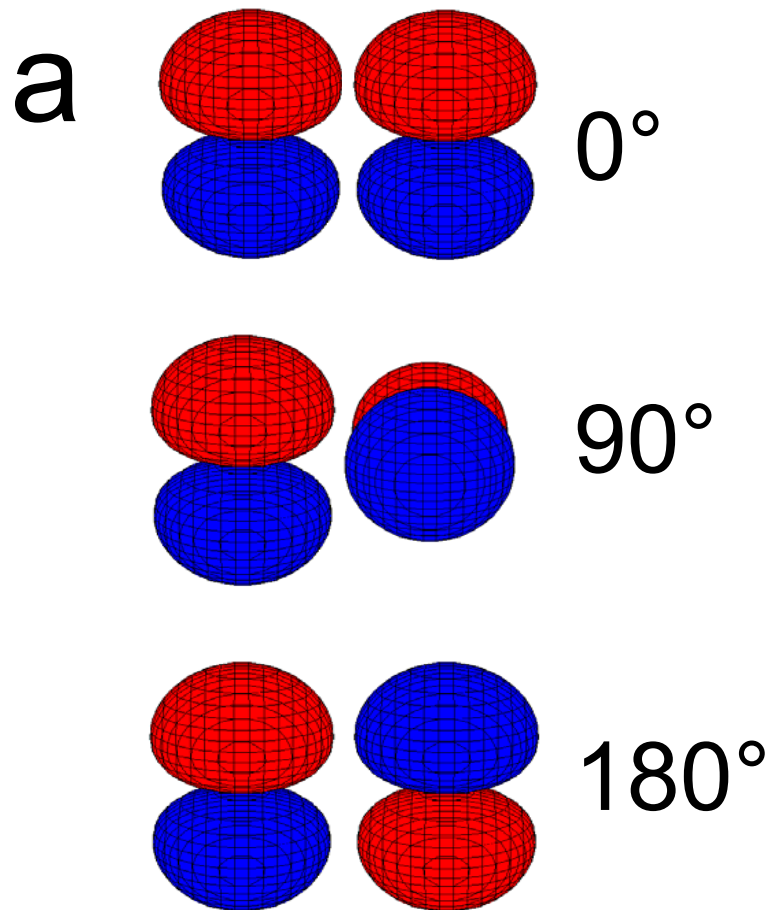
# Photochemical Reactions in Nature: Isomerization of Rhodopsin



Q. Wang, R. W. Schoenlein, L. A. Peteanu, R. A. Mathies, C. V. Shank,  
Science 266 (1994) 422

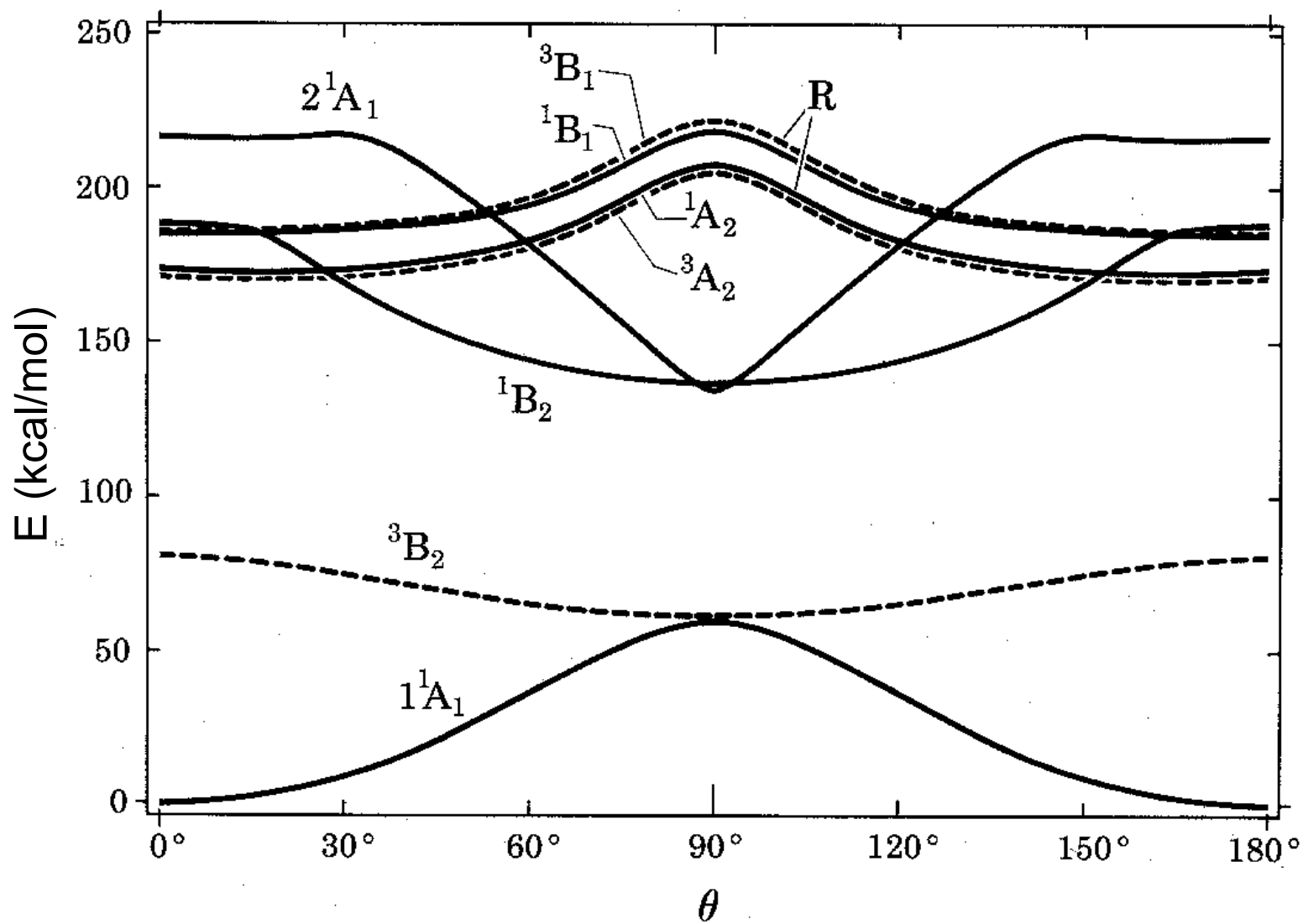


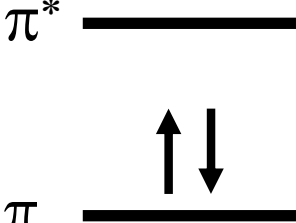
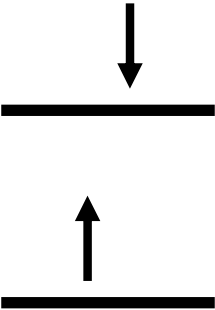
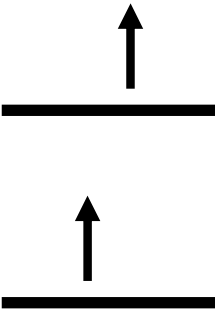
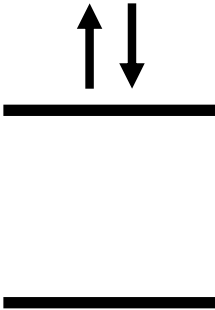
# Ethylene: MO picture





# Ethylene: Large Scale CI



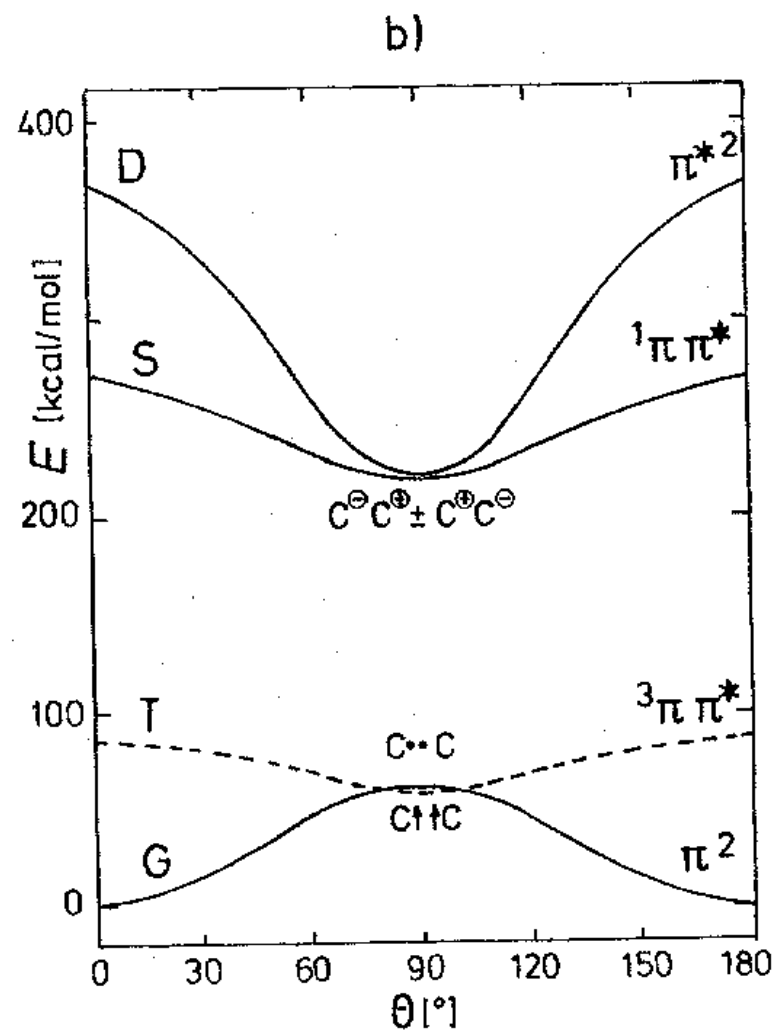
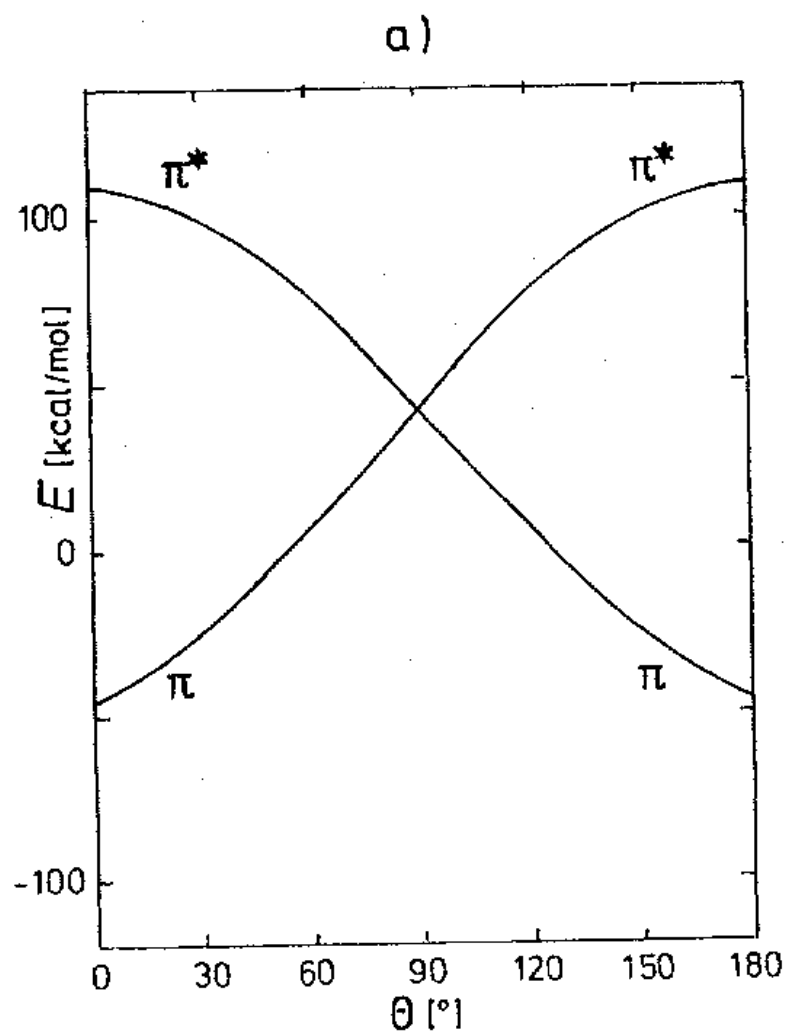
	$\Psi_1$ 	$\Psi_2$ 	$\Psi_3$ 	$\Psi_4$ 
spatial part	$\pi(1)\pi(2)$ symmetric under particle exchange	$\pi(1)\pi^*(2) +$ $\pi(2)\pi^*(1)$ symmetric	$\pi(1)\pi^*(2) -$ $\pi(2)\pi^*(1)$ antisymmetric	$\pi^*(1)\pi^*(2)$ symmetric
spin part	$\alpha(1)\beta(2) - \alpha(2)\beta(1)$	$\alpha(1)\beta(2) - \alpha(2)\beta(1)$	$\alpha(1)\alpha(2)$ $b(1)b(2)$ $\alpha(1)\beta(2) + \alpha(2)\beta(1)$	$\alpha(1)\beta(2) - \alpha(2)\beta(1)$
	Singlet ${}^1A_1$	Singlet ${}^1B_2$	Triplet ${}^3B_2$	Singlet ${}^1A_1$

Symmetric case:  $\{\Psi_1, \Psi_4\}$  couple

Asymmetric case:  $\{\Psi_1, \Psi_2, \Psi_4\}$  couple  $\longrightarrow$  3x3 CI Model

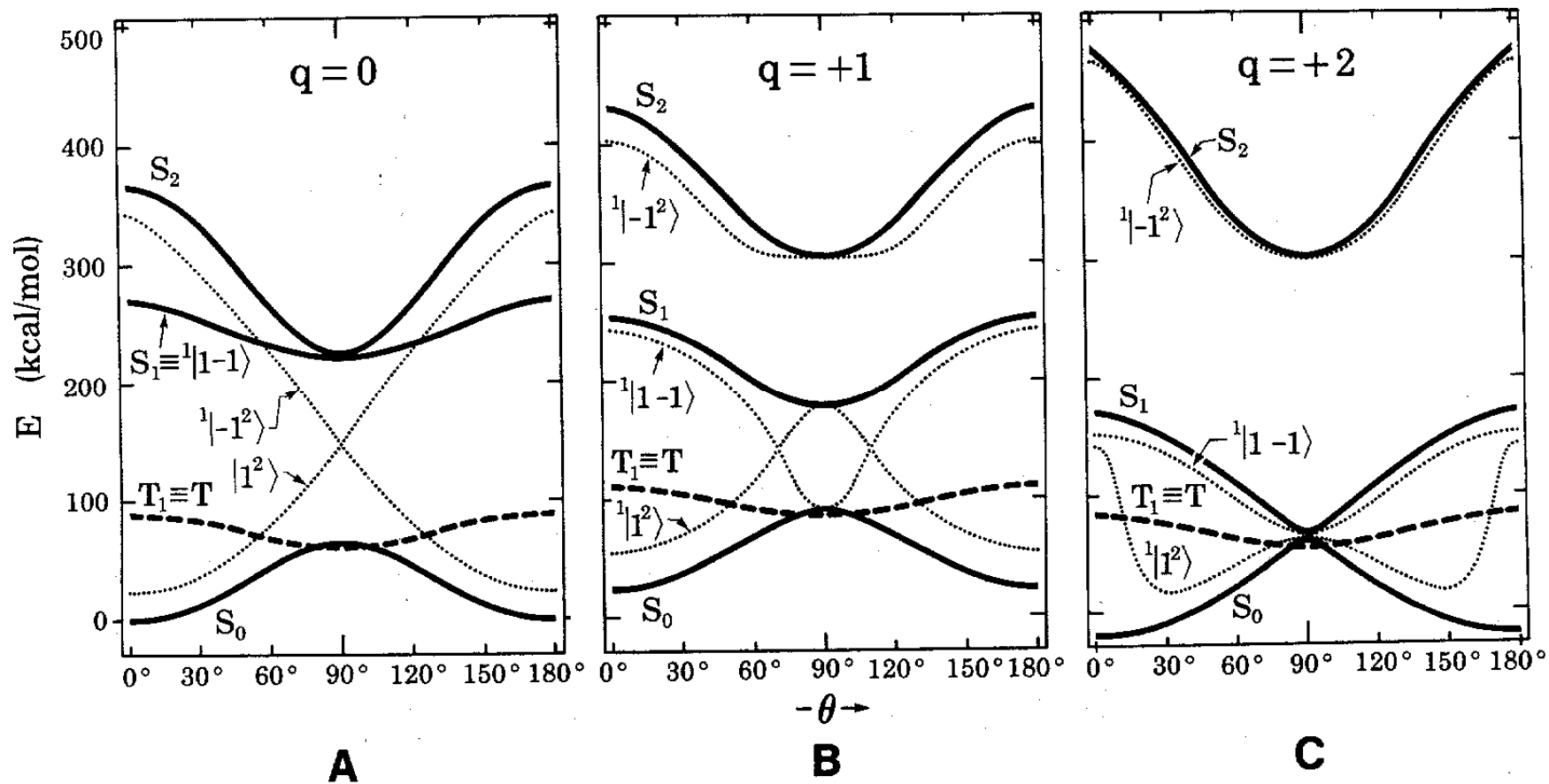


# Prototype Isomerization: Ethylene



# Breaking the Symmetry

Charge 1.85 Å away along the C=C axis

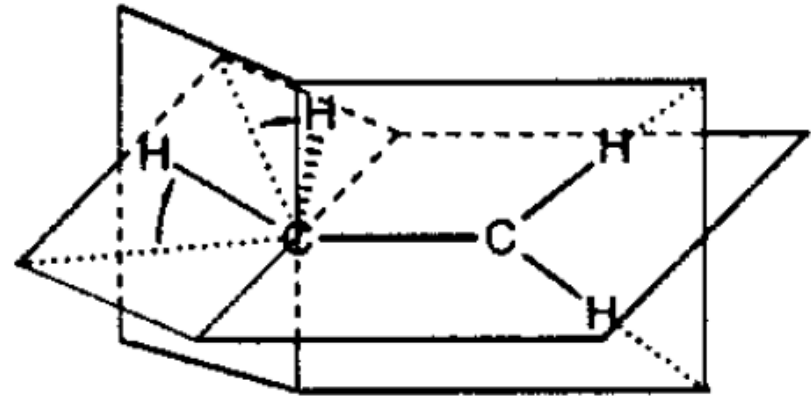
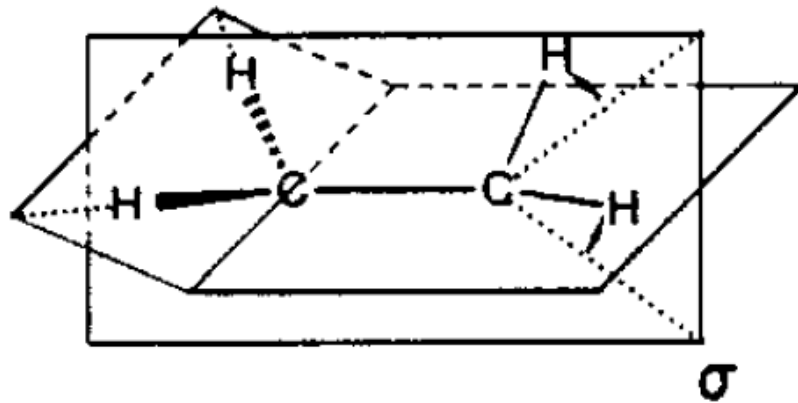


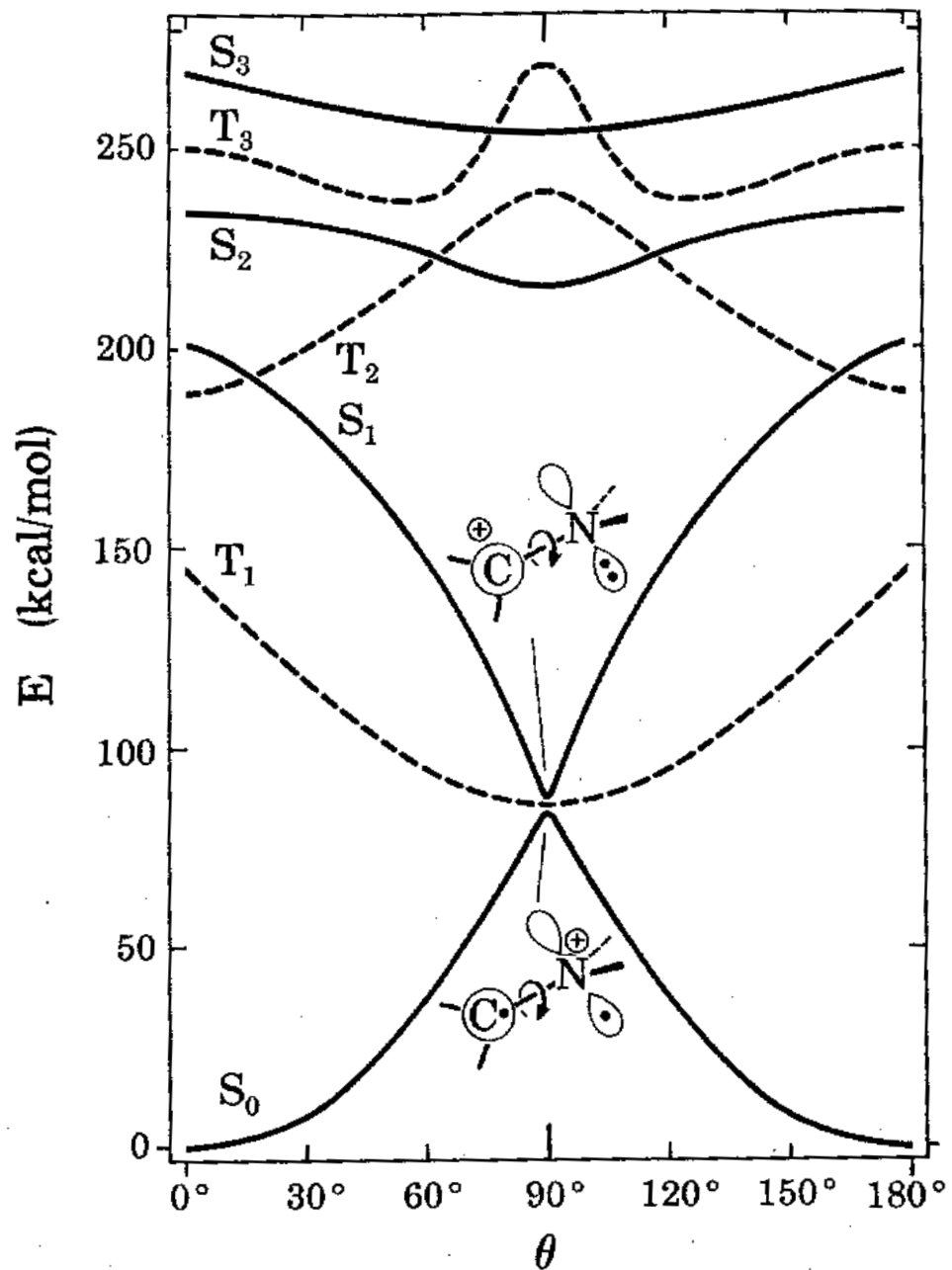
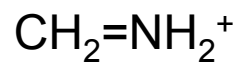




# Prototype Isomerization: Ethylene

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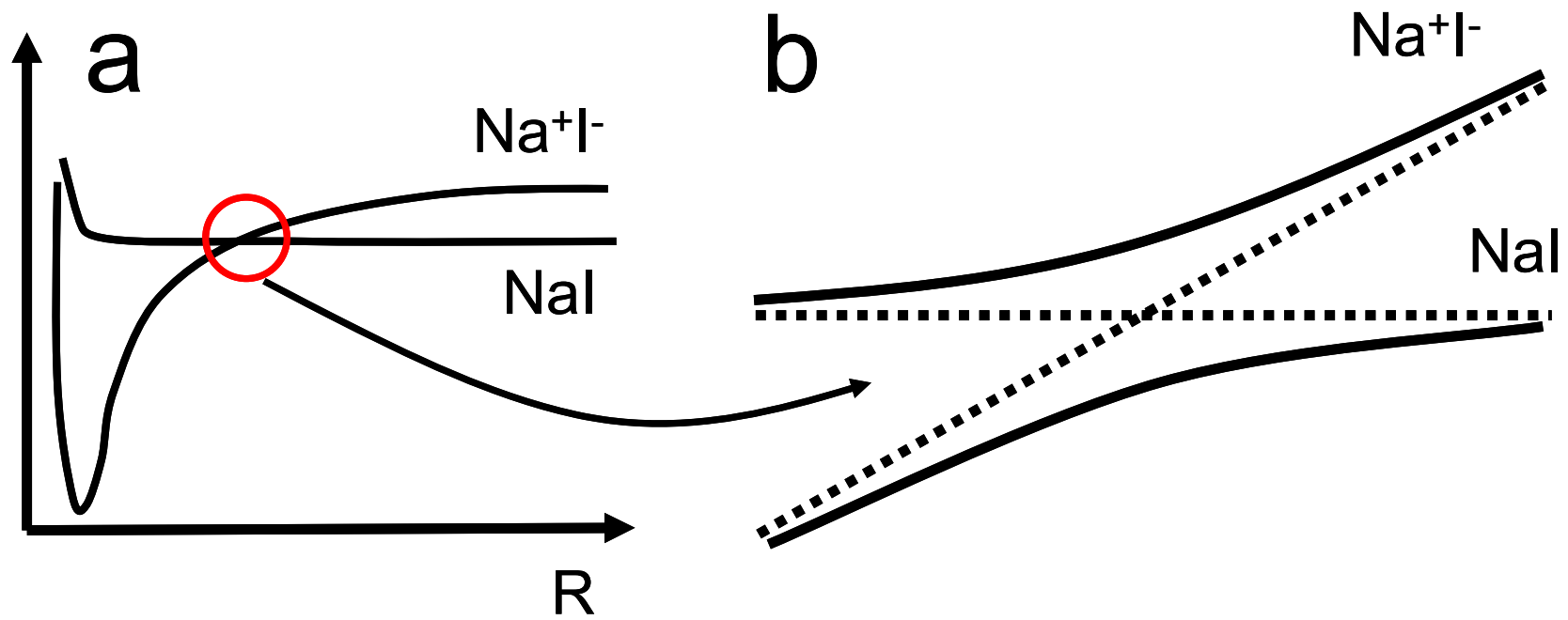
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# Ionic Bond





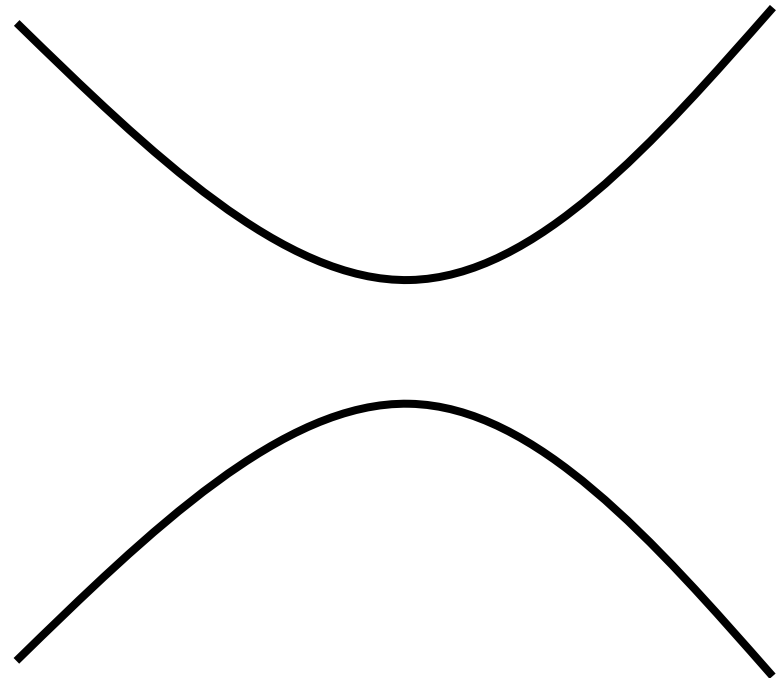
# Avoided Crossing, Non-crossing Rule

---

$$H(R) = \begin{pmatrix} H_{11}(R) & H_{12}(R) \\ H_{21}(R) & H_{22}(R) \end{pmatrix}$$

Two surfaces cross when:

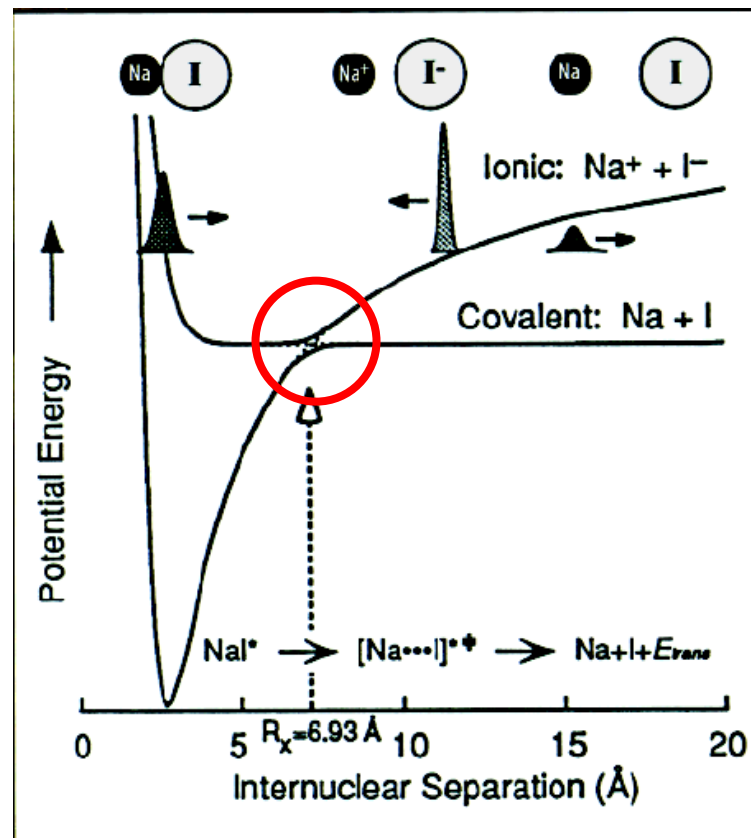
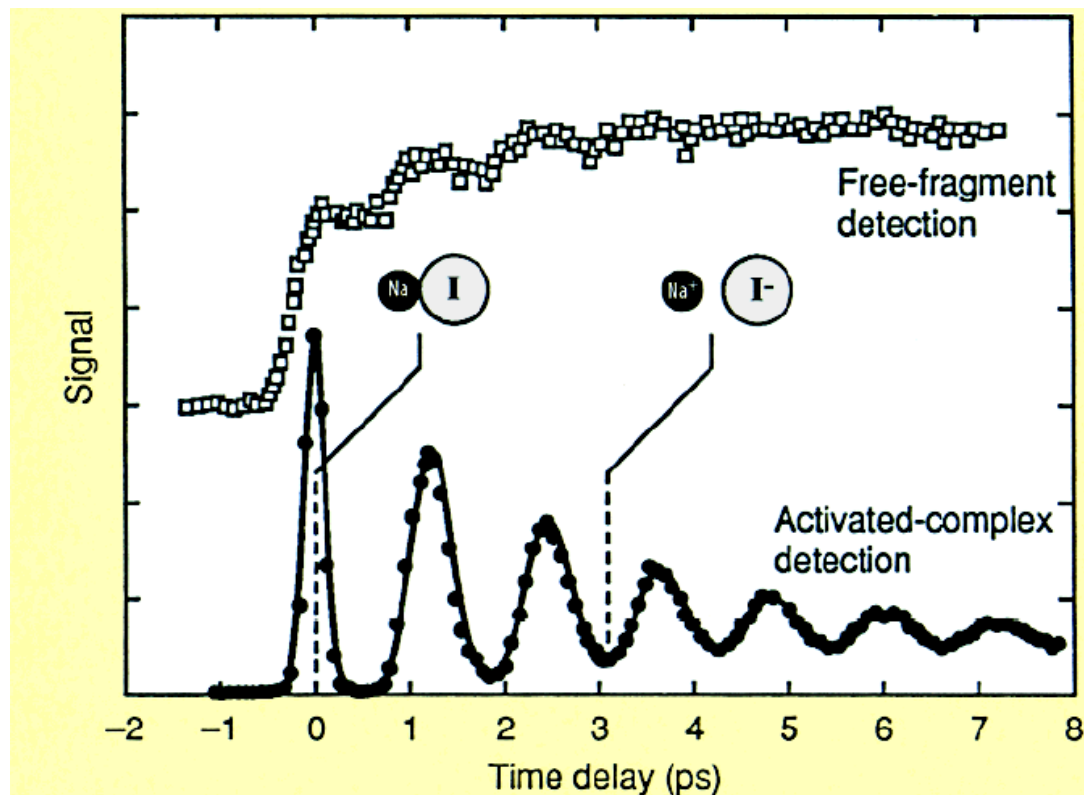
$$H_{11}(R) = H_{22}(R)$$
$$H_{12}(R) = 0$$



In 1D: Avoided Crossing



# Avoided Crossing in NaI



T. S. Rose, M. J. Rosker, A. H. Zewail, J. Chem. Phys. 91 (1989) 7415  
A. H. Zewail, J. Phys. Chem. A 104 (2000) 5660



# Avoided Crossing, Non-crossing Rule

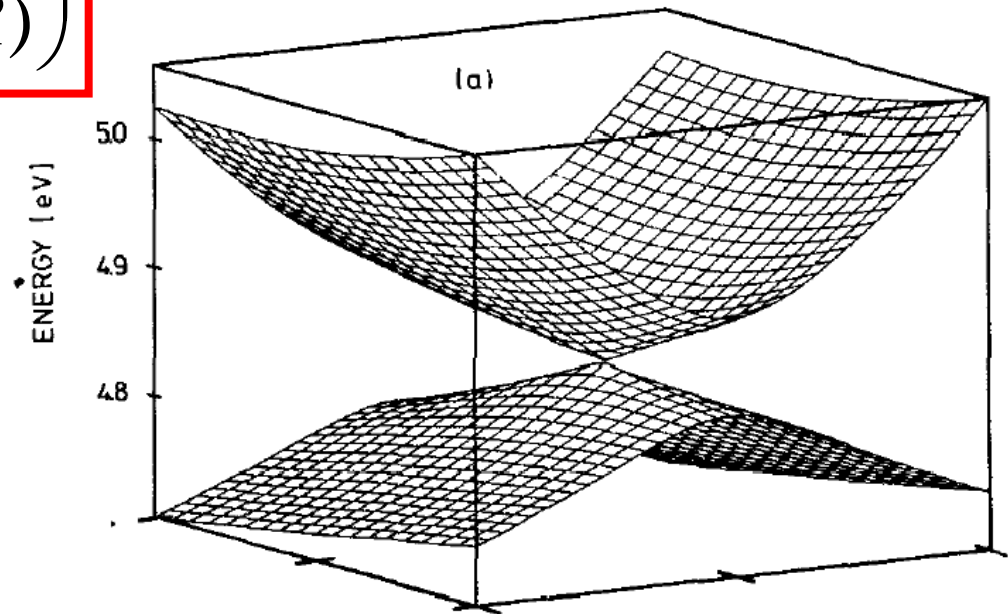
$S_1$  and  $S_2$  in pyrazine in the  $Q_{6a}$  and  $Q_{10a}$  subspace

$$H(R) = \begin{pmatrix} H_{11}(R) & H_{12}(R) \\ H_{21}(R) & H_{22}(R) \end{pmatrix}$$

Two surfaces cross when:

$$H_{11}(R) = H_{22}(R)$$
$$H_{12}(R) = 0$$

In 2D: 0D-Conical Intersection



C. Woywod, W. Domcke, A. L. Sobolewski, H.-J. Werner J. Chem. Phys. 100, 1400 (1994)



# Femtochemistry: Basic Concepts

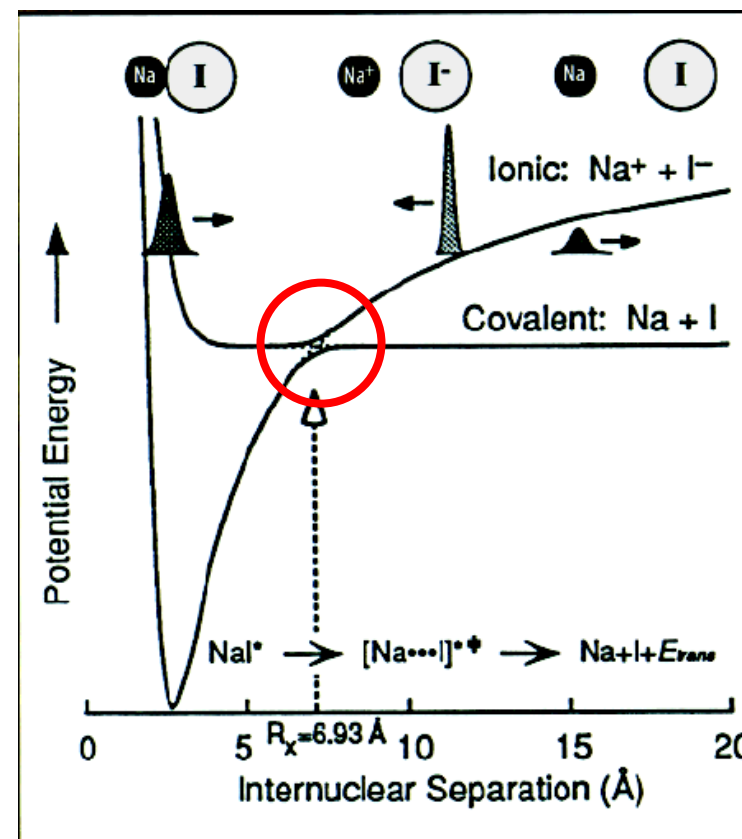
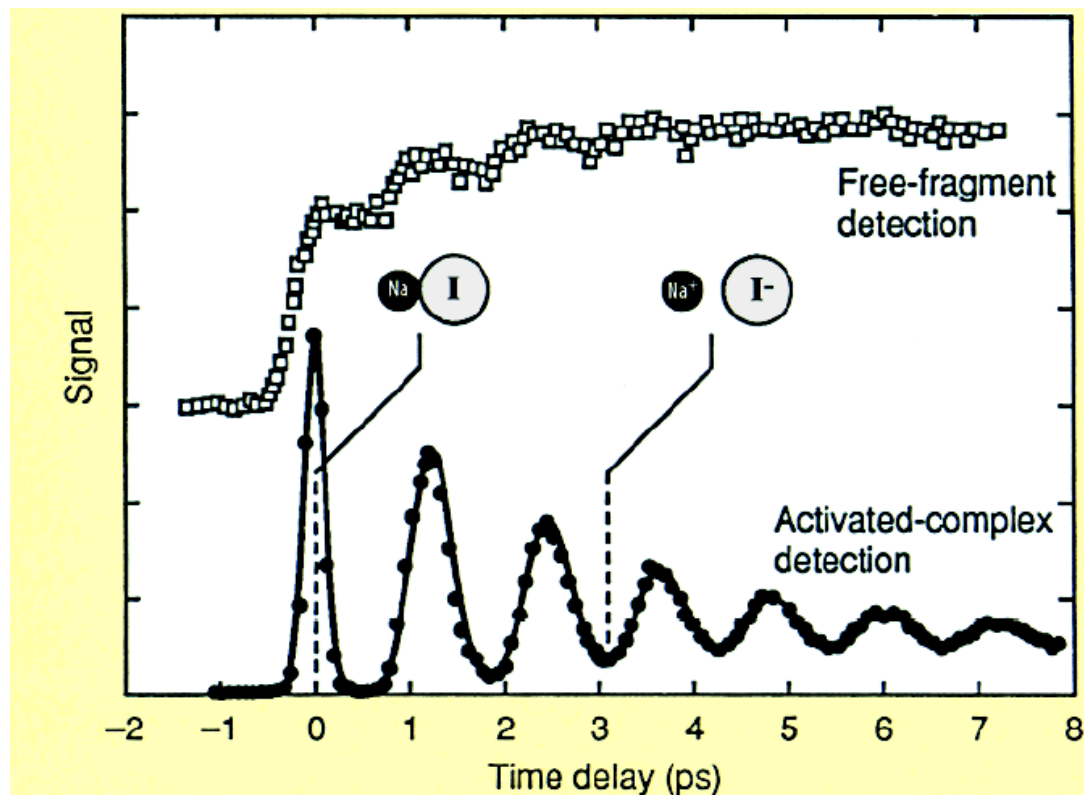
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- Examples of Photochemical Reactions
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- Jablonski Diagram, Fermi Golden Rule, Energy Gap Law
- Prototype Potential Energy Surfaces
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- **Born Oppenheimer Approximation and its Breakdown**
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- Solvation
- Electron Transfer Theory
- Excitation Transfer: Exciton- and Förster Transfer





# Avoided Crossing in NaI



T. S. Rose, M. J. Rosker, A. H. Zewail, J. Chem. Phys. 91 (1989) 7415  
A. H. Zewail, J. Phys. Chem. A 104 (2000) 5660

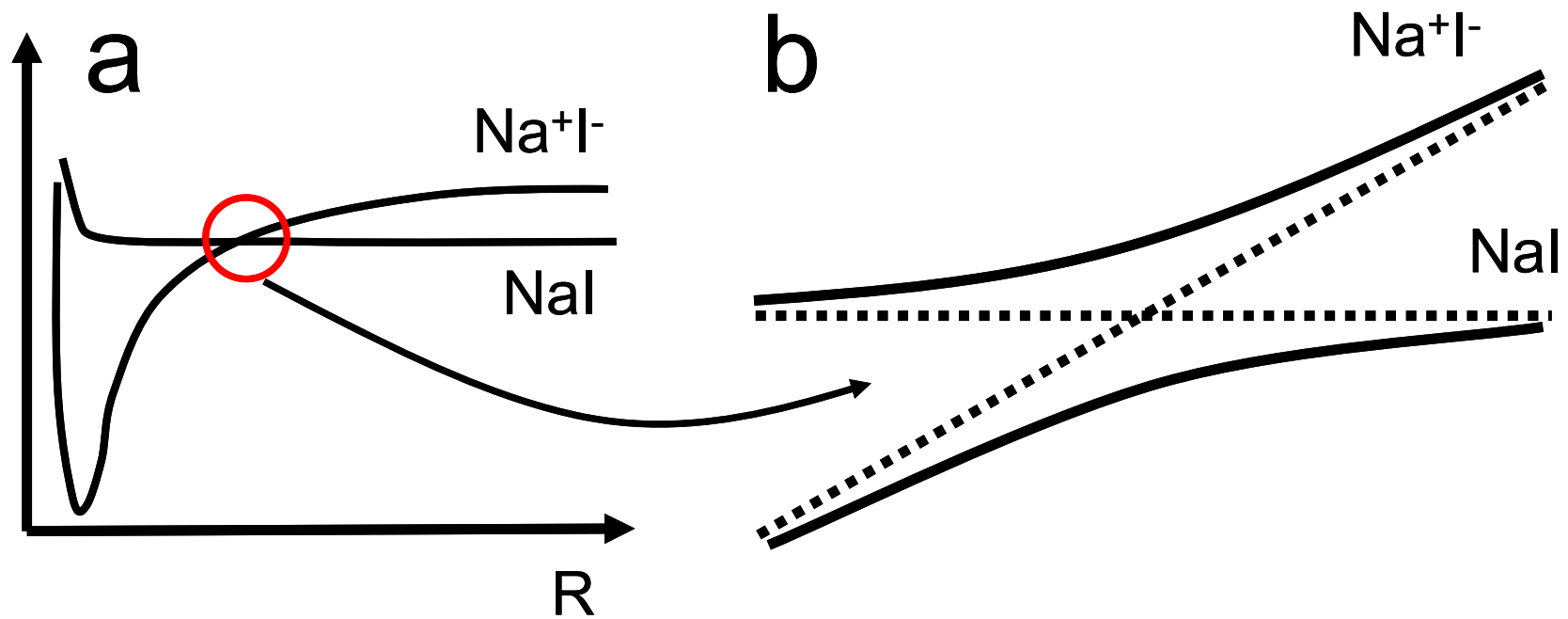
## Born Oppenheimer Expansion

$$E_j(R)\chi_j(R) + \sum_i \langle \Psi_j | \hat{T}_{nuc} | \Psi_i \rangle \chi_i = \epsilon \chi_j(R)$$

$$\begin{aligned} \langle \Psi_j | \hat{T}_{nuc} | \Psi_i \rangle \chi_i &= -\frac{\hbar^2}{2M} \left\langle \Psi_j \left| \frac{\partial^2}{\partial R^2} \right| \Psi_i \right\rangle \chi_i \\ &\quad -\frac{\hbar^2}{M} \left\langle \Psi_j \left| \frac{\partial}{\partial R} \right| \Psi_i \right\rangle \left( \frac{\partial}{\partial R} \chi_i \right) \\ &\quad -\frac{\hbar^2}{2M} \langle \Psi_j | \Psi_i \rangle \left( \frac{\partial^2}{\partial R^2} \chi_i \right) \\ &\equiv -\frac{\hbar^2}{2M} \left( G_{ij} \chi_i + 2F_{ij} \frac{\partial \chi_i}{\partial R} \right) - \delta_{ij} \frac{\hbar^2}{2M} \frac{\partial^2}{\partial R^2} \chi_i \end{aligned}$$



# Ionic Bond



## Adiabatic Representation

$$i\hbar \frac{\partial}{\partial t} \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix} = \left[ \begin{pmatrix} T_{nuc} & F_{12} \\ F_{12} & T_{nuc} \end{pmatrix} + \begin{pmatrix} E_1^{(ad)} & 0 \\ 0 & E_2^{(ad)} \end{pmatrix} \right] \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix}$$

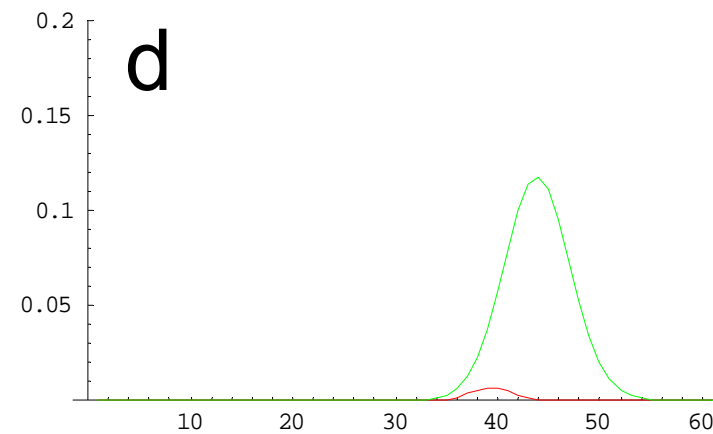
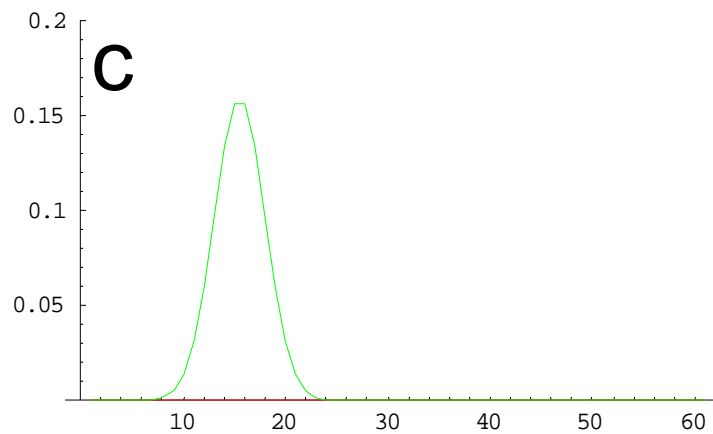
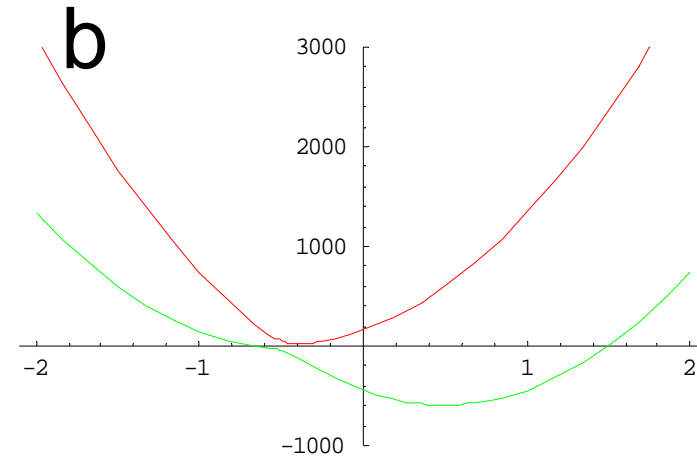
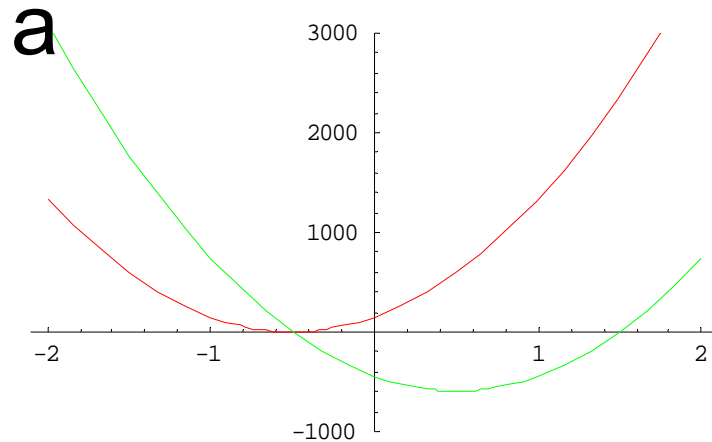
$$\text{with: } F_{12} = \langle \Psi_1 | \frac{\partial}{\partial R} | \Psi_2 \rangle$$

## Diabatic Representation

$$i\hbar \frac{\partial}{\partial t} \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix} = \left[ \begin{pmatrix} T_{nuc} & 0 \\ 0 & T_{nuc} \end{pmatrix} + \begin{pmatrix} E_1^{(dia)} & E_{12}^{(dia)} \\ E_{12}^{(dia)} & E_2^{(dia)} \end{pmatrix} \right] \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix}$$



# Wavepacket on Coupled Surfaces



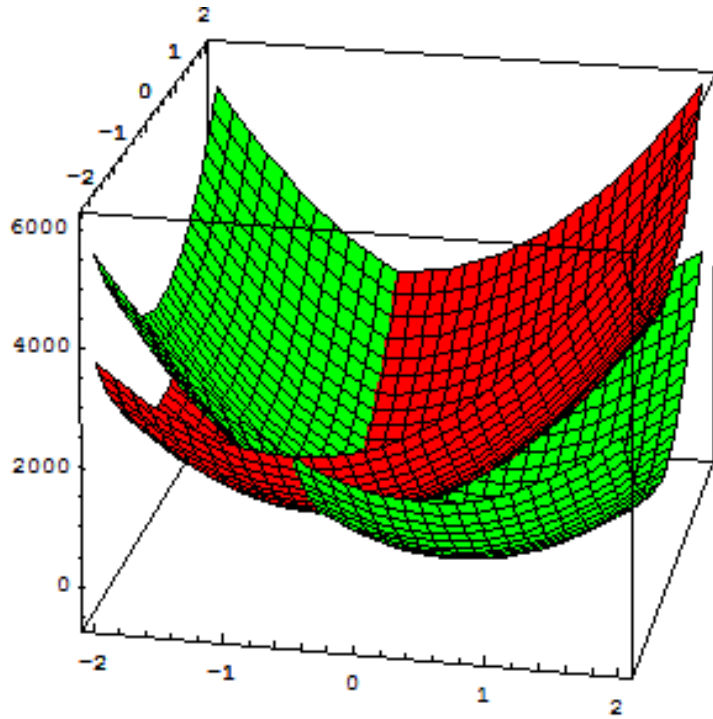
## Adiabatic Representation

- + Output of quantum chemistry programs
- + Born Oppenheimer approximation
- Discontinuous at CI
- Breaks down in avoided crossing
- Useless for numerical wavepacket propagation

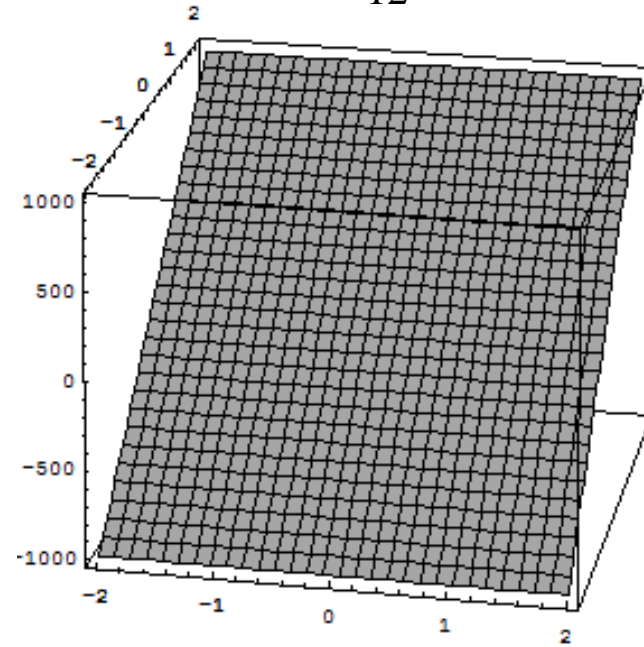
## Diabatic Representation

- + renders  $\partial/\partial R\Psi^{(el)} = 0$  or small
- + closer to chemical intuition
- + continuous even in CI
- + Better description in avoided crossing region
- + Useful for numerical purposes
- Requires additional coupling surface  $E_{12}$
- Not calculated by quantum chemistry programs
- Not unique in more than 1D

$V_1, V_2$



$V_{12}$

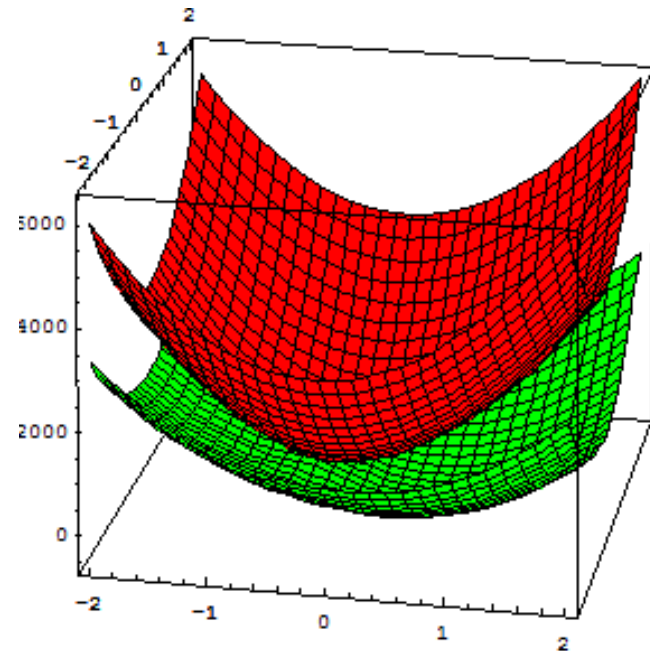


$$V_1 = k_1(x_1 - 0.5)^2 + k_2x_2^2$$

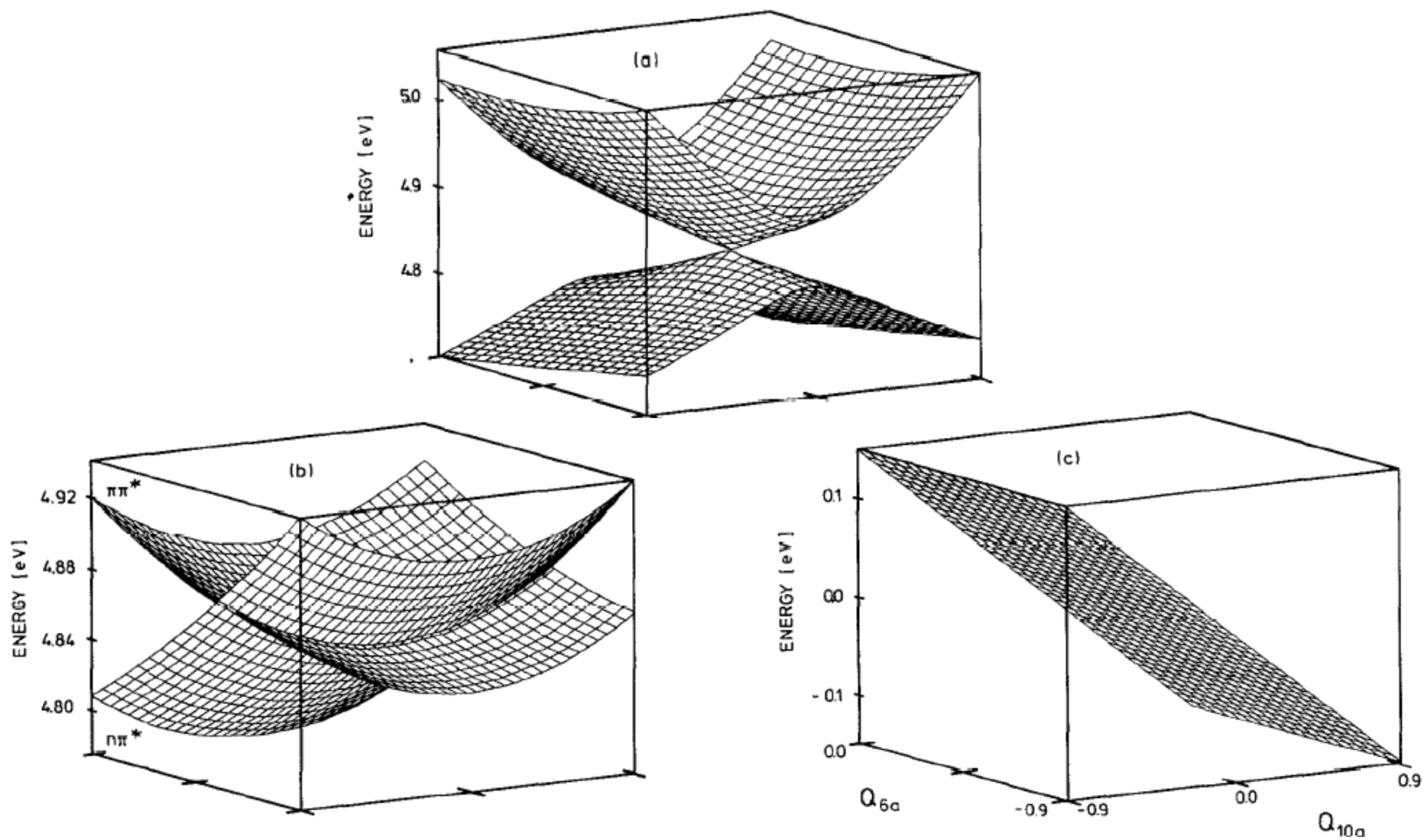
$$V_2 = k_1(x_1 + 0.5)^2 + k_2x_2^2$$

$$V_{12} = k_{12}x_2$$

$$H = \begin{pmatrix} V_1 & V_{12} \\ V_{12} & V_2 \end{pmatrix}$$



# $S_1$ and $S_2$ in pyrazine in the $Q_{6a}$ and $Q_{10a}$ subspace

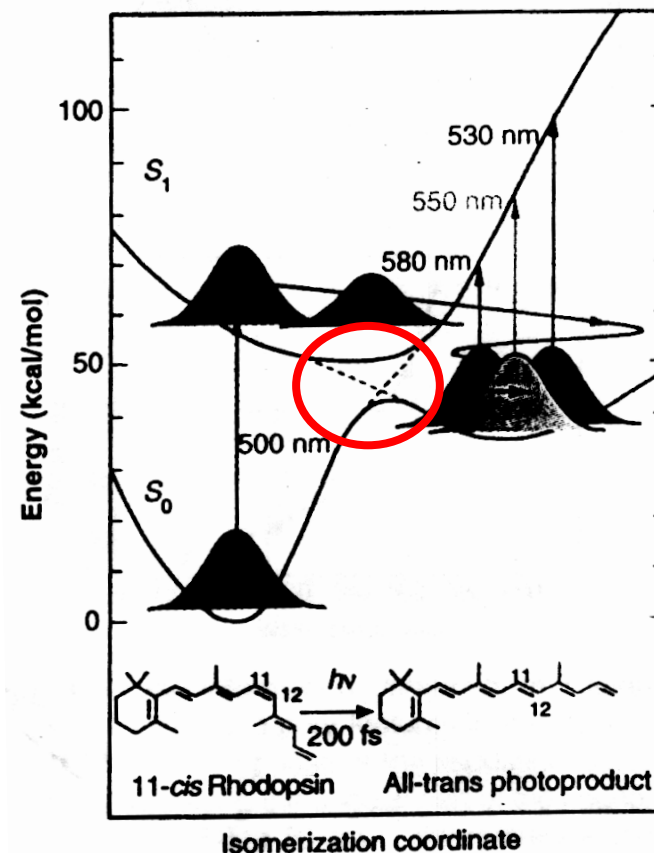
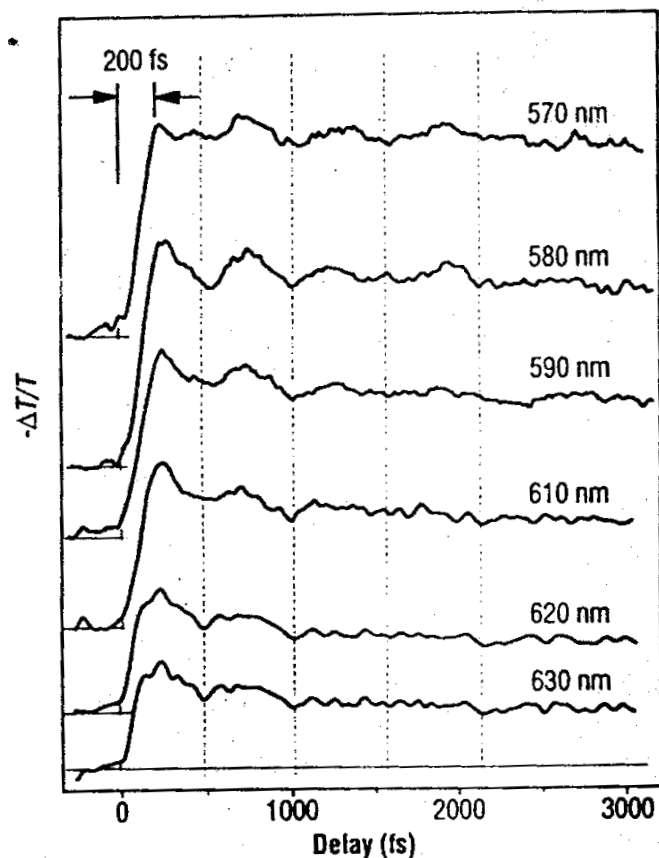


Domcke et al. JCP 100 (1994) 1400



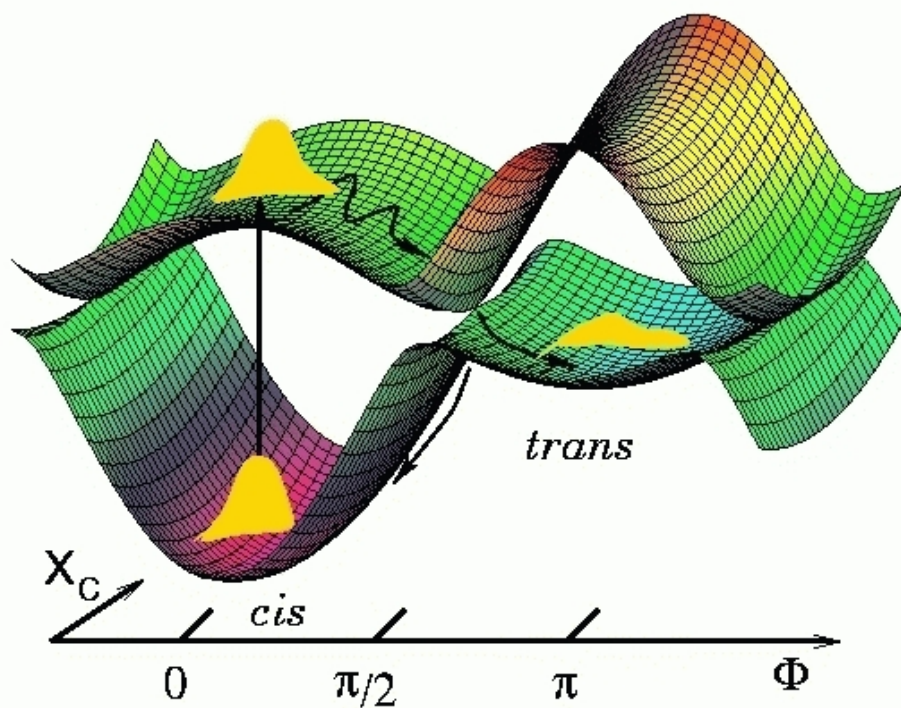


# Photochemical Reactions in Nature: Isomerization of Rhodopsin

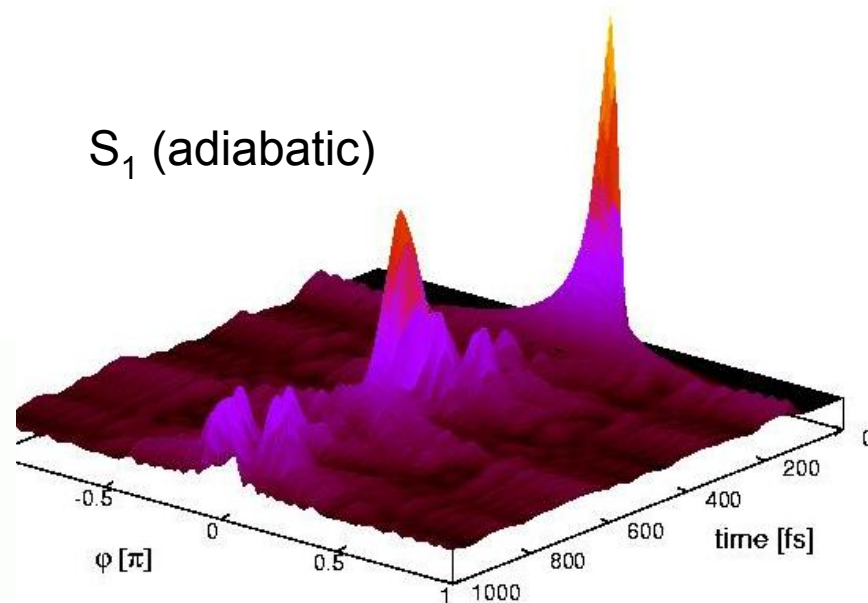


Q. Wang, R. W. Schoenlein, L. A. Peteanu, R. A. Mathies, C. V. Shank,  
Science 266 (1994) 422

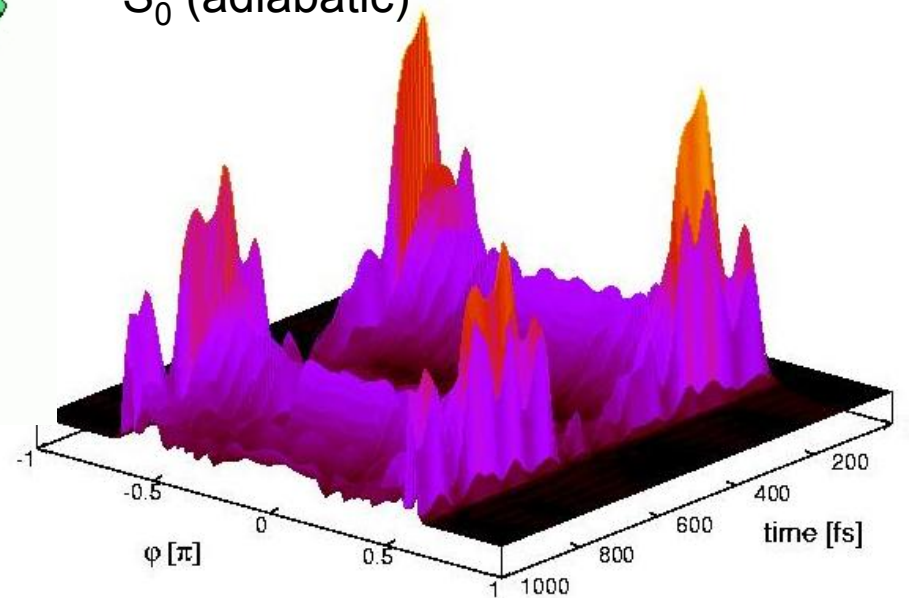
# Model Rhodopsin



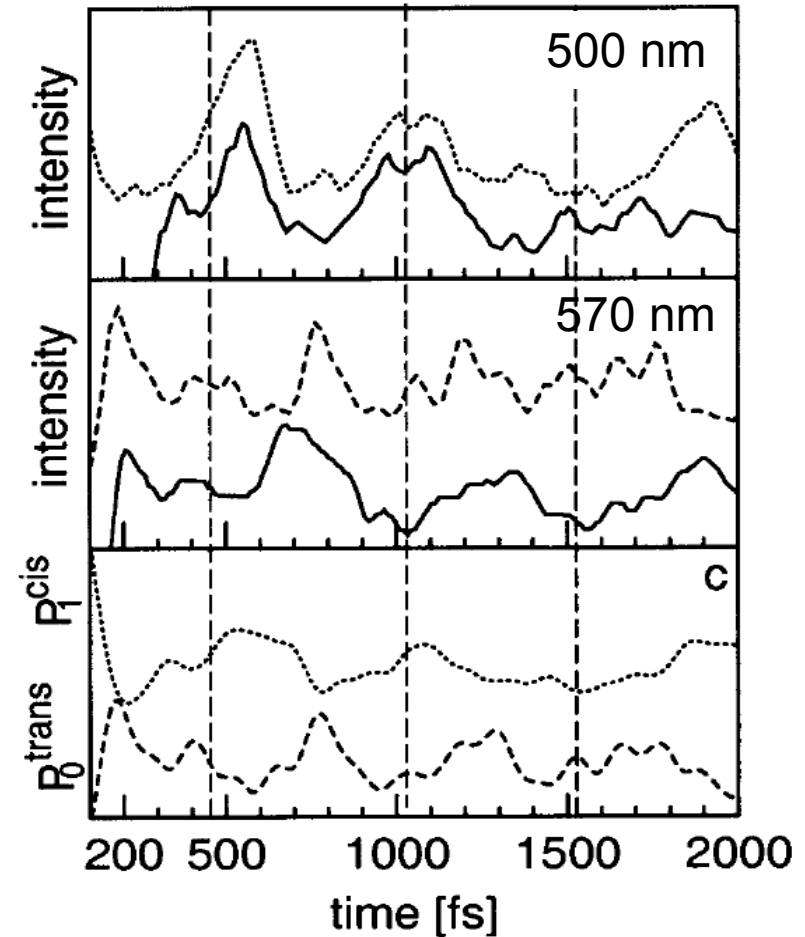
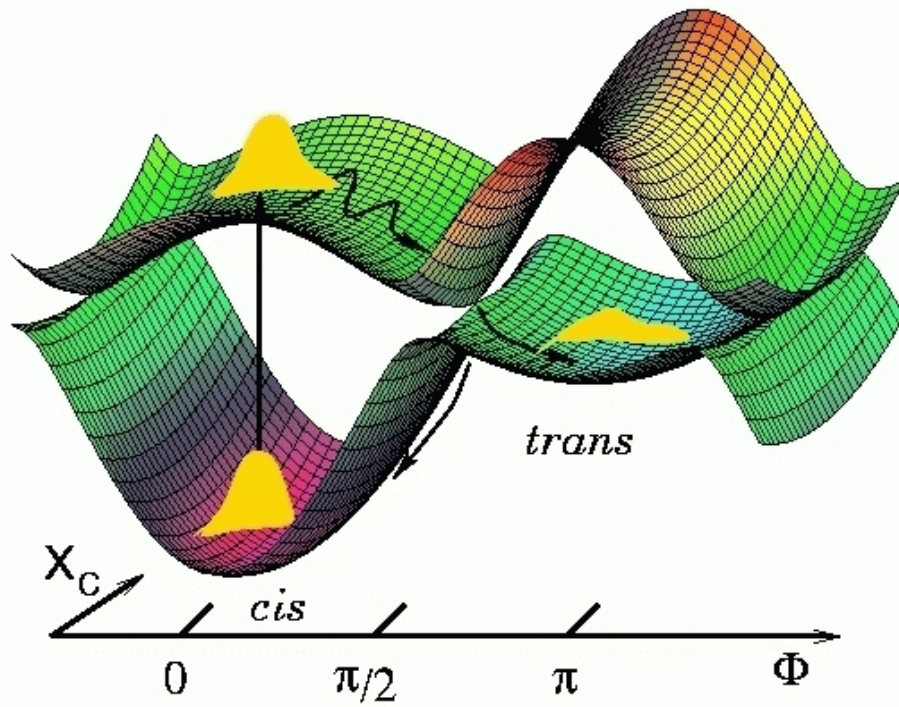
$S_1$  (adiabatic)



$S_0$  (adiabatic)

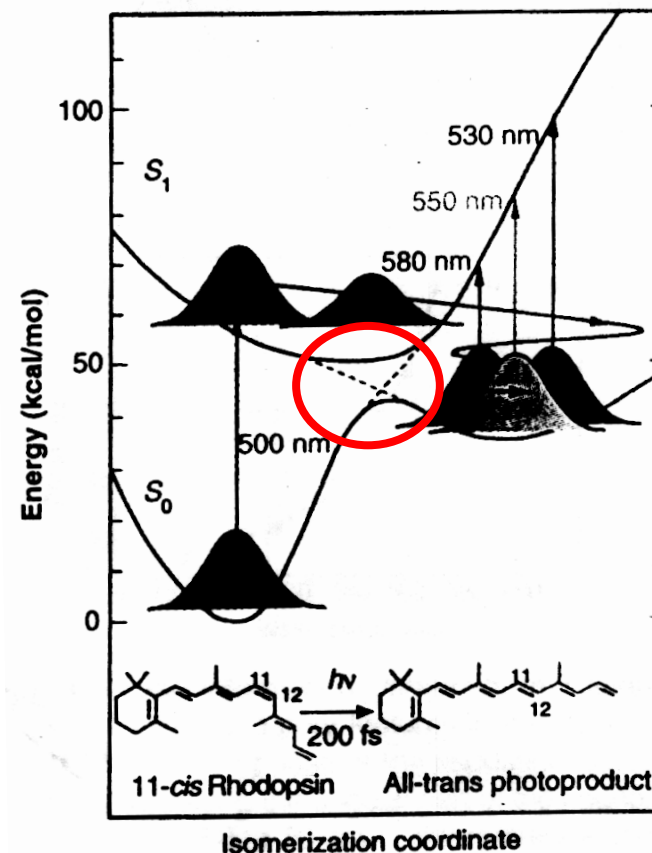
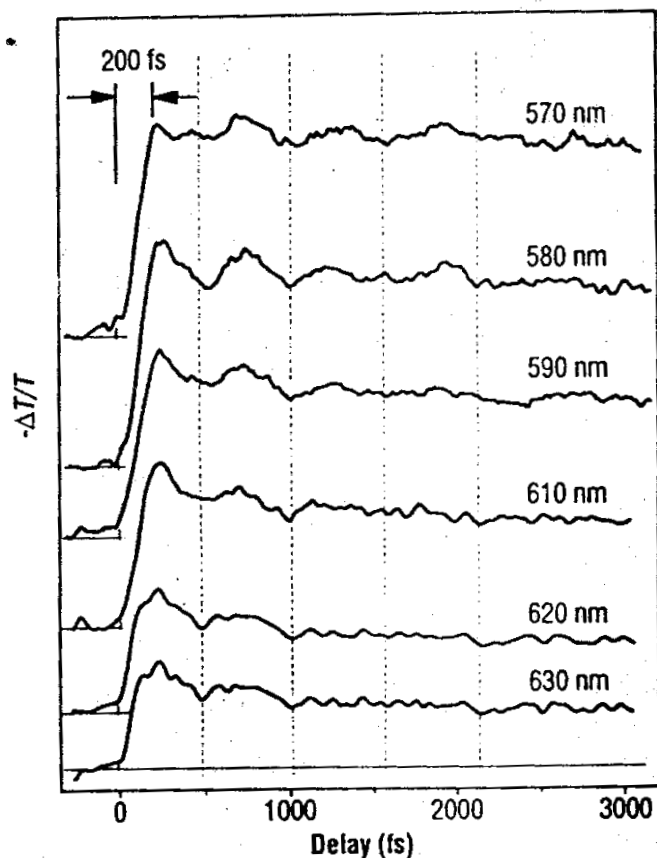


# Model Rhodopsin

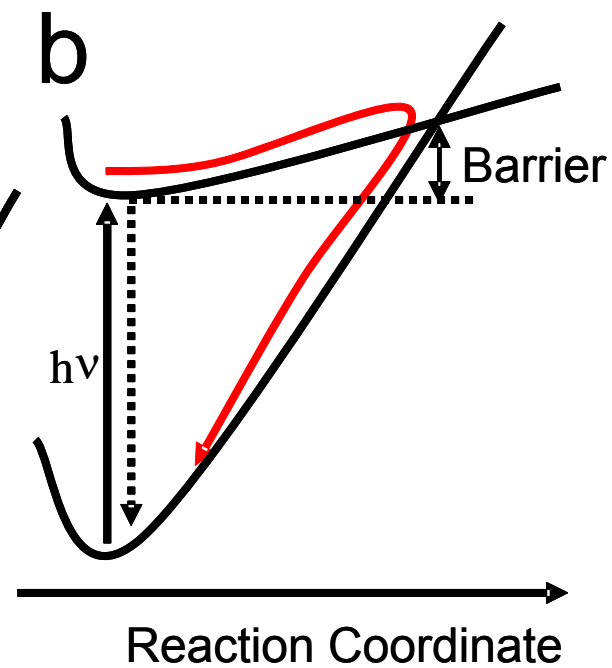
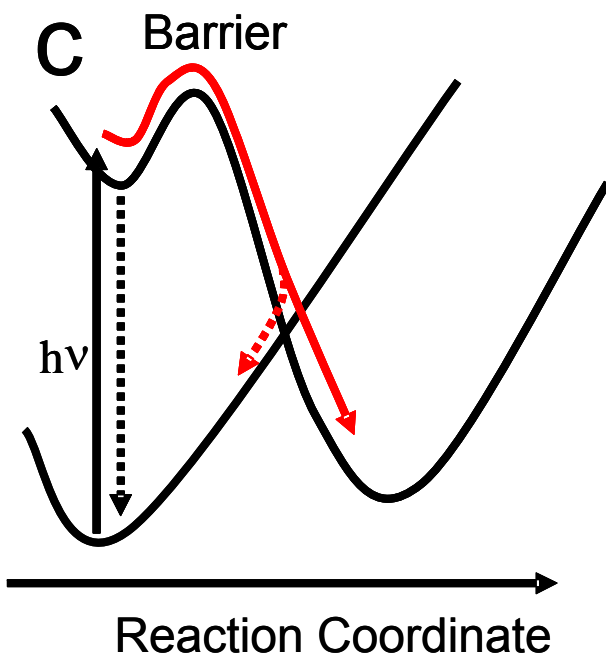
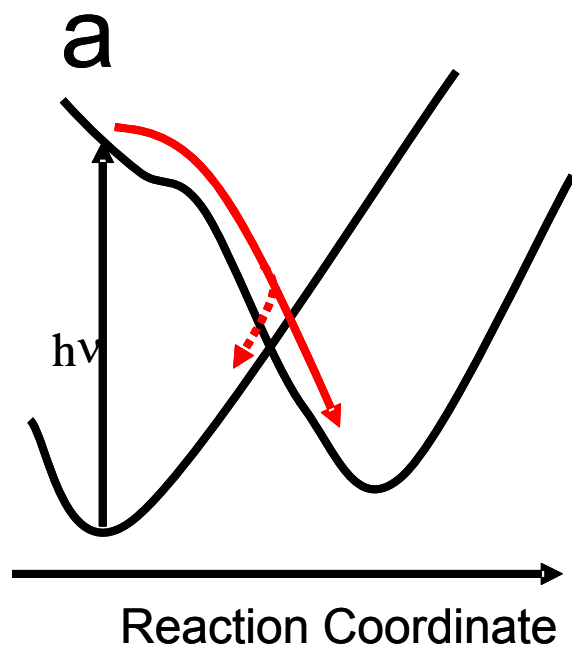




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Q. Wang, R. W. Schoenlein, L. A. Peteanu, R. A. Mathies, C. V. Shank,  
Science 266 (1994) 422





# Femtochemistry: Basic Concepts

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## Diabatic Representation

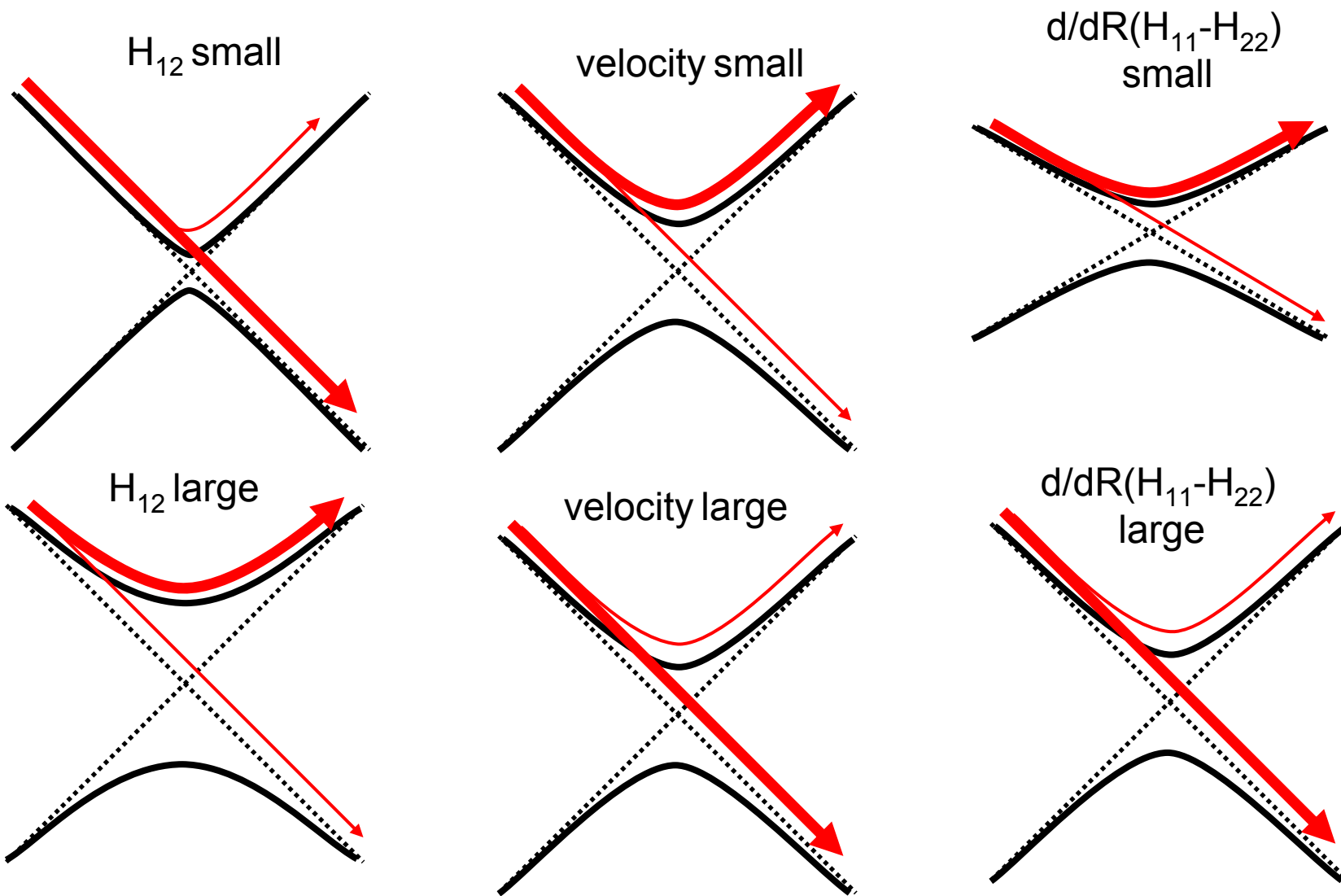
$$i\hbar \frac{\partial}{\partial t} \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix} = \left[ \begin{pmatrix} T_{nuc} & 0 \\ 0 & T_{nuc} \end{pmatrix} + \begin{pmatrix} H_1^{(dia)} & H_{12}^{(dia)} \\ H_{12}^{(dia)} & H_2^{(dia)} \end{pmatrix} \right] \begin{pmatrix} \chi_1 \\ \chi_2 \end{pmatrix}$$

Semiclassical Approximation:

$$R(t) = v \times t$$

$$i\hbar \frac{\partial}{\partial t} \begin{pmatrix} c_1 \\ c_2 \end{pmatrix} = \left[ \begin{pmatrix} H_1^{(dia)}(R(t)) & H_{12}^{(dia)}(R(t)) \\ H_{12}^{(dia)}(R(t)) & H_2^{(dia)}(R(t)) \end{pmatrix} \right] \begin{pmatrix} c_1 \\ c_2 \end{pmatrix}$$

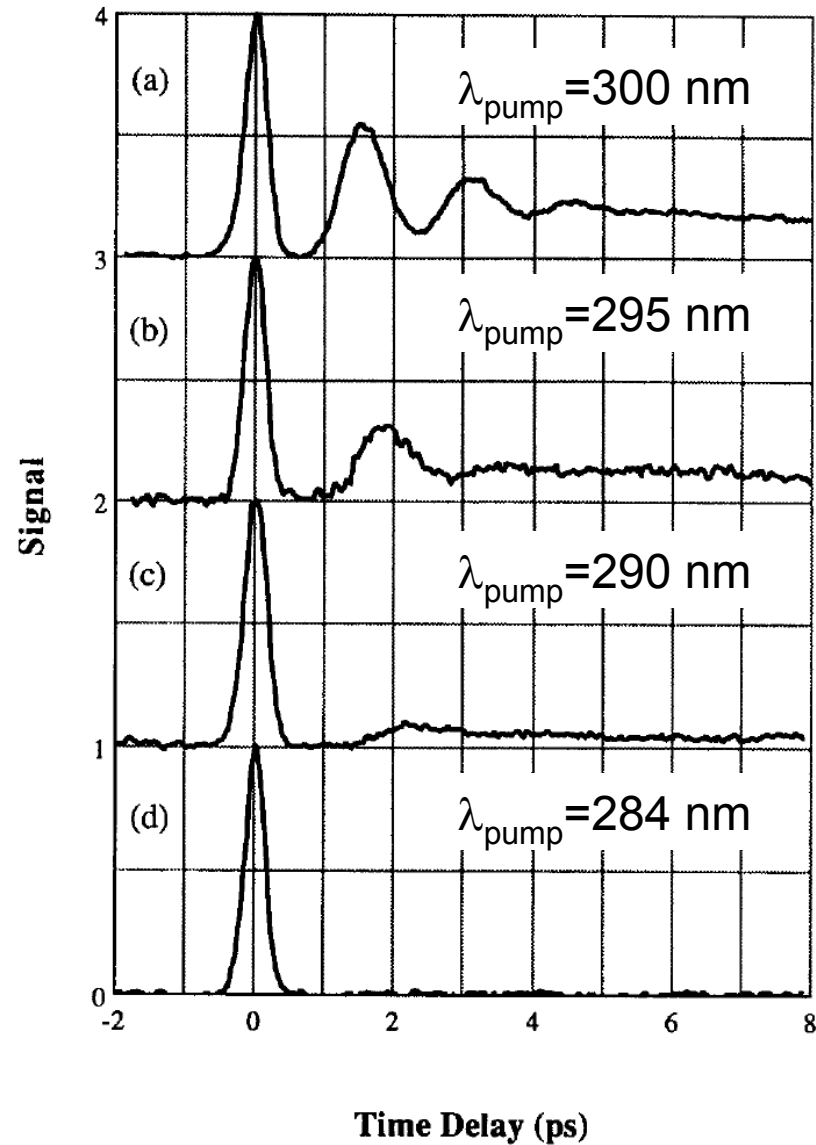
$$P^{(dia)} = 1 - \exp\left[-\frac{4\pi^2}{h\nu} \frac{H_{12}^2}{\left|\partial/\partial R(H_{11} - H_{22})\right|}\right]$$







# Landau Zener: Velocity Dependence





# Mean-Field Approach

---

$$MR\ddot{R}(t) = F^q$$

Equation of motion of classical subsystem

$$i\hbar\frac{\partial}{\partial t}\Psi(t) = H(R)\Psi(t)$$

Equation of motion of quantum subsystem

$$F^q = -\frac{\partial}{\partial R}\langle E \rangle = -\frac{\partial}{\partial R}\langle \Psi | H | \Psi \rangle = -\langle \Psi | \frac{\partial}{\partial R} H | \Psi \rangle$$

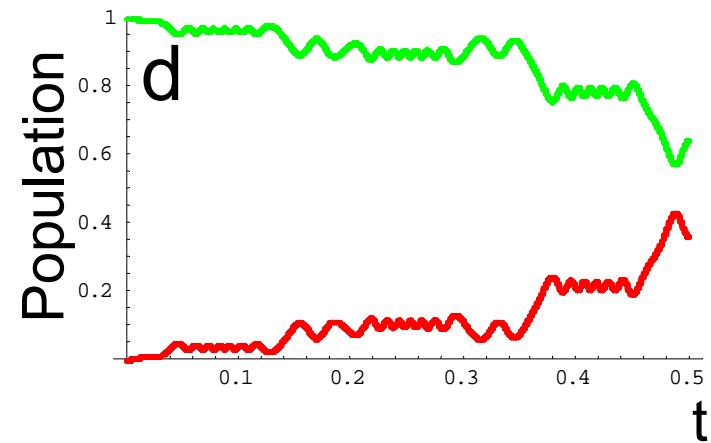
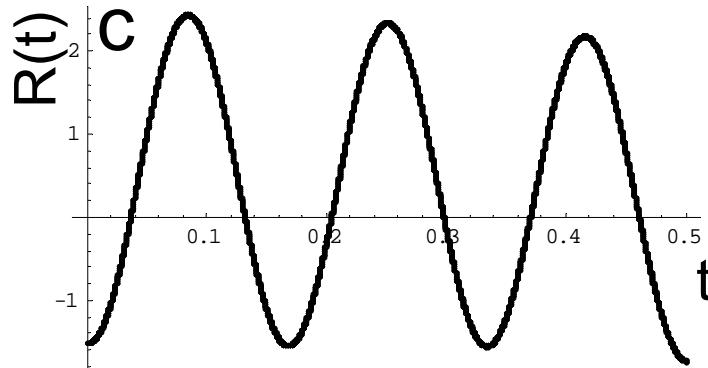
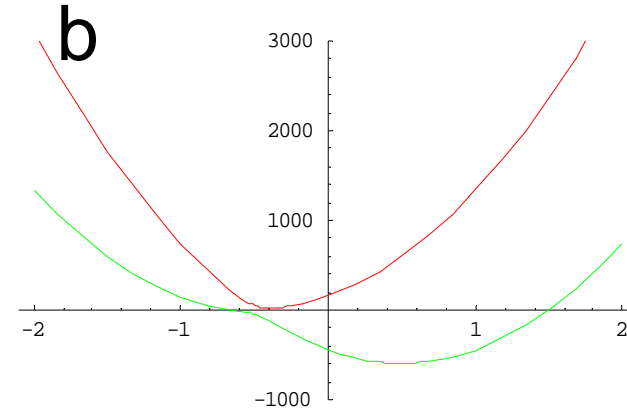
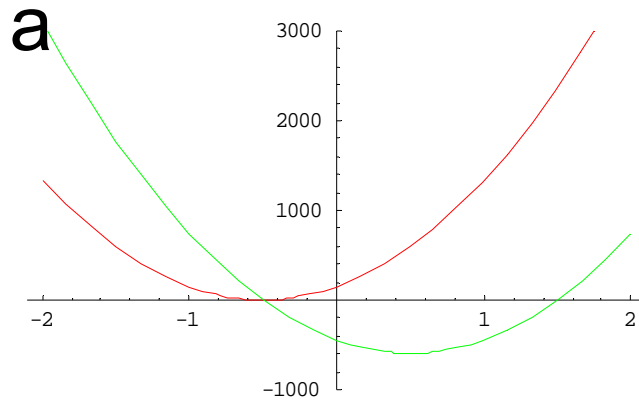
Hellmann-Feynmann force

$$E_{tot} = \langle \Psi | H | \Psi \rangle + \frac{1}{2}M\dot{R}^2 = const'$$

Energy conservation

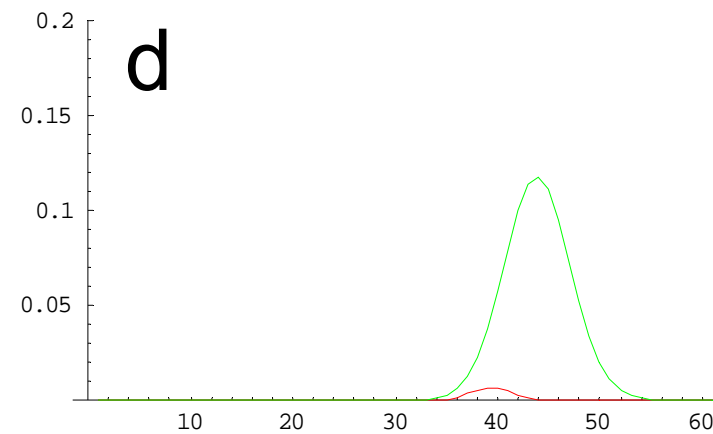
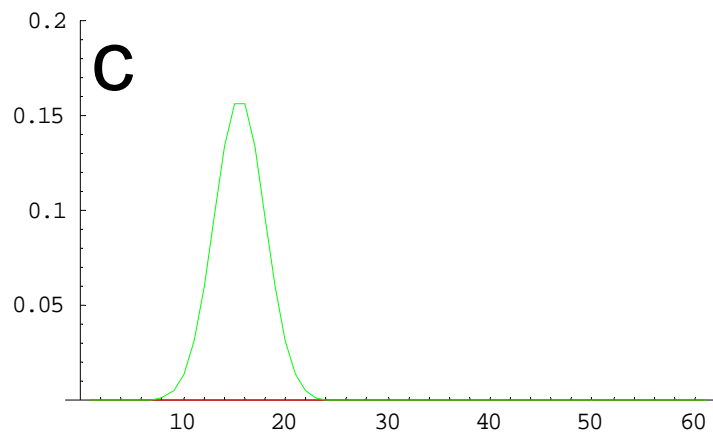
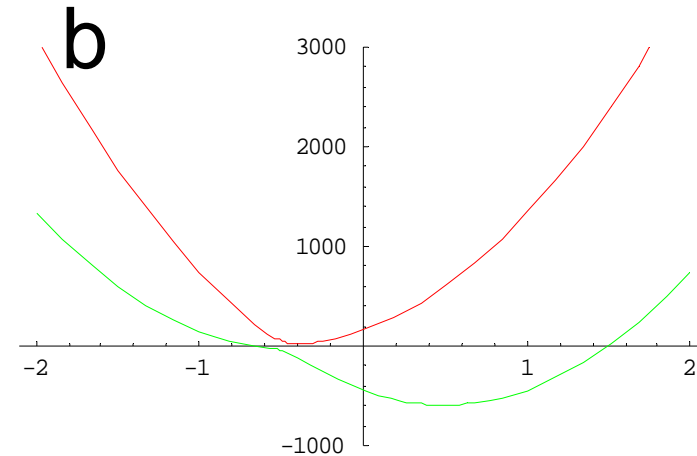
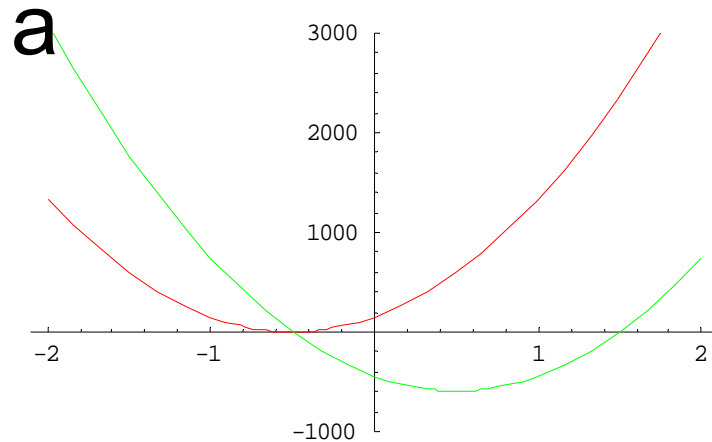


# Mean-Field Approach



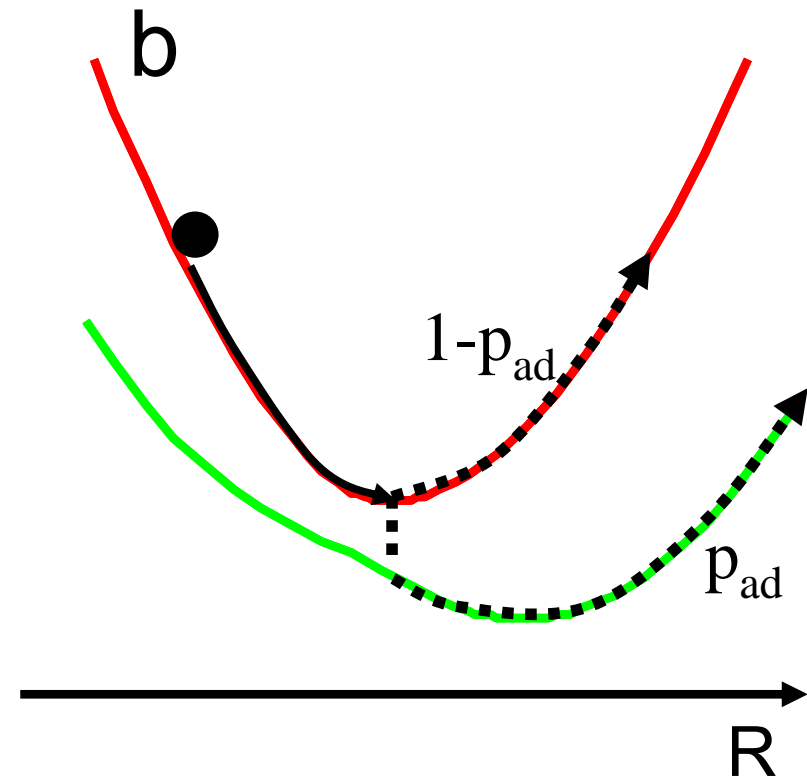
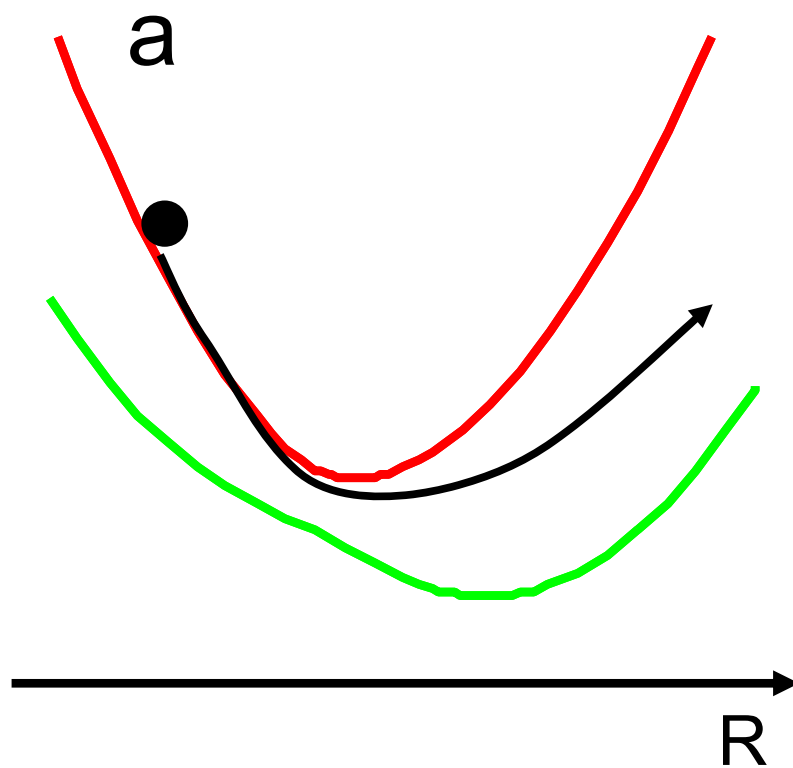


# Wavepacket on Coupled Surfaces





# Mean-Field *versus* Surface Hopping





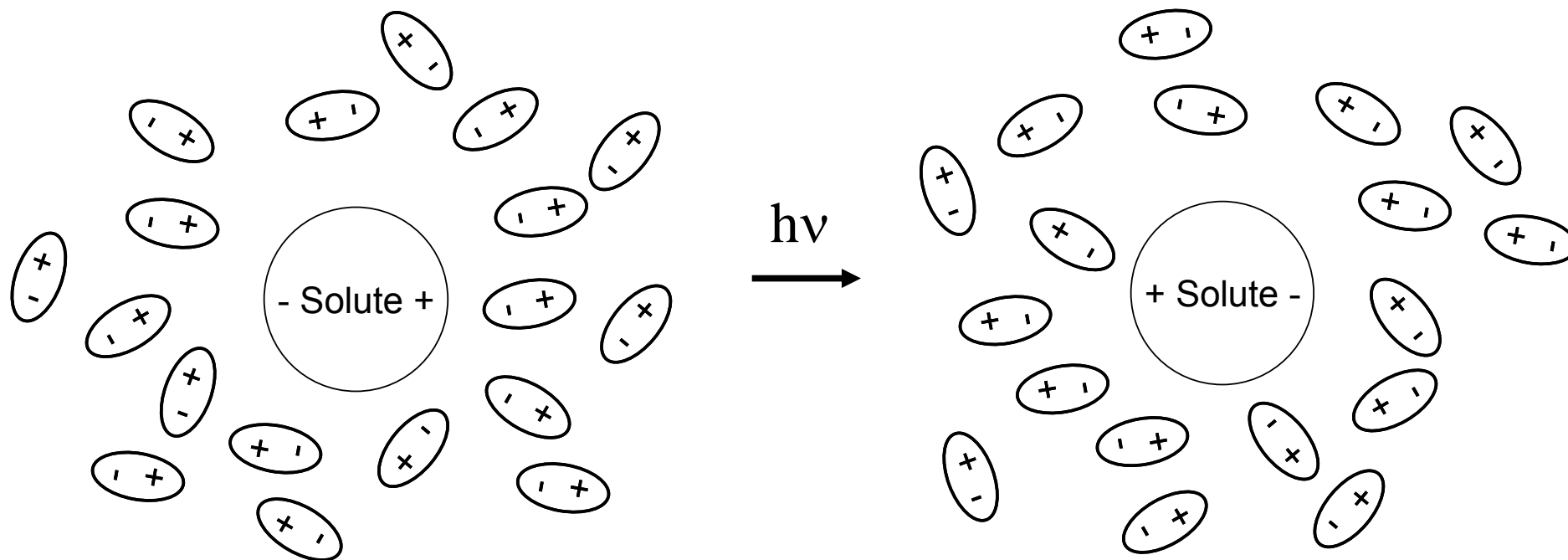
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# Solvation

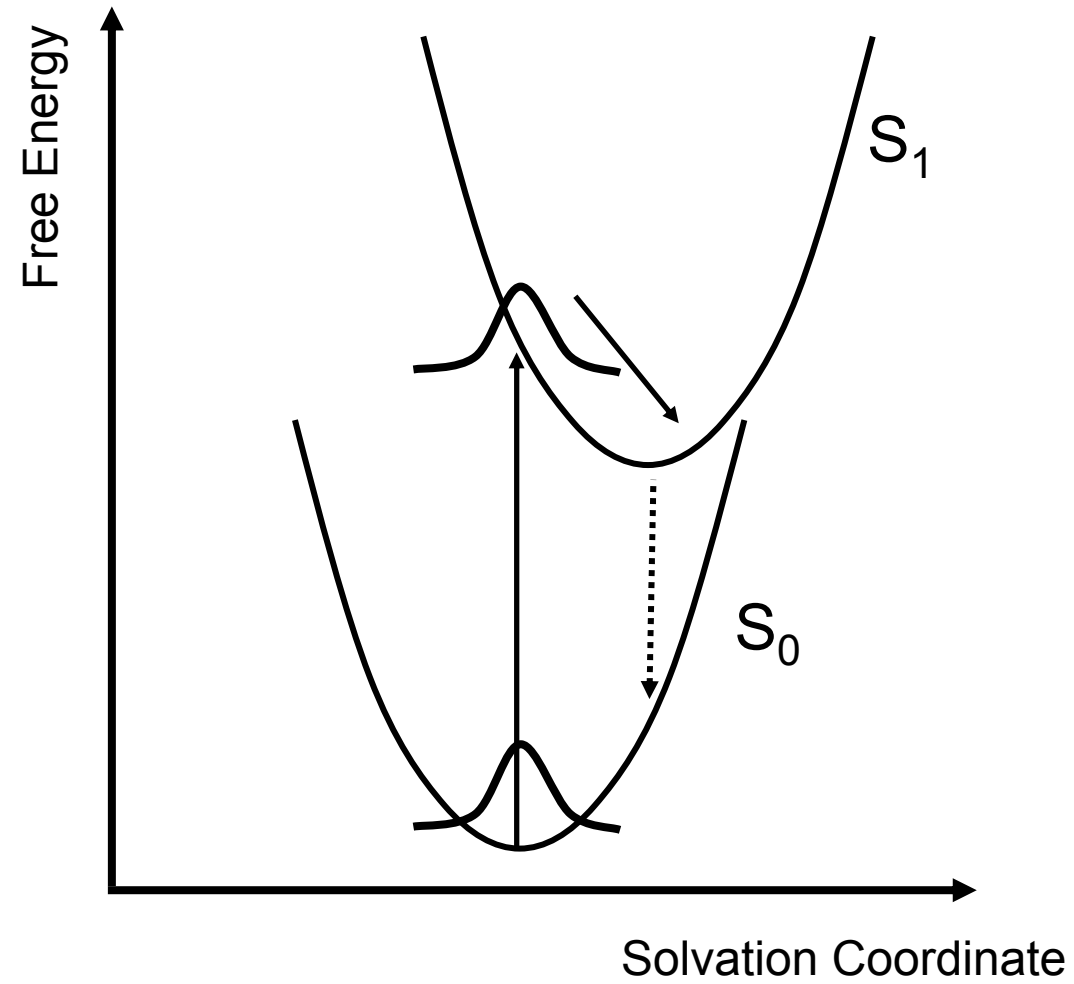


$$\Delta E = \frac{(\epsilon - 1)}{(2\epsilon + 1)r^3} \mu^2$$

Onsager's Reaction Field Model



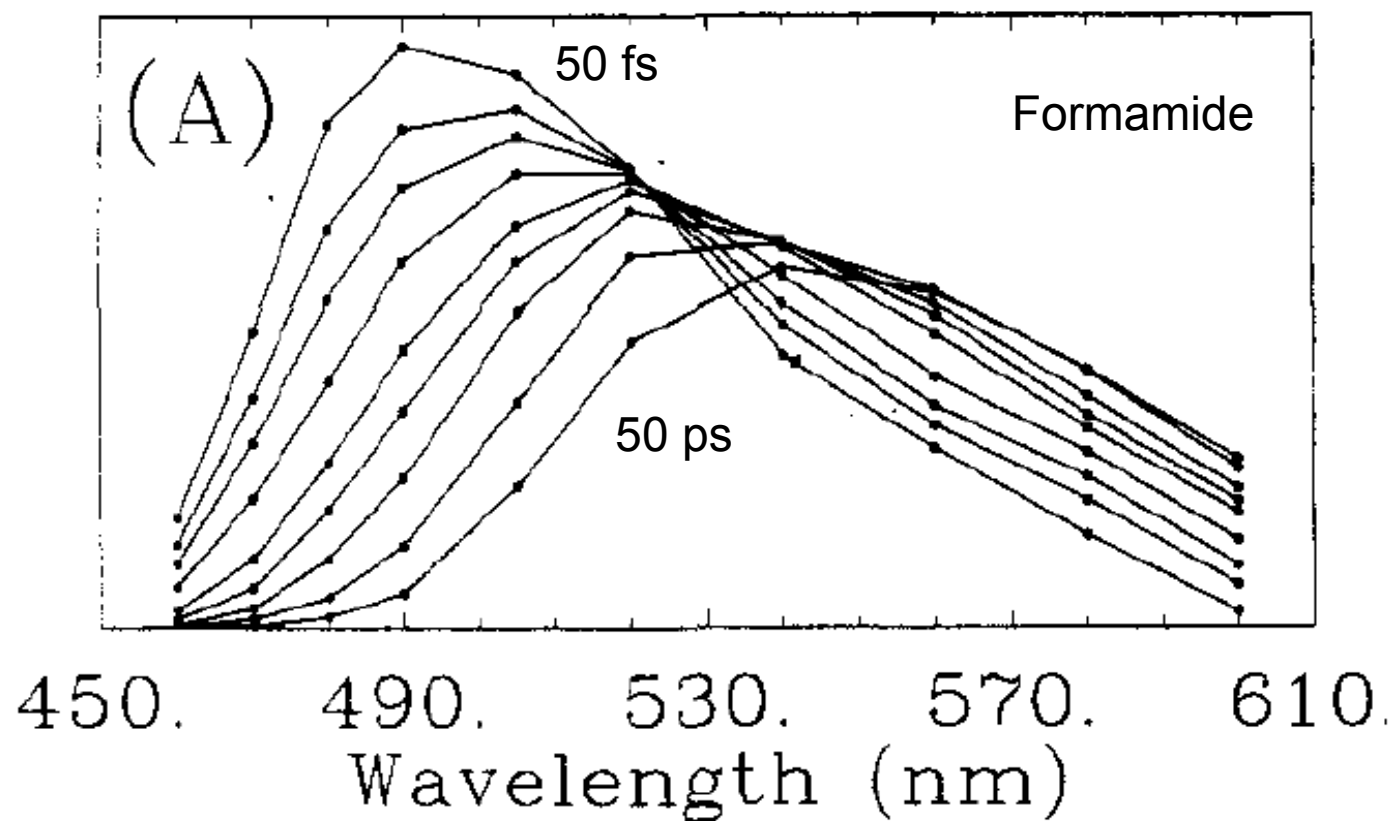
# Solvation







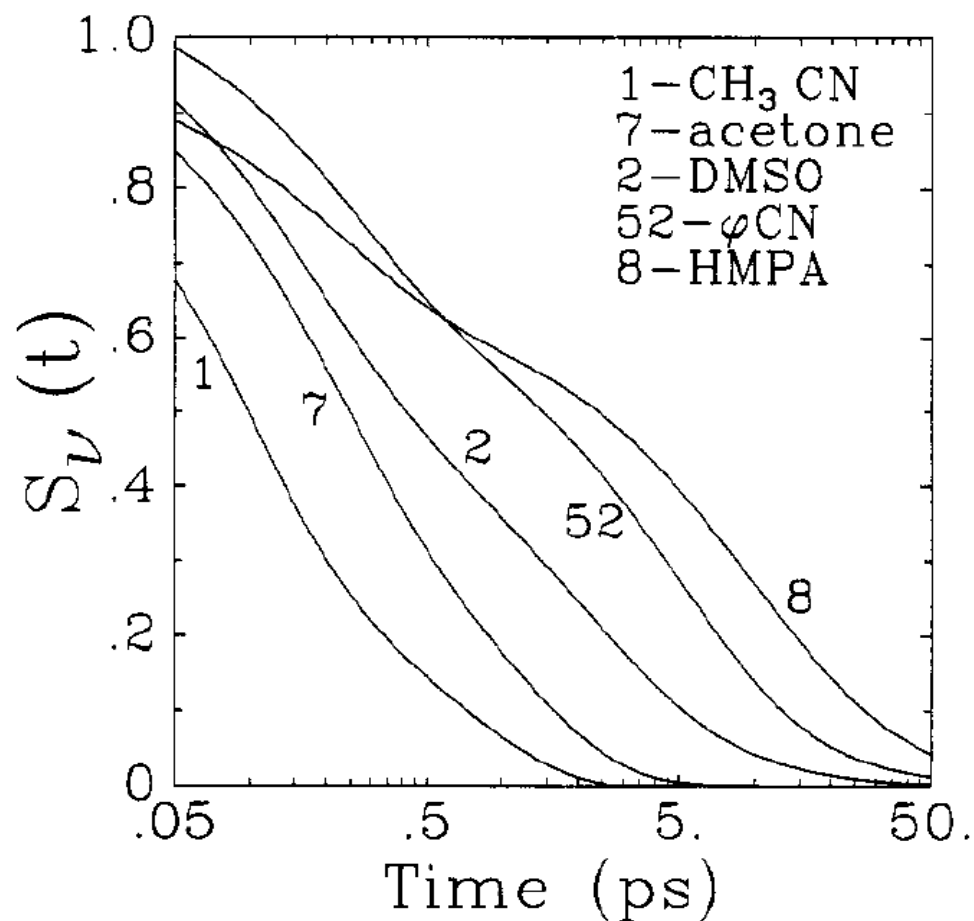
# Solvation of Coumarin in Polar Solvents



M. L. Horng, J. A. Gardecki, A. Papazyan, M. Maroncelli, *Subpicosecond Measurements of Polar Solvation Dynamics: Coumarin 153 Revisited* J. Phys. Chem.; **1995**; 99(48); 17311-17337.



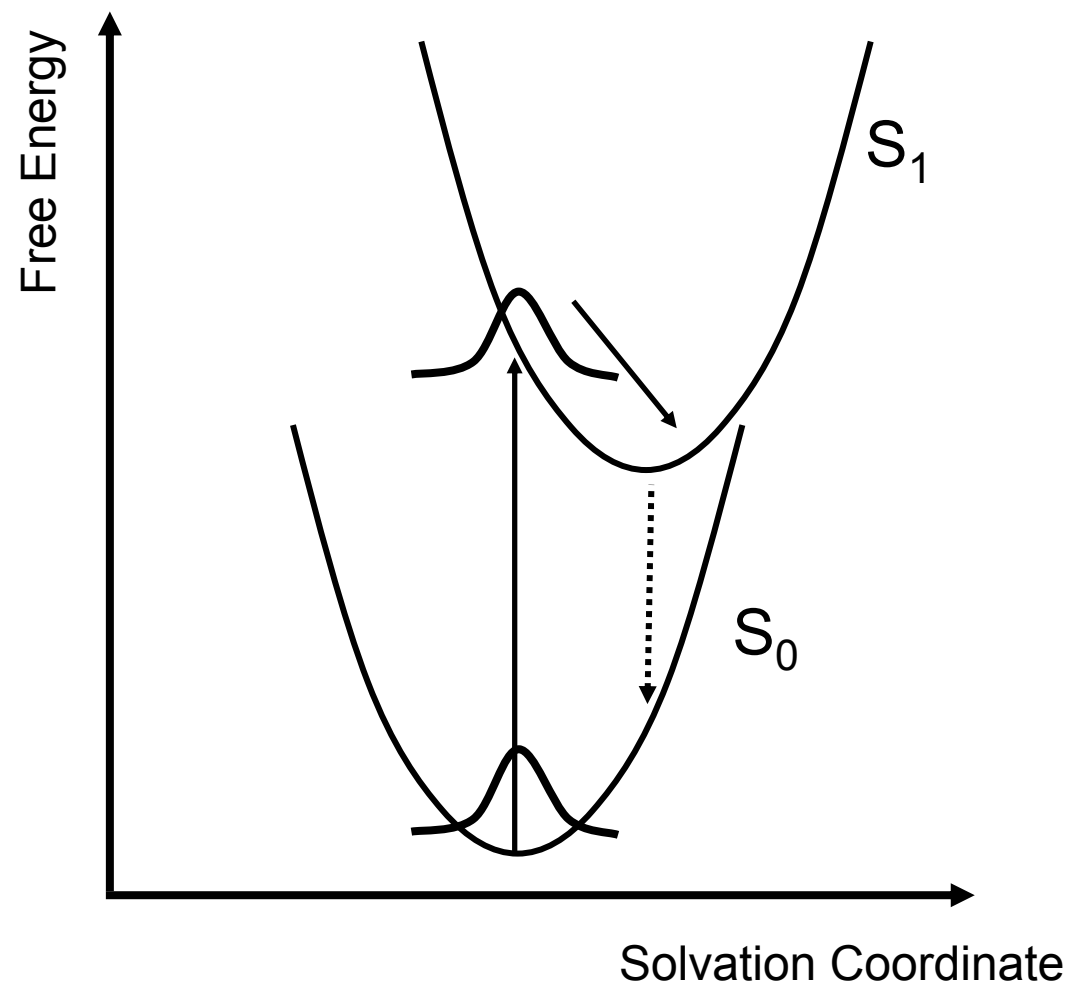
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# Solvation





# Central Limit Theorem

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When a random property is the sum of many random properties, e.g.:

$$P = \sum_{i=1}^N \mu_z$$

then, the sum ( $P$ ) is Gaussian distributed (in the limit  $N \rightarrow \infty$ ), regardless what the distribution of the individual terms ( $\mu_z$ ) is. The mean of the sum is:

$$\langle P \rangle = N \langle \mu_z \rangle$$

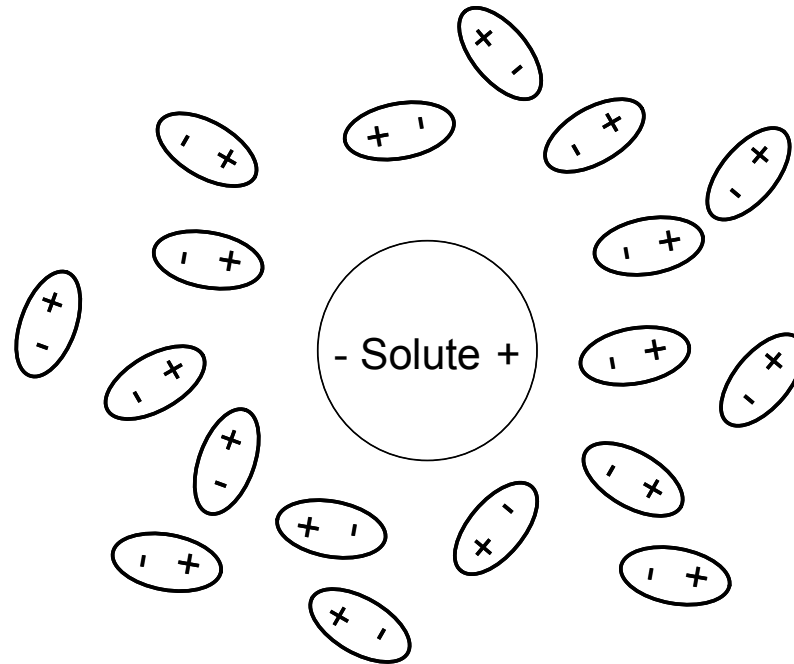
and the variance:

$$\langle (P - \langle P \rangle)^2 \rangle = N \langle (\mu_z - \langle \mu_z \rangle)^2 \rangle$$



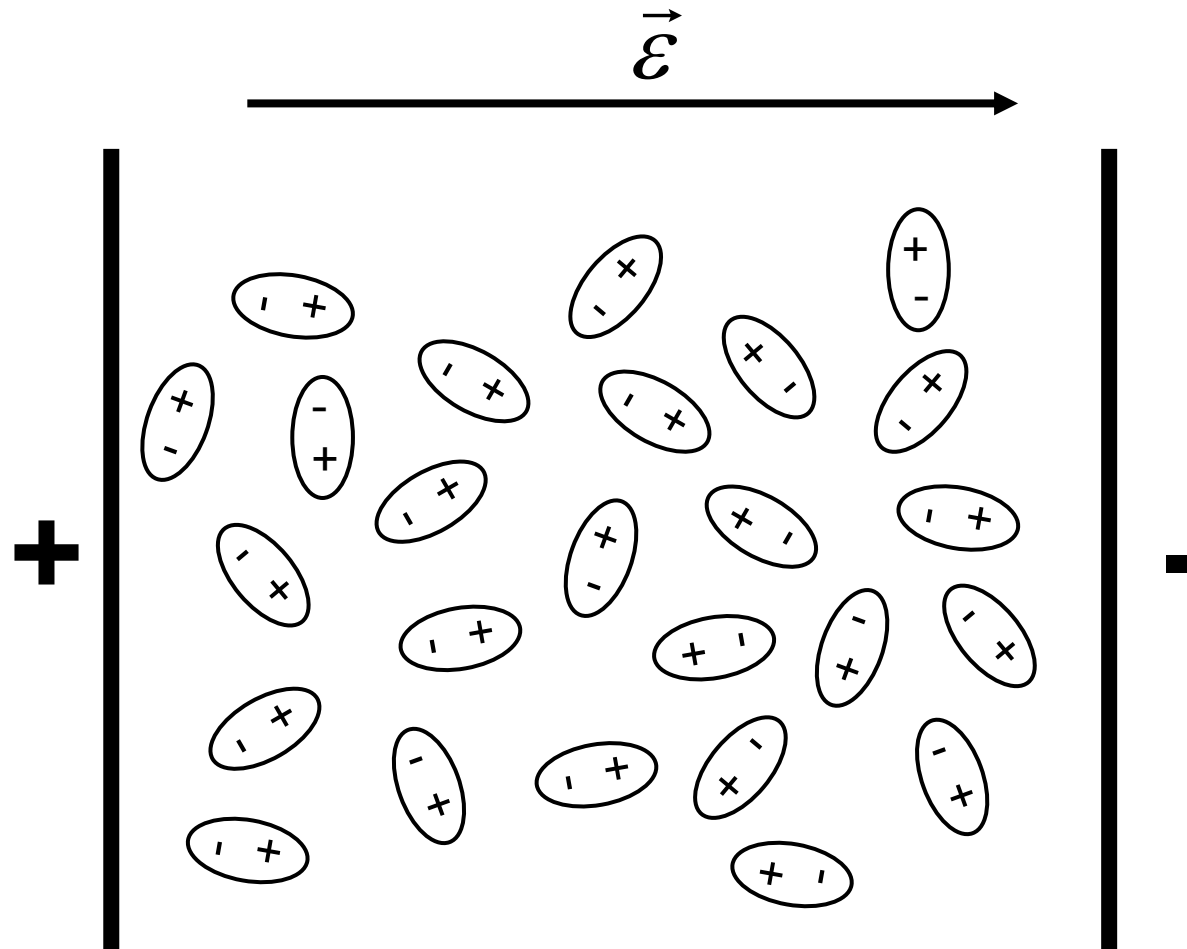
# Polarisation around a dipole

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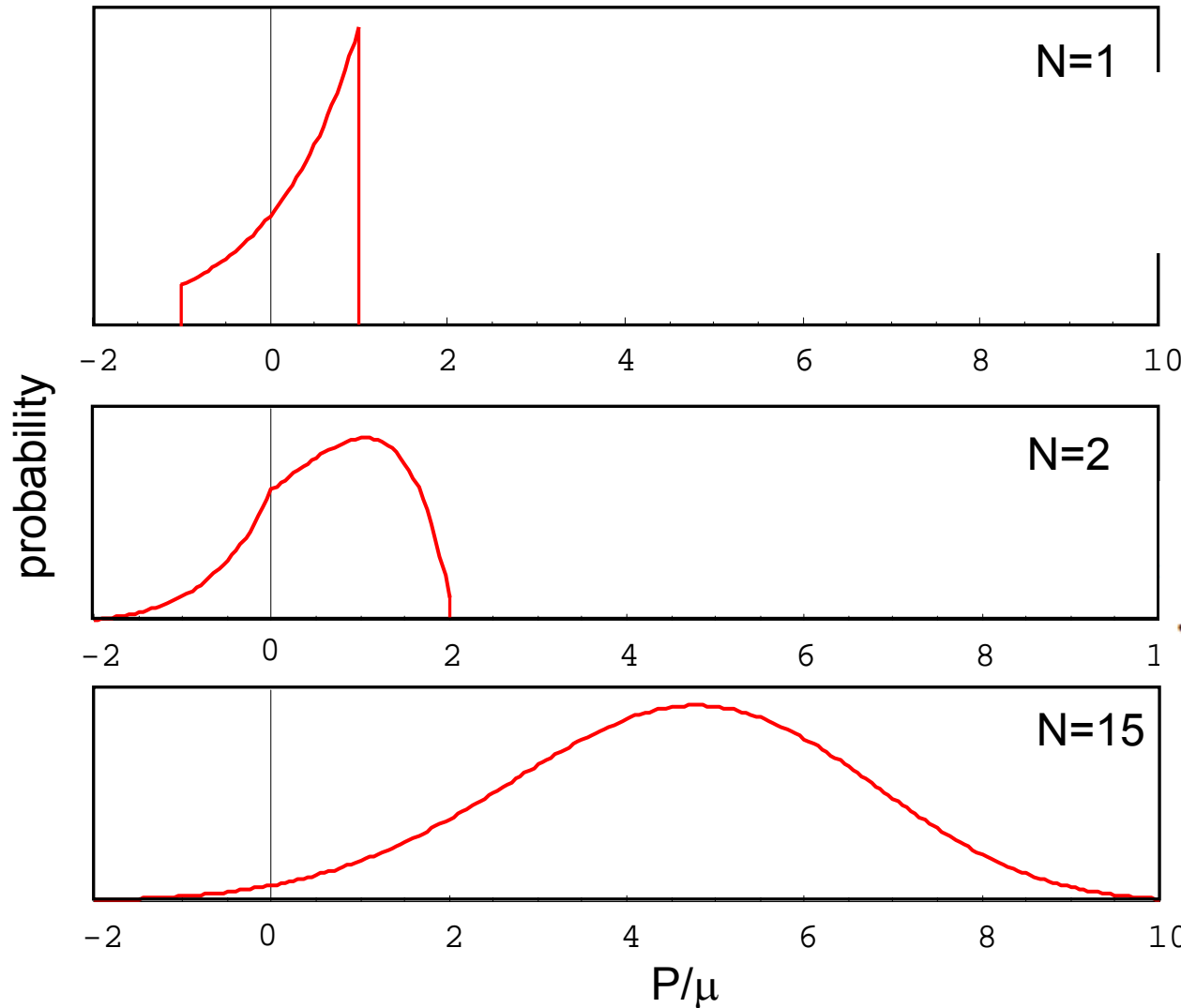
# Polarisation in a Plate Capacitor



Energy of a single solute molecule  $E = -\vec{\epsilon} \cdot \vec{\mu} = -\epsilon_x \mu_x$



# Polarisation in a Plate Capacitor



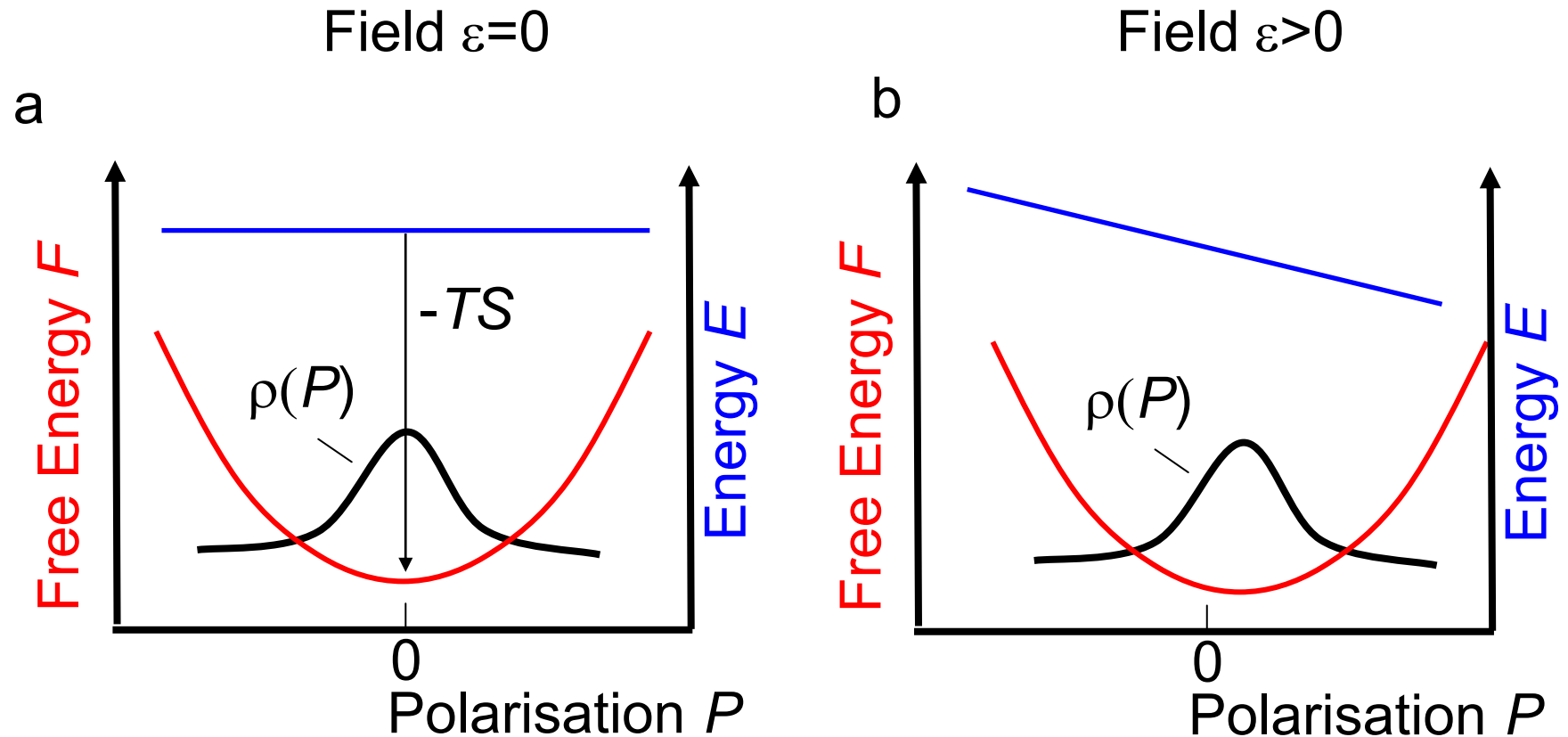
$$\rho(\mu_x) = \frac{1}{n} e^{\frac{\epsilon_x \mu_x}{k_B T}}$$

$$\rho'(P) =$$

$$\int_{-N|\bar{\mu}|}^{+N|\bar{\mu}|} \rho(\mu_x) \rho(P - \mu_x) d\mu_x$$



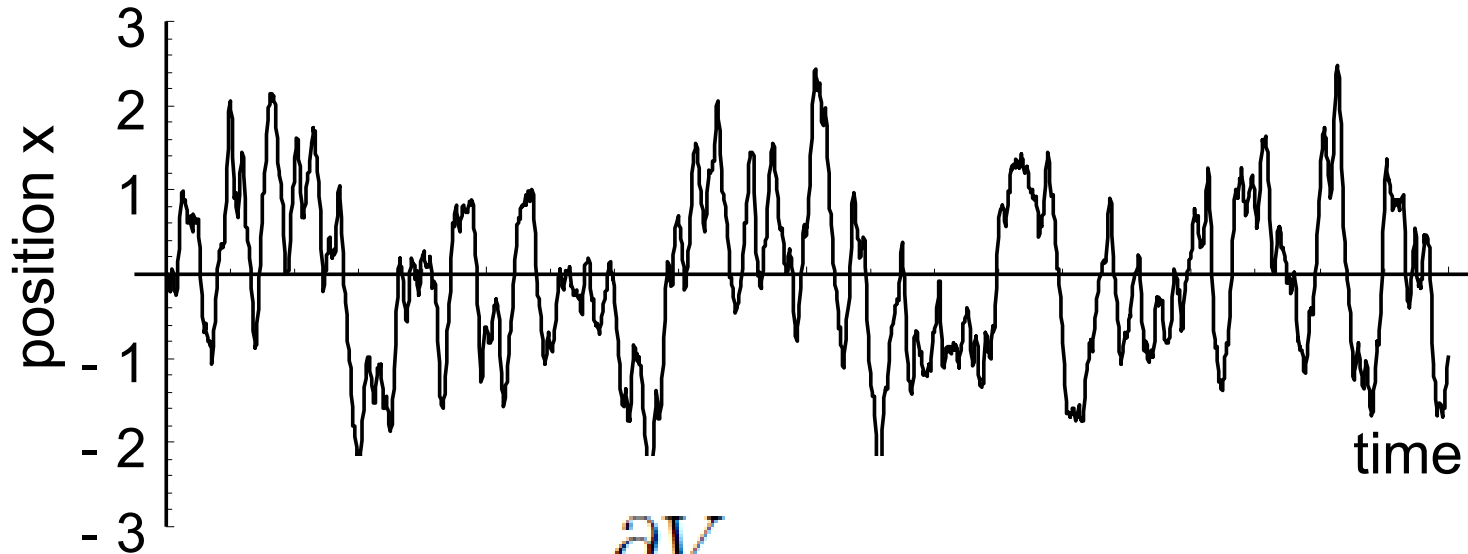
# Polarisation in a Plate Capacitor







# Langevin Dynamics



$$m\ddot{x} = -\frac{\partial V}{\partial x} - \gamma m\dot{x} + \delta F(t)$$

with  $\langle F(0)F(t) \rangle = \delta F_0^2 \cdot \delta(t)$

$$\delta F_0^2 = 2\gamma m k_B T$$

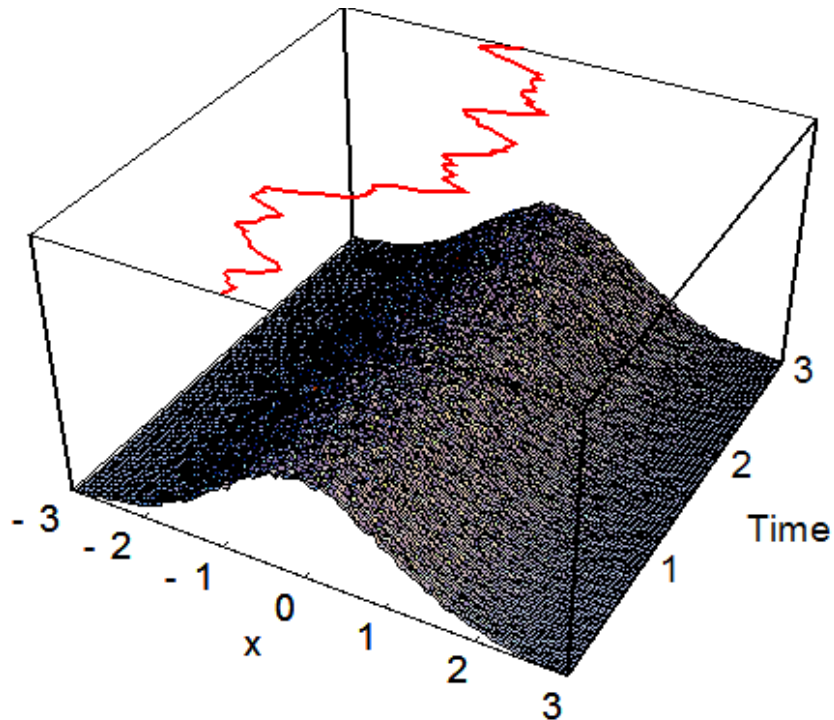
Fluctuation-Dissipation Theorem



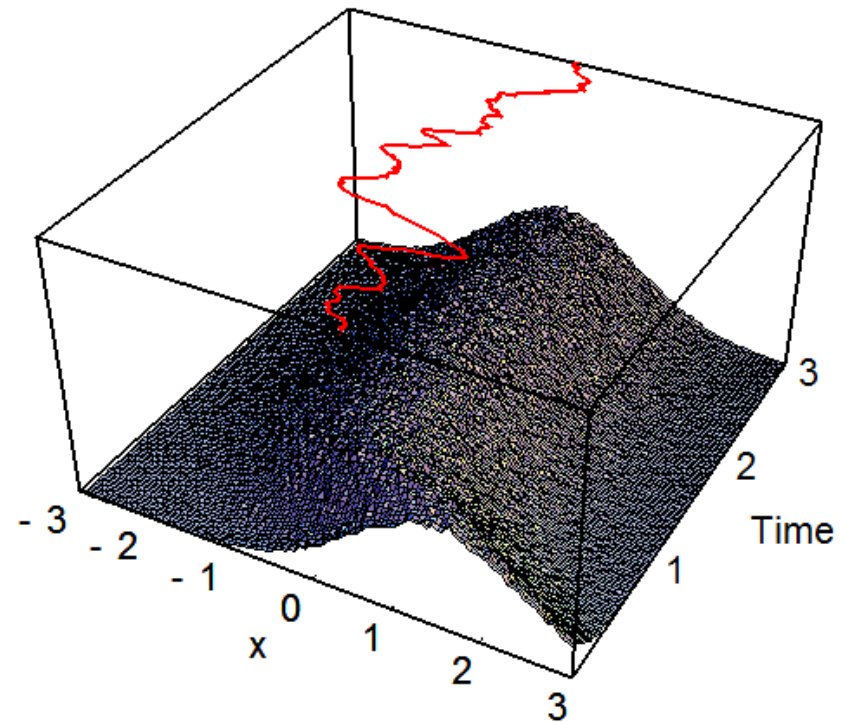
# Ensemble of Particles

thermal equilibrium

$$\rho(x) = e^{-\frac{V(x)}{k_B T}}$$

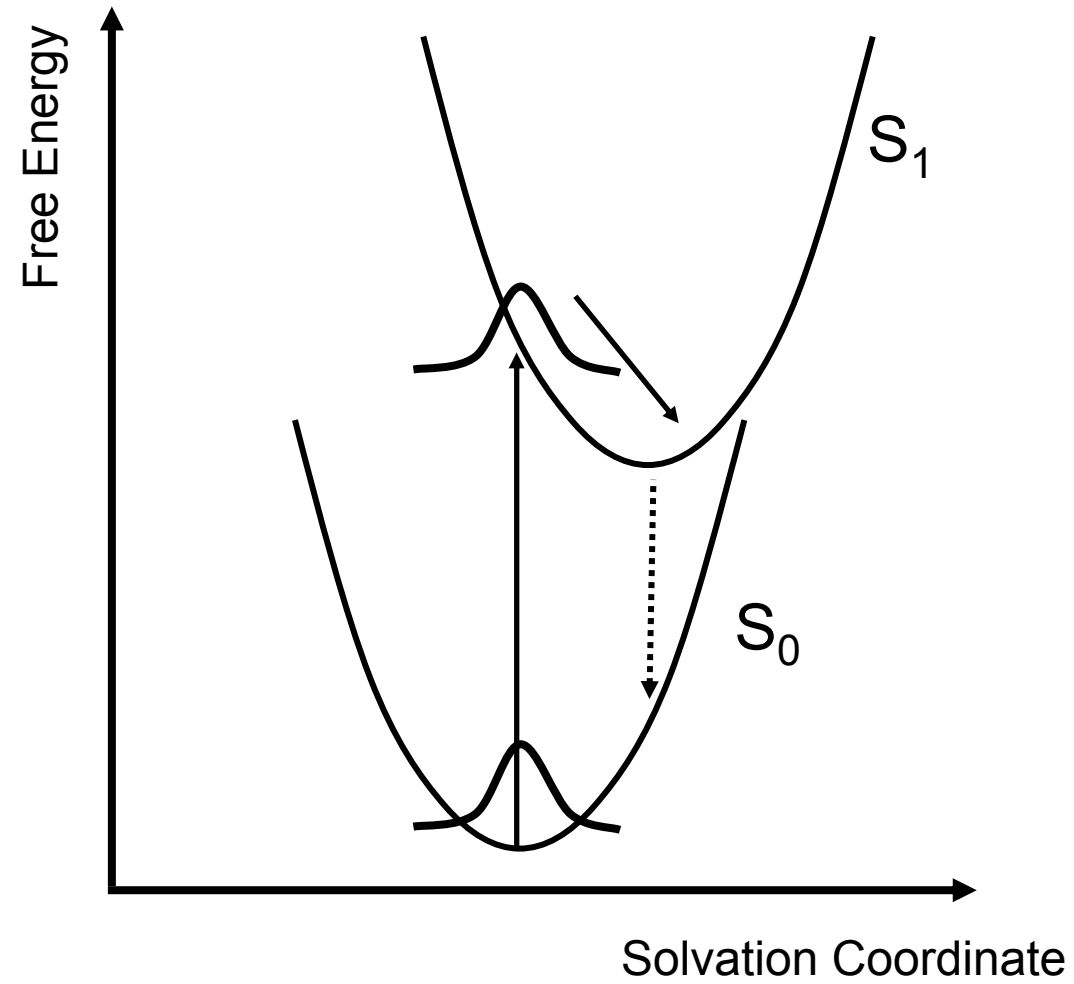


non-equilibrium



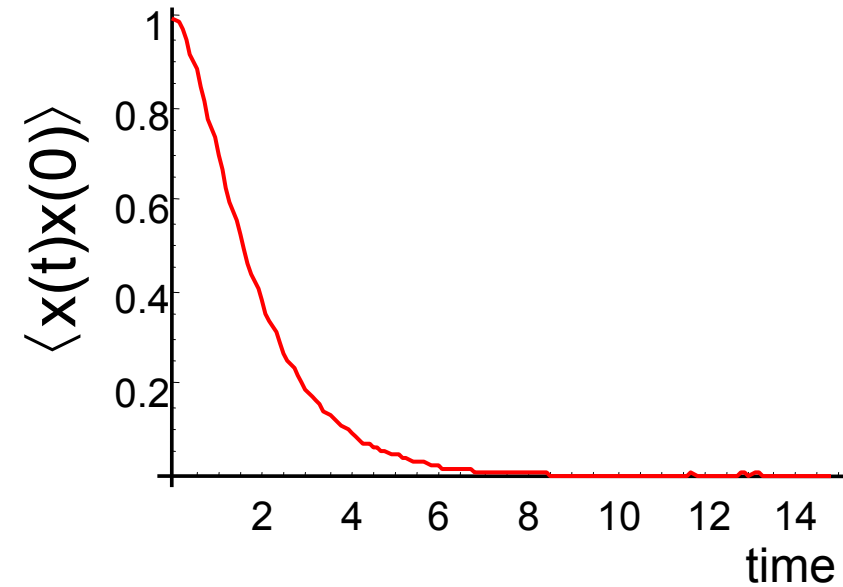
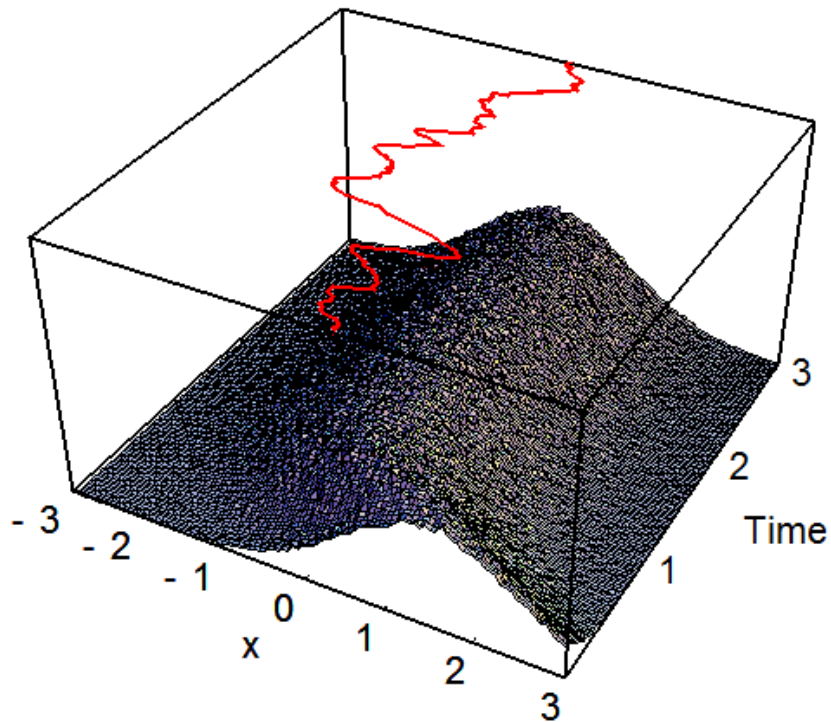


# Solvation





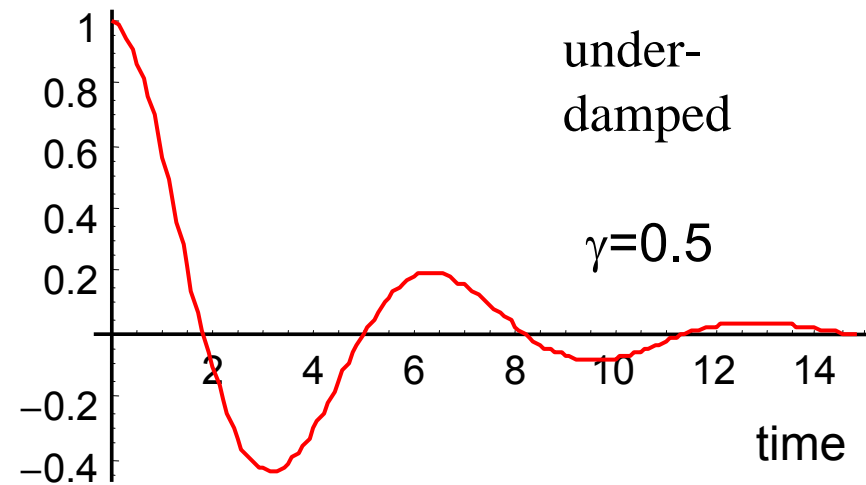
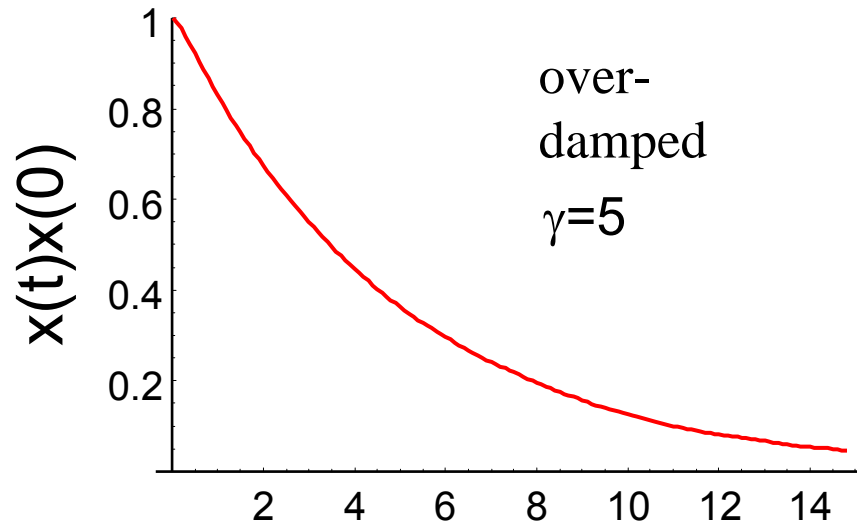
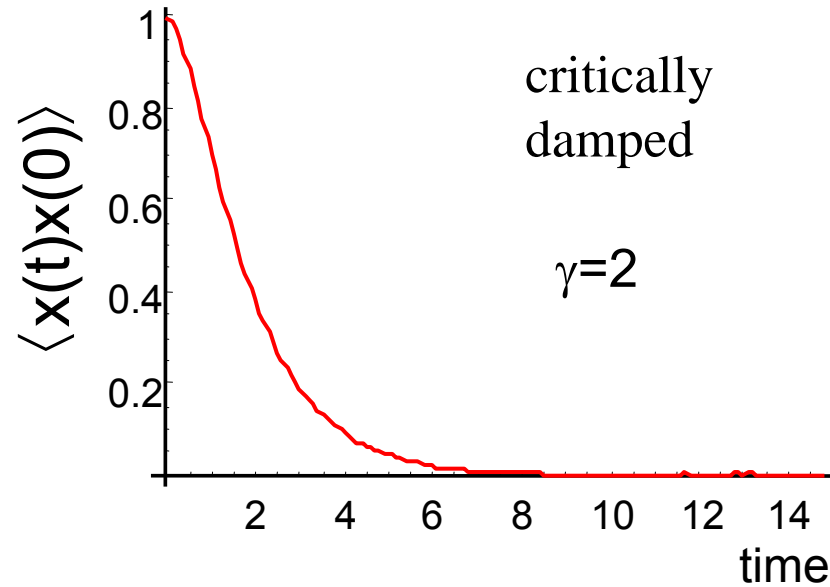
# Onsager Regression Hypothesis



$$\langle x(t) \rangle_{noneq} \propto \langle x(t)x(0) \rangle_{eq}$$



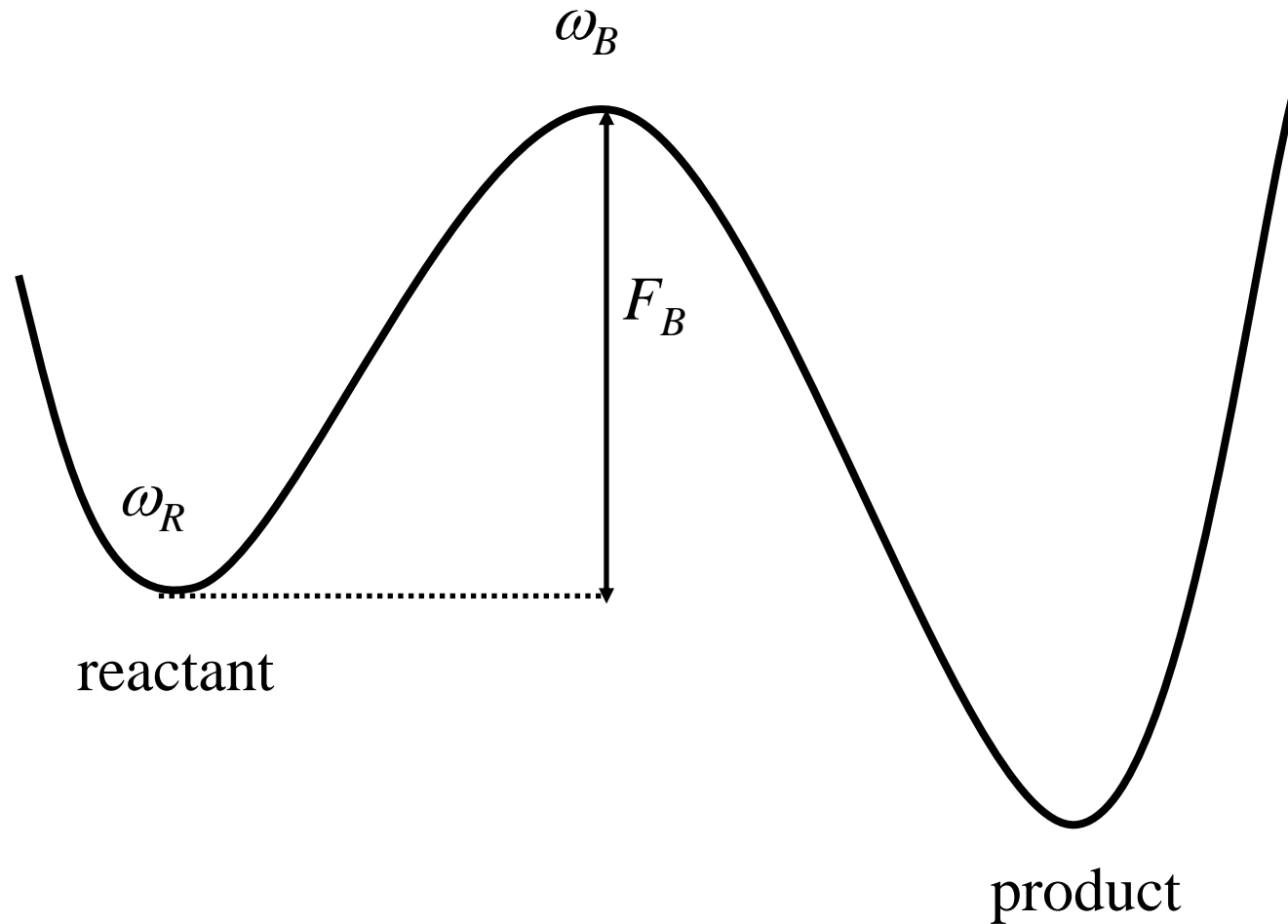
# Correlation Function





# Kramers Theory of Reaction Kinetics

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# Kramers Theory of Reaction Kinetics

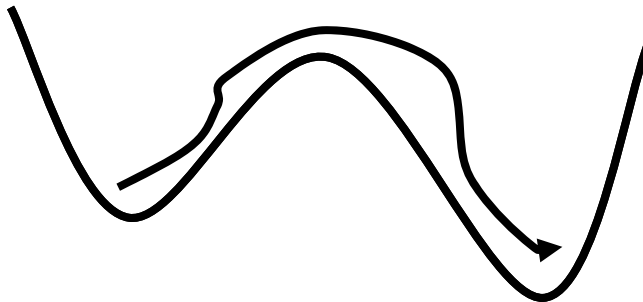
strongly overdamped



$$\gamma \gg \omega_R$$

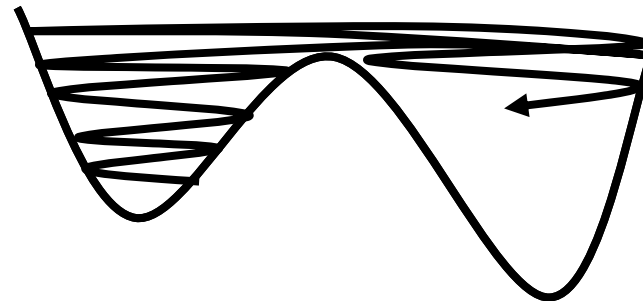
$$k_R = \frac{\omega_B \omega_R}{2\pi\gamma} e^{-\frac{E_b}{k_B T}}$$

critically damped



$$k_R = \frac{1}{\omega_B} \left( -\frac{\gamma}{2} + \sqrt{\frac{\gamma^2}{4} - \omega_B^2} \right) \left\{ \frac{\omega_R}{2\pi} e^{-\frac{E_b}{k_B T}} \right\}$$

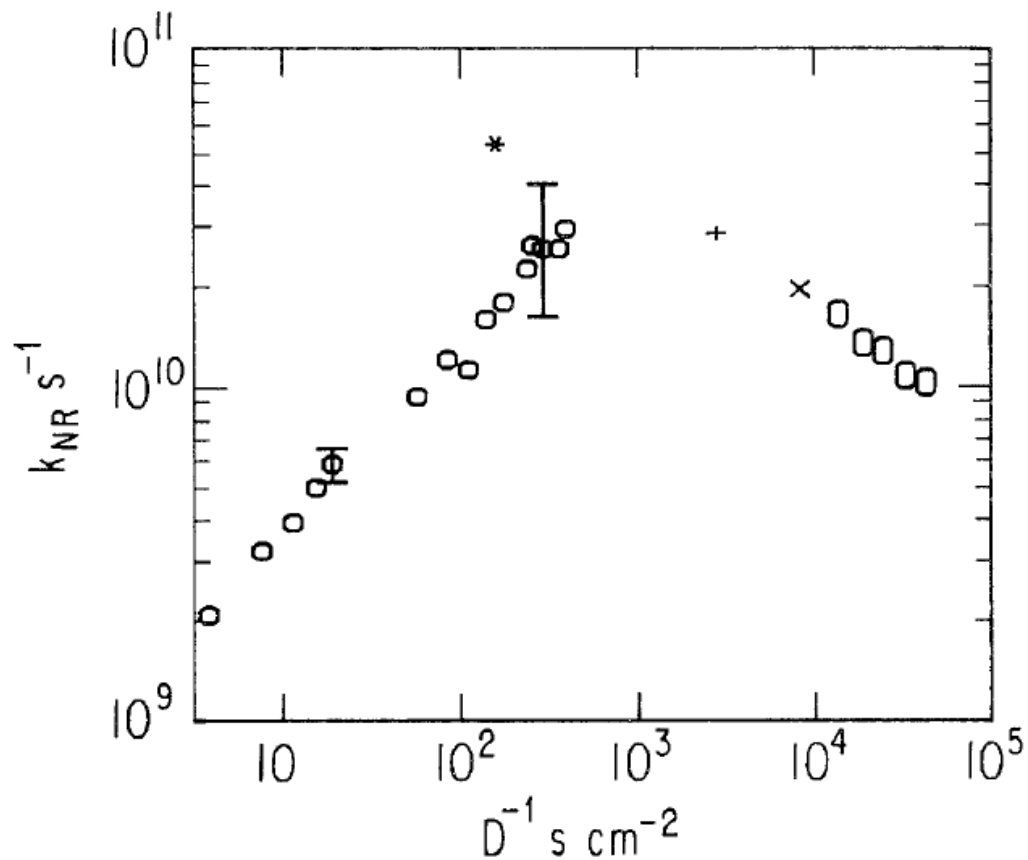
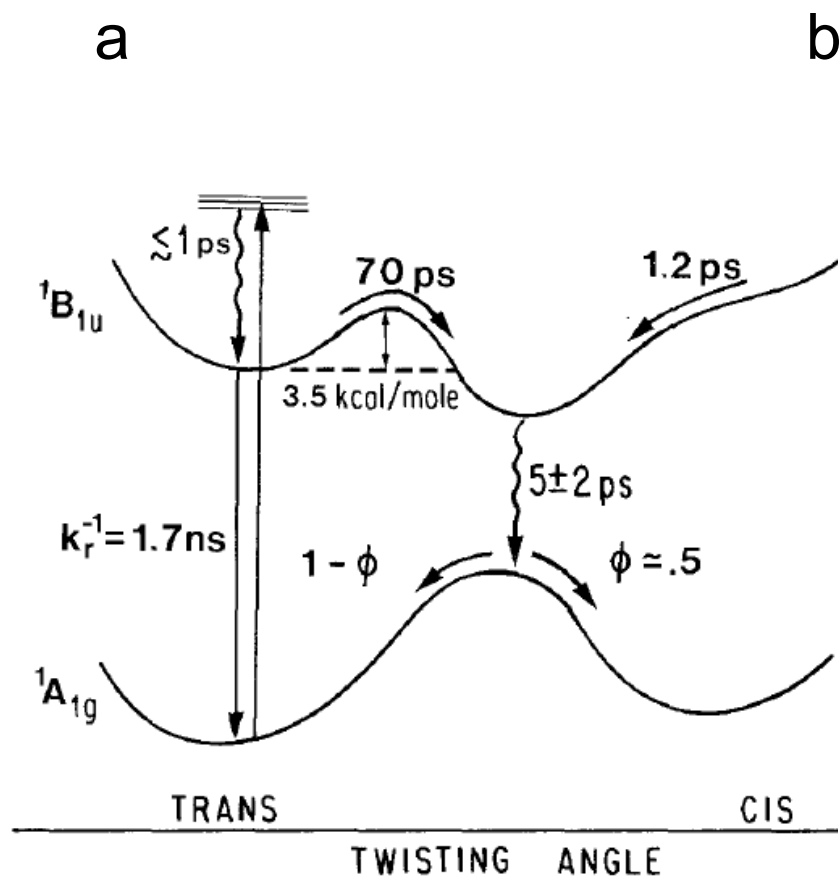
under-damped



$$k_R = p\gamma \frac{I(E_b)}{k_B T} \left\{ \frac{\omega_R}{2\pi} e^{-\frac{E_b}{k_B T}} \right\}$$



# Photoisomerisation of Stilbene: Dependence on Solvent Viscosity







# Femtochemistry: Basic Concepts

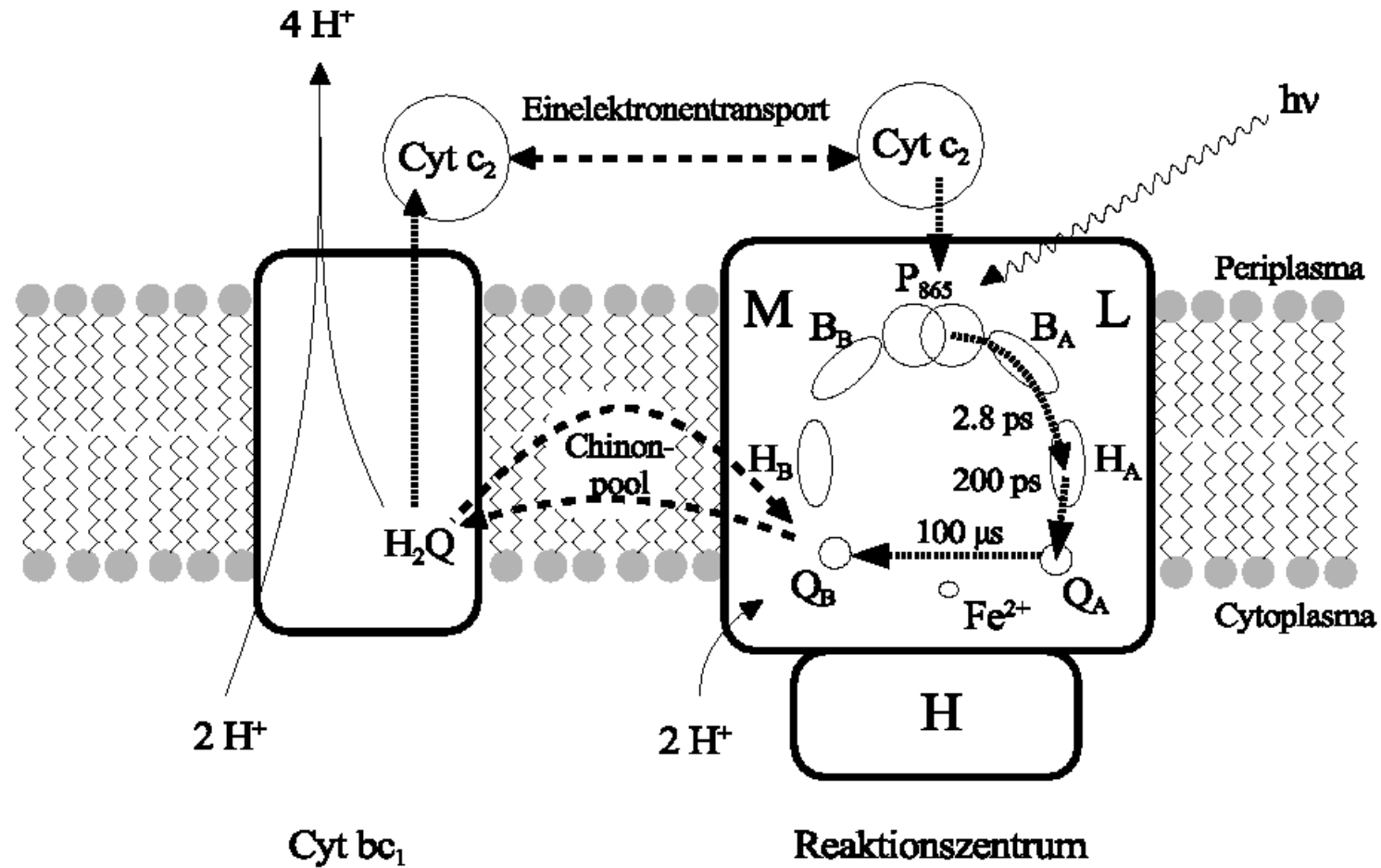
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- Examples of Photochemical Reactions
- Experimental Methods
- Motion in Quantum Mechanics: Wavepackets
- Franck-Condon Transition
- Jablonski Diagram, Fermi Golden Rule, Energy Gap Law
- Prototype Potential Energy Surfaces
- Non-Crossing Rule, Avoided Crossings, Conical Intersections
- Born Oppenheimer Approximation and its Breakdown
- Adiabatic and Diabatic Surfaces
- Mixed Quantum-Classical Methods, Landau Zener Theory
- Solvation
- **Electron Transfer Theory**
- Excitation Transfer: Exciton- and Förster Transfer





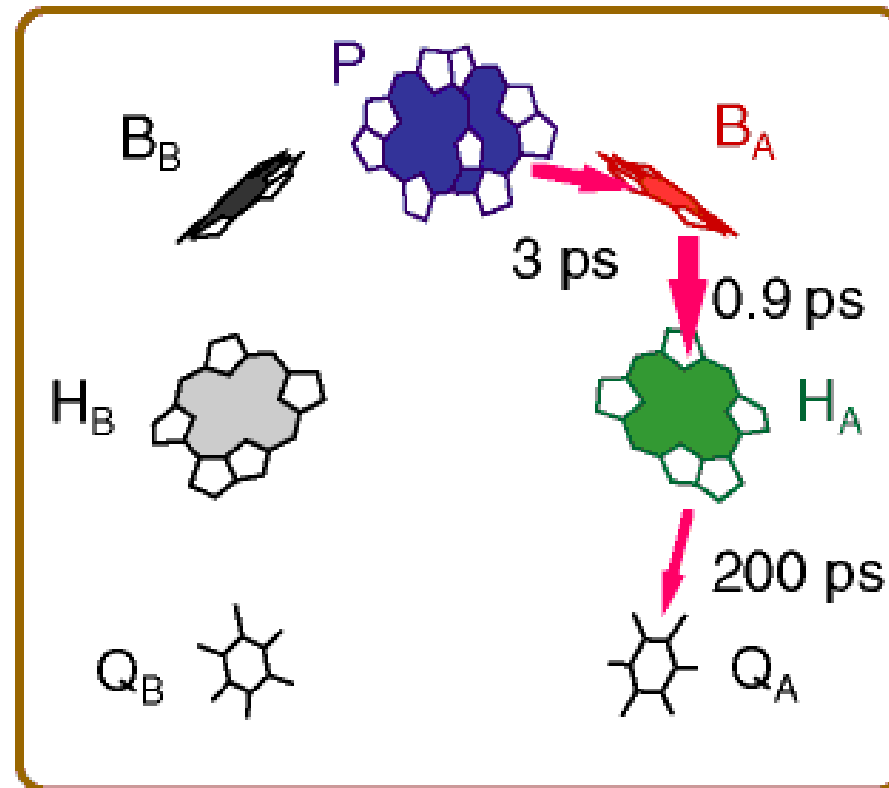
# Photochemical Reactions in Nature: Electron Transfer in Photosynthesis





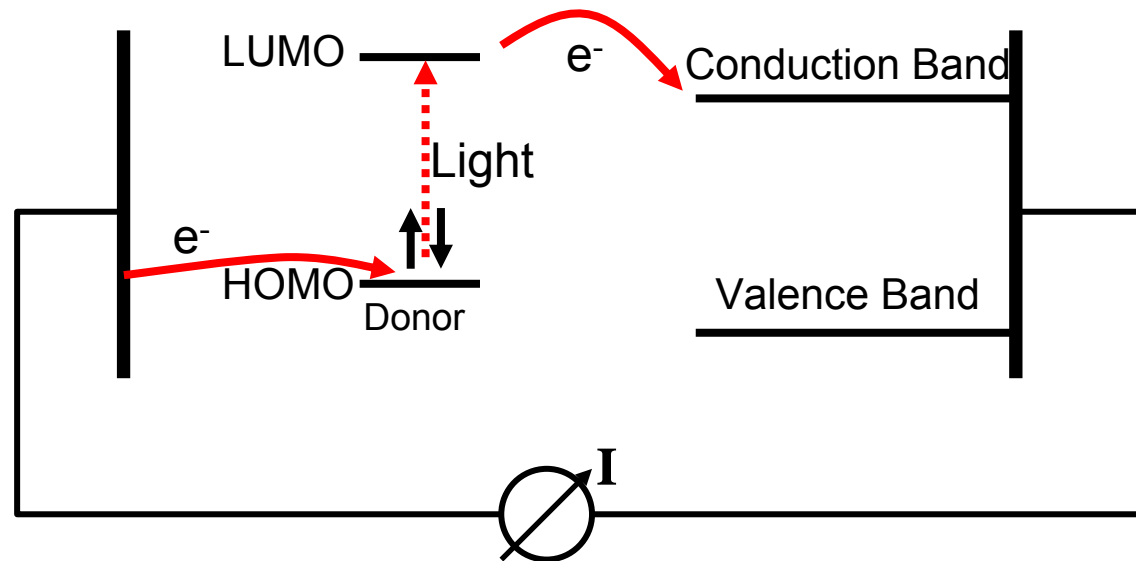
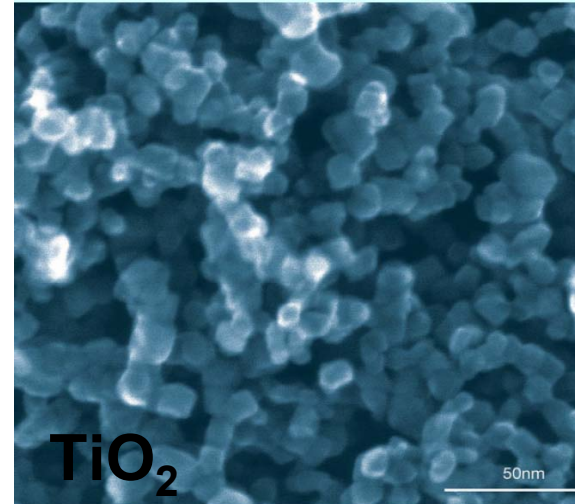
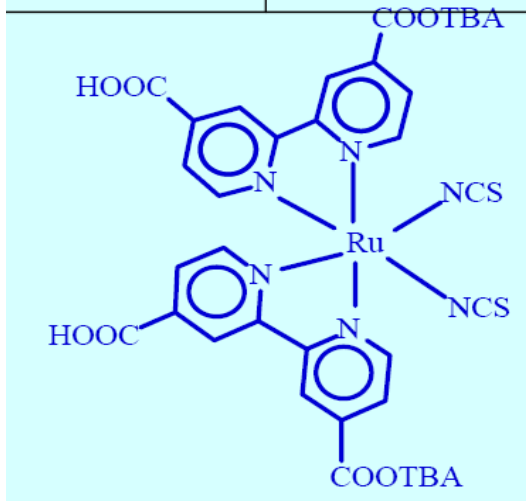
# Photochemical Reactions in Nature: Electron Transfer in Photosynthesis

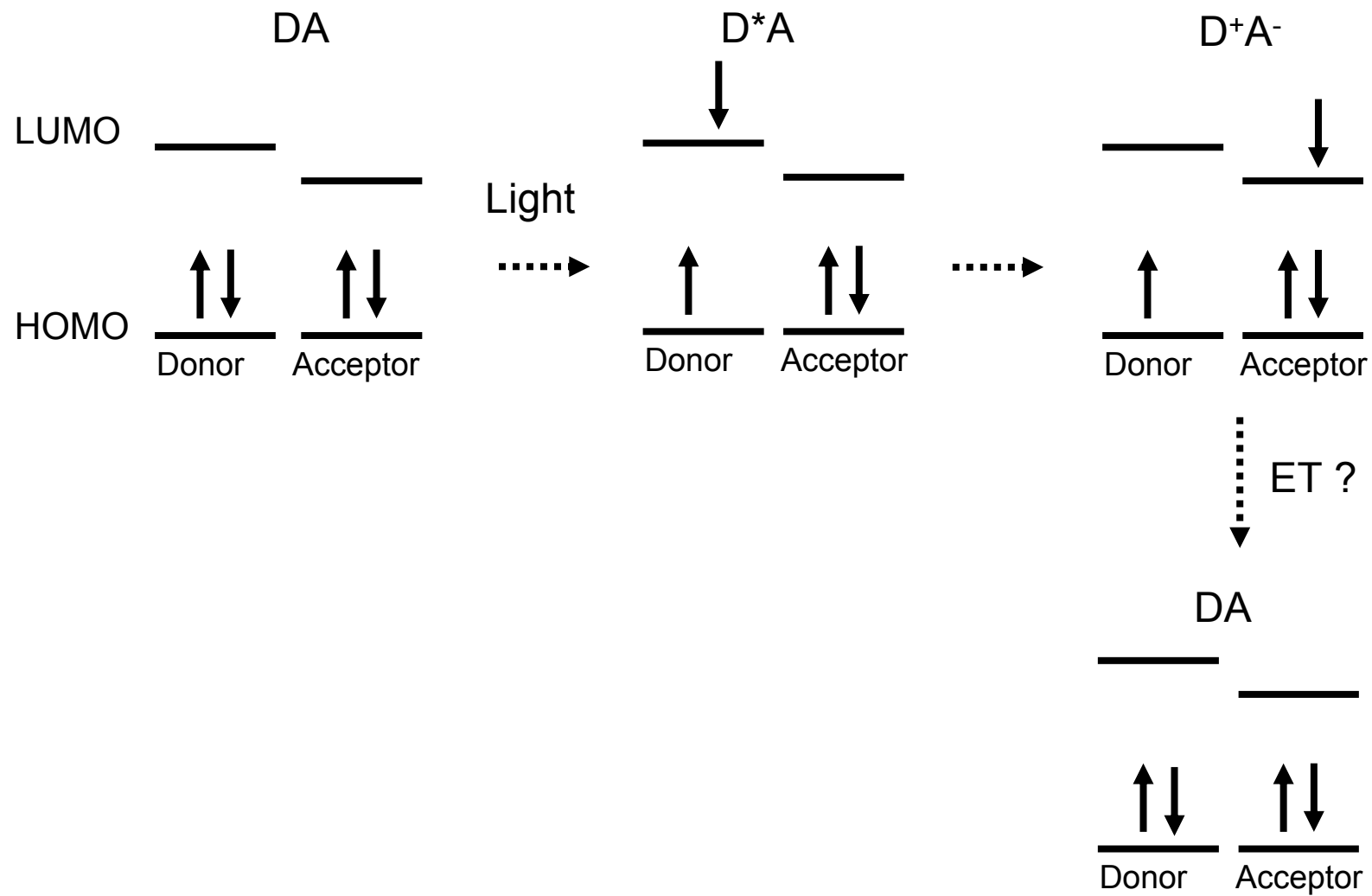
## Der primäre Elektronentransfer im Reaktionszentrum

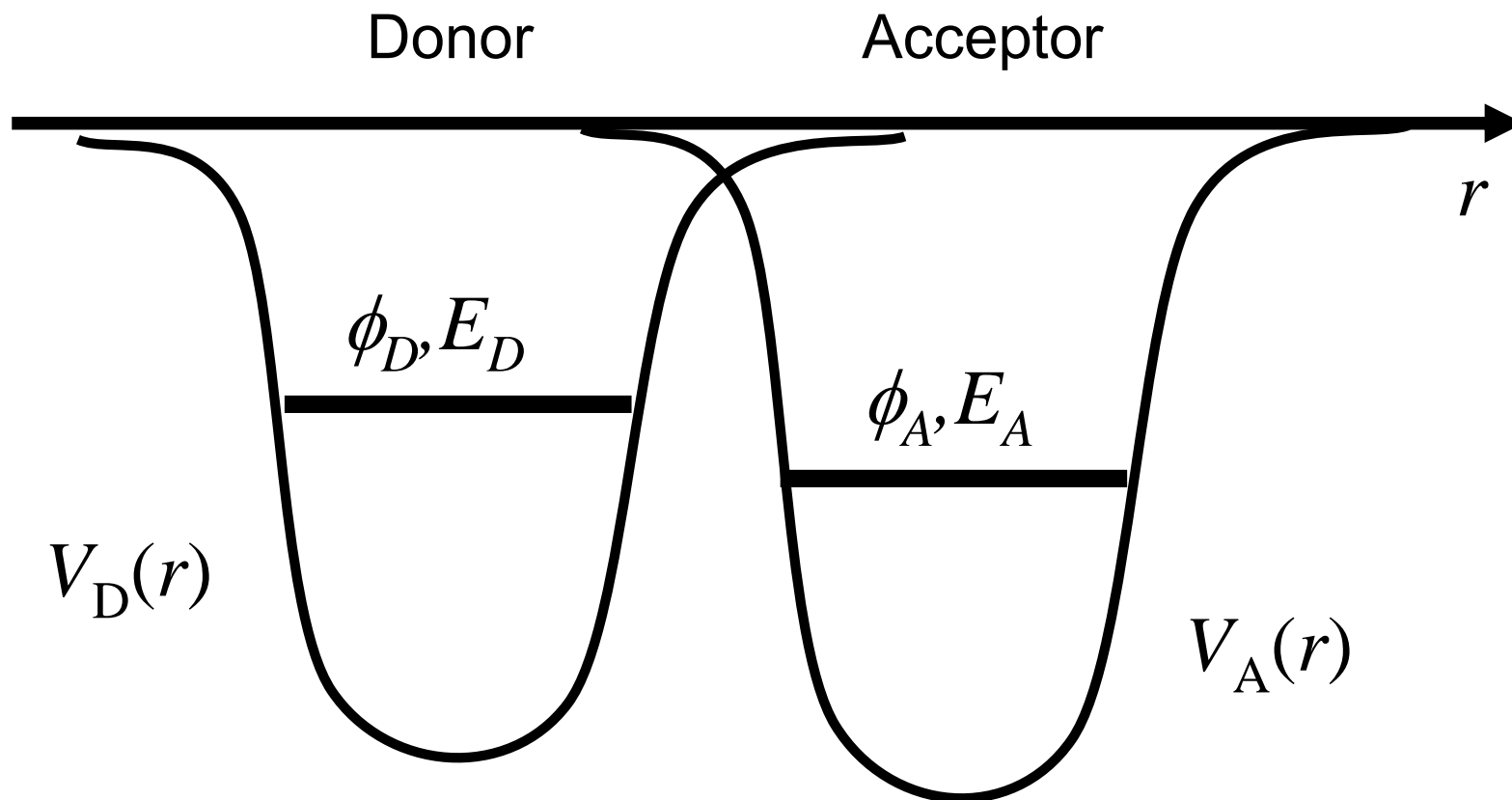




# Artificial Photosynthesis: Grätzel Cell





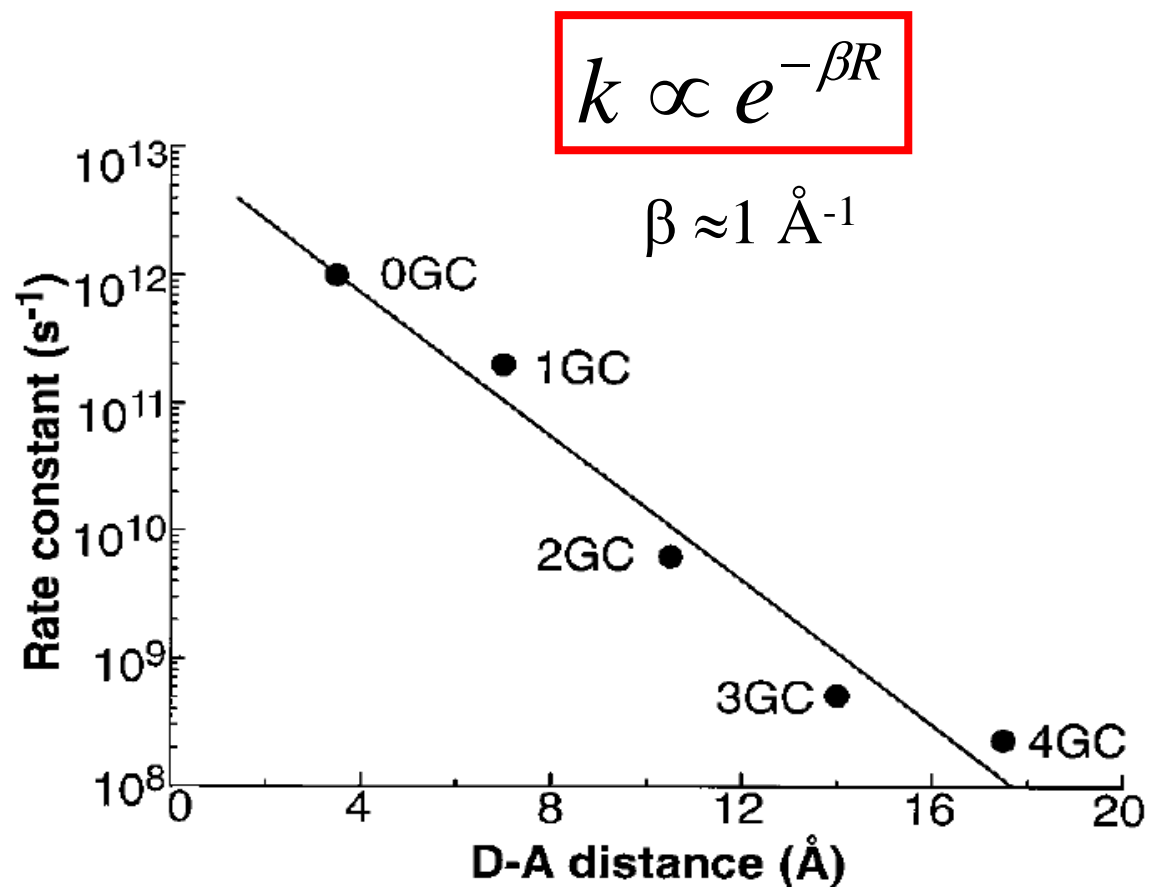
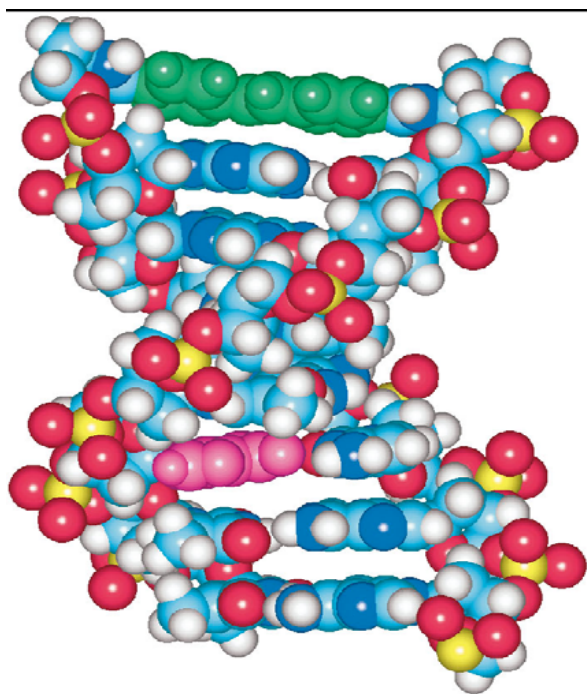


$$H_{el} = \begin{pmatrix} E_{DA} & V_{DA} \\ V_{DA} & E_{D+A^-} \end{pmatrix}$$

$$V_{DA} \propto e^{-\beta r_{DA}}$$



# Distance Dependence of Electron Transfer



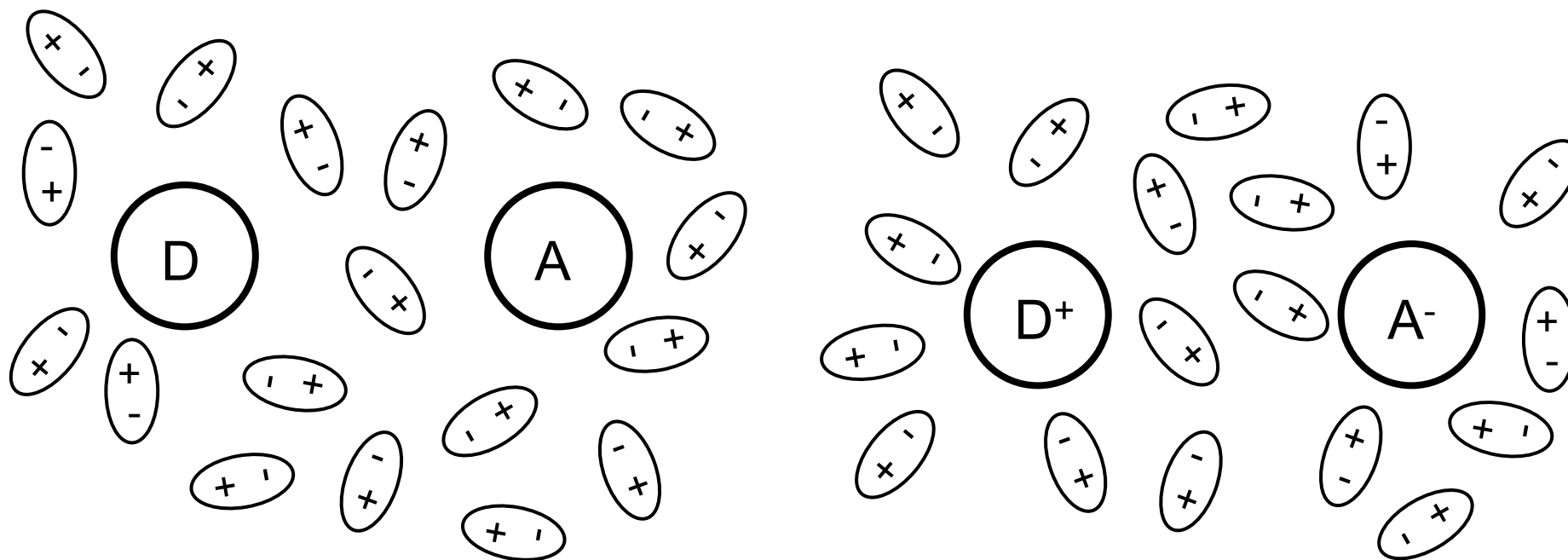
F. D. Lewis,\* T. Wu, Y. Zhang, R. L. Letsinger, S. R. Greenfield, M. R. Wasielewski, *Distance-Dependent Electron Transfer in DNA Hairpins* Science 277 (1997) 673





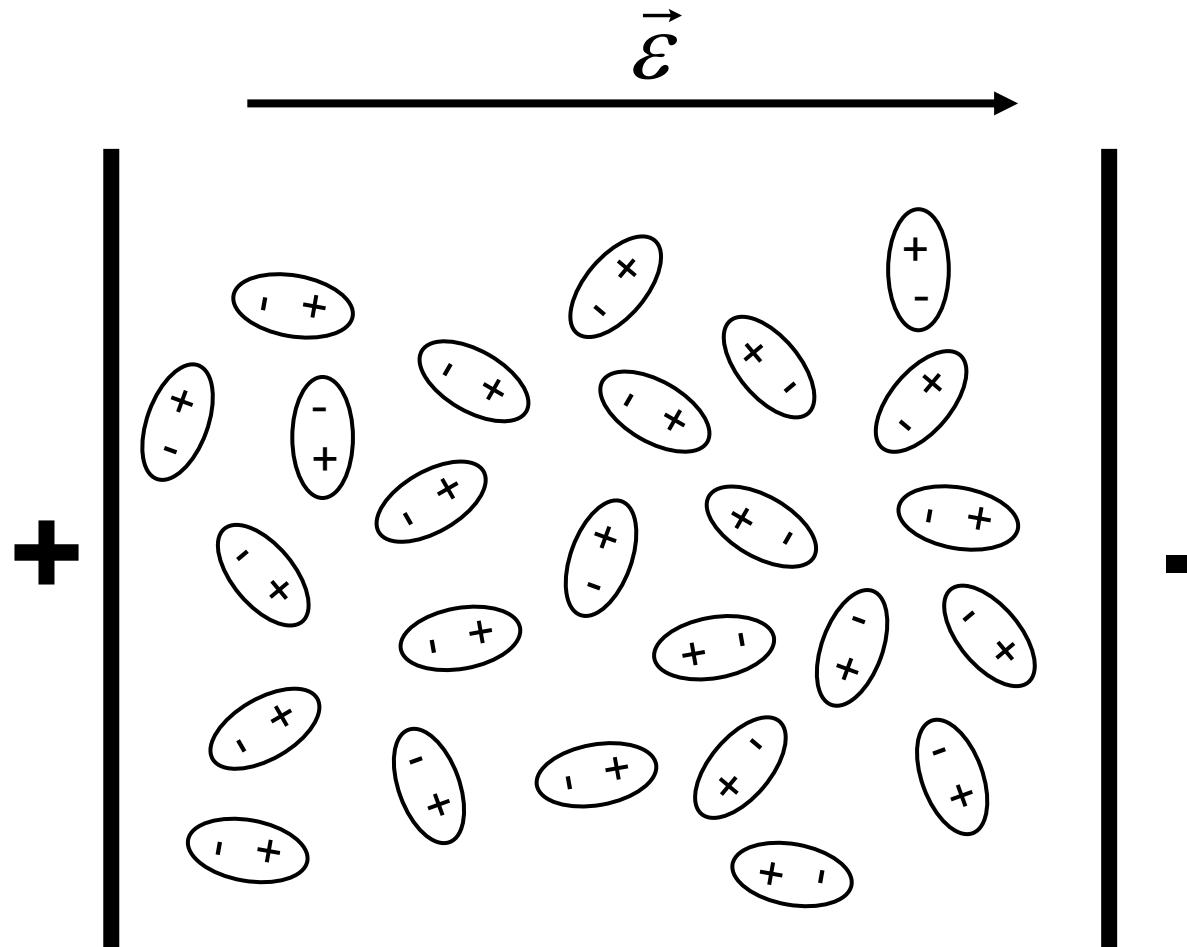
# Solvation of a Charge Transfer Complex

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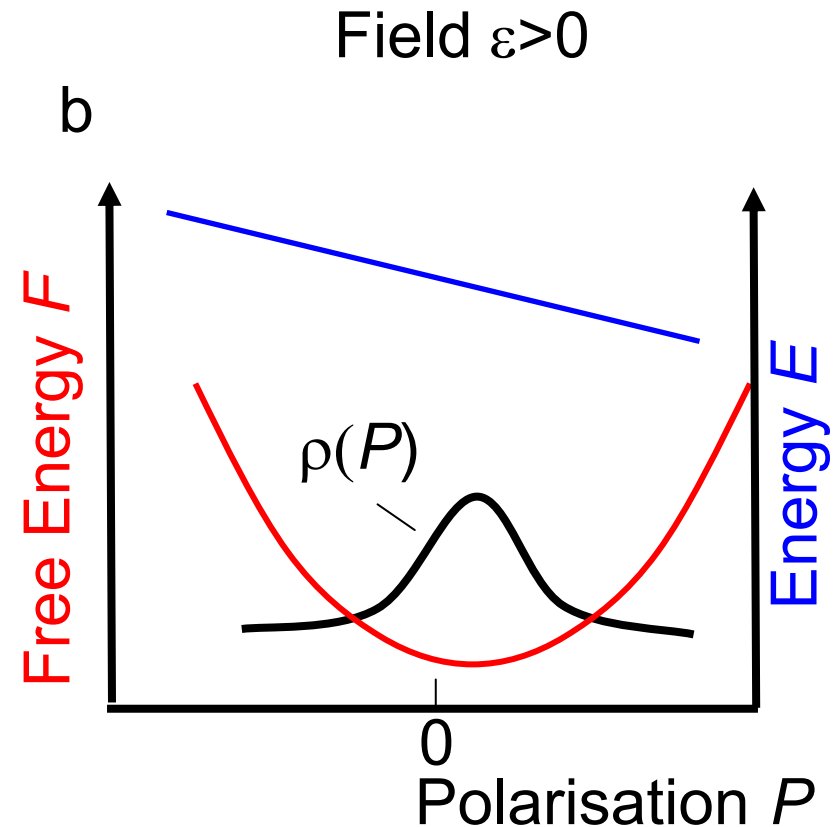
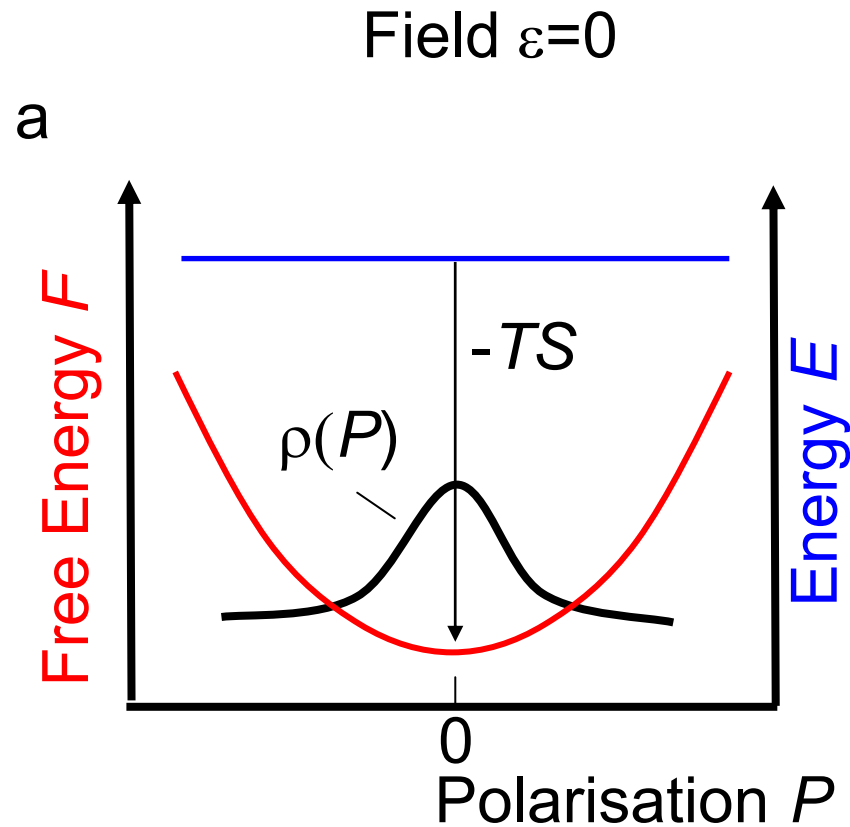
# Polarisation in a Plate Capacitor



Energy of a single solute molecule  $E = -\vec{\epsilon} \cdot \vec{\mu} = -\epsilon_x \mu_x$

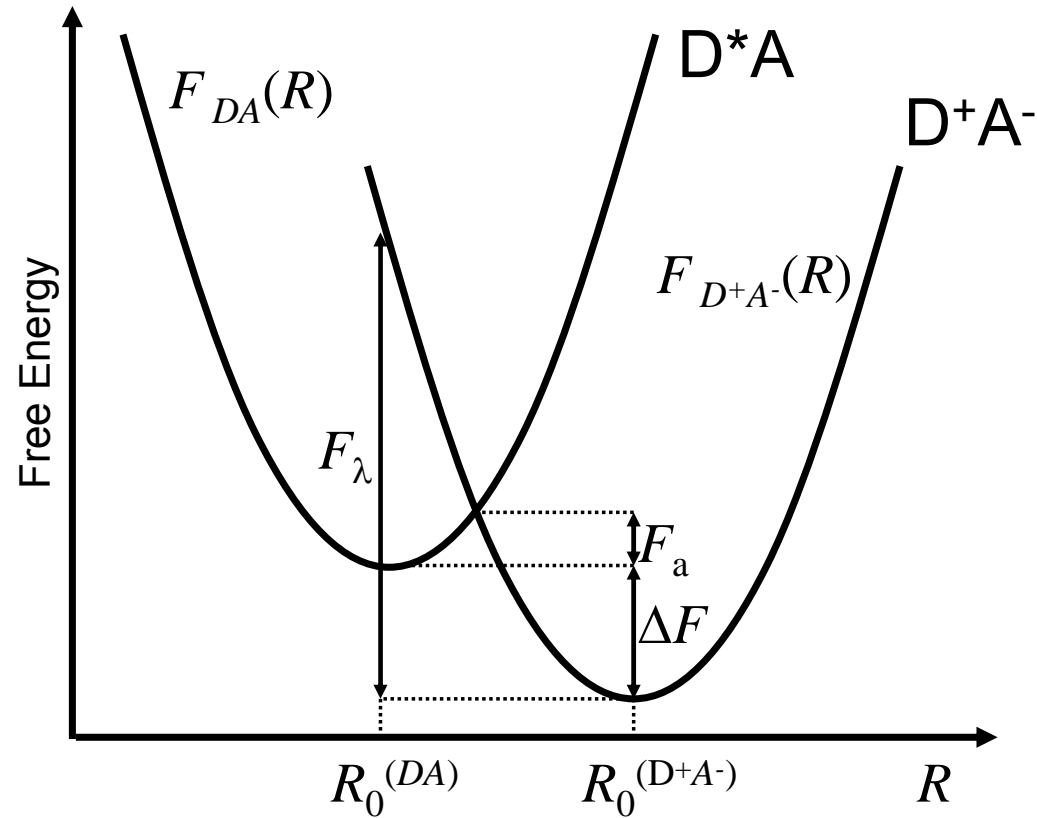


# Polarisation in a Plate Capacitor





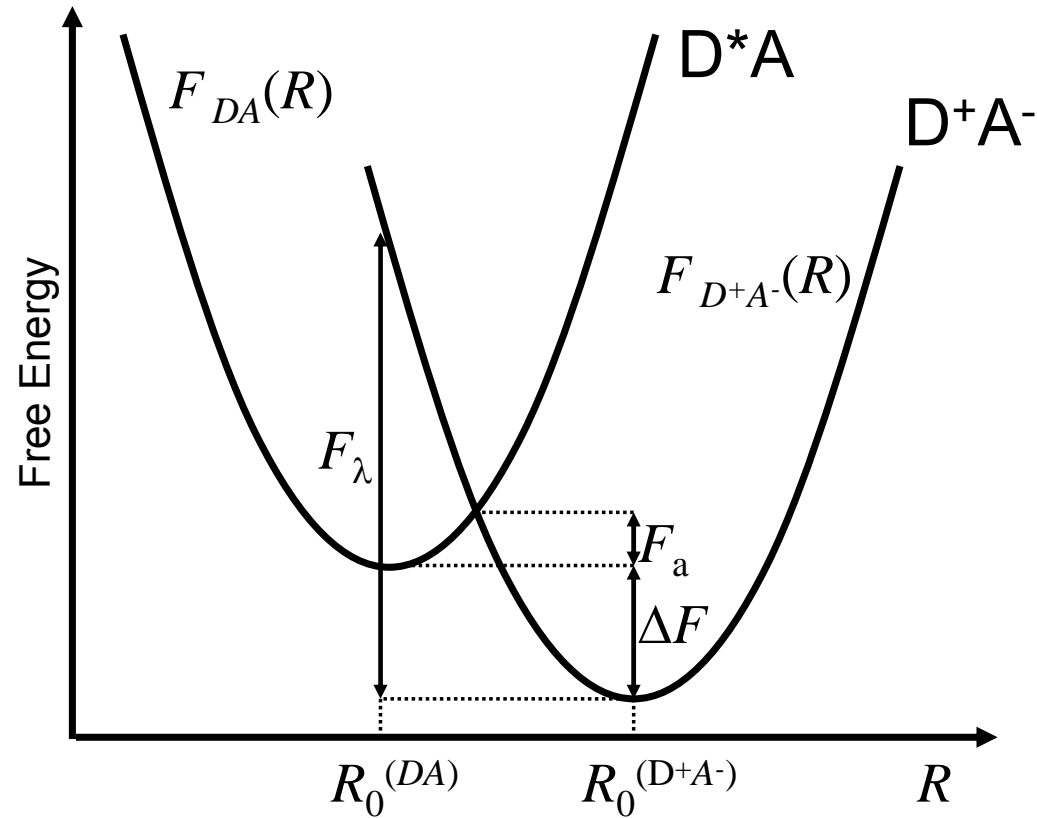
# Marcus Theory of Electron Transfer



$$k_{ET} = V_{DA}^2 \sqrt{\frac{\pi}{\hbar^2 k_B T F_\lambda}} \exp\left(-\frac{F_a}{k_B T}\right)$$



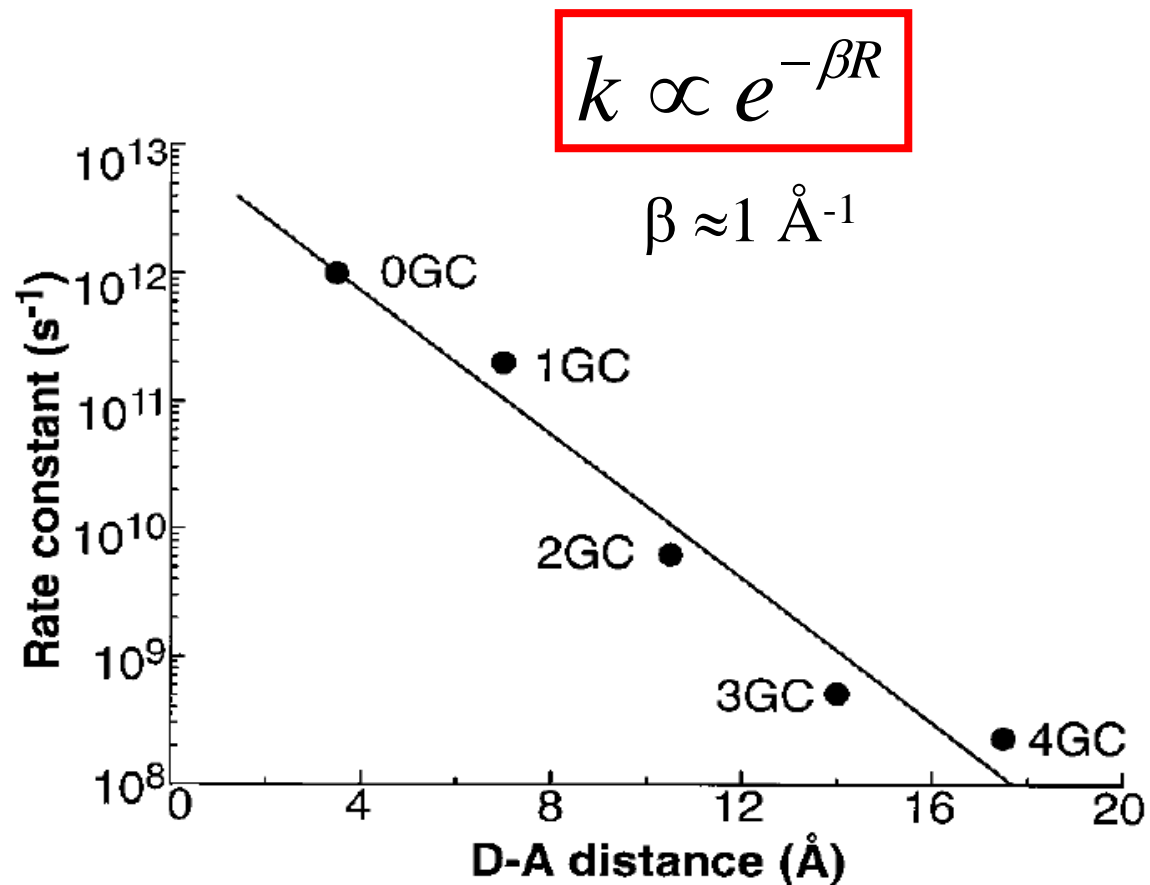
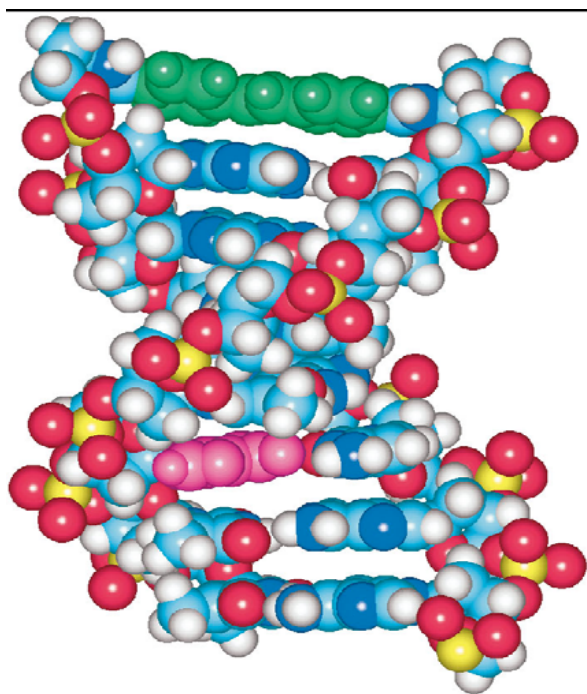
# Marcus Theory of Electron Transfer



$$k_{ET} = V_{DA}^2 \sqrt{\frac{\pi}{\hbar^2 k_B T F_\lambda}} \exp\left(-\frac{(\Delta F - F_\lambda)^2}{4F_\lambda k_B T}\right)$$



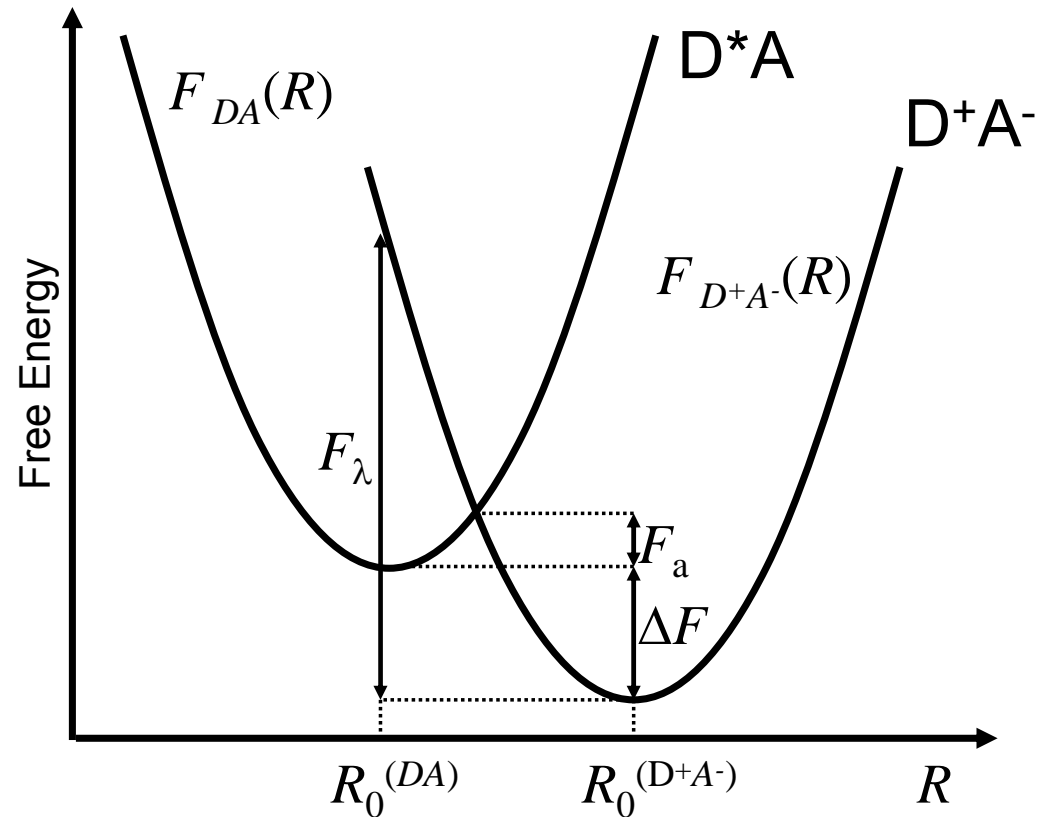
# Distance Dependence of Electron Transfer



F. D. Lewis,\* T. Wu, Y. Zhang, R. L. Letsinger, S. R. Greenfield, M. R. Wasielewski, *Distance-Dependent Electron Transfer in DNA Hairpins* Science 277 (1997) 673



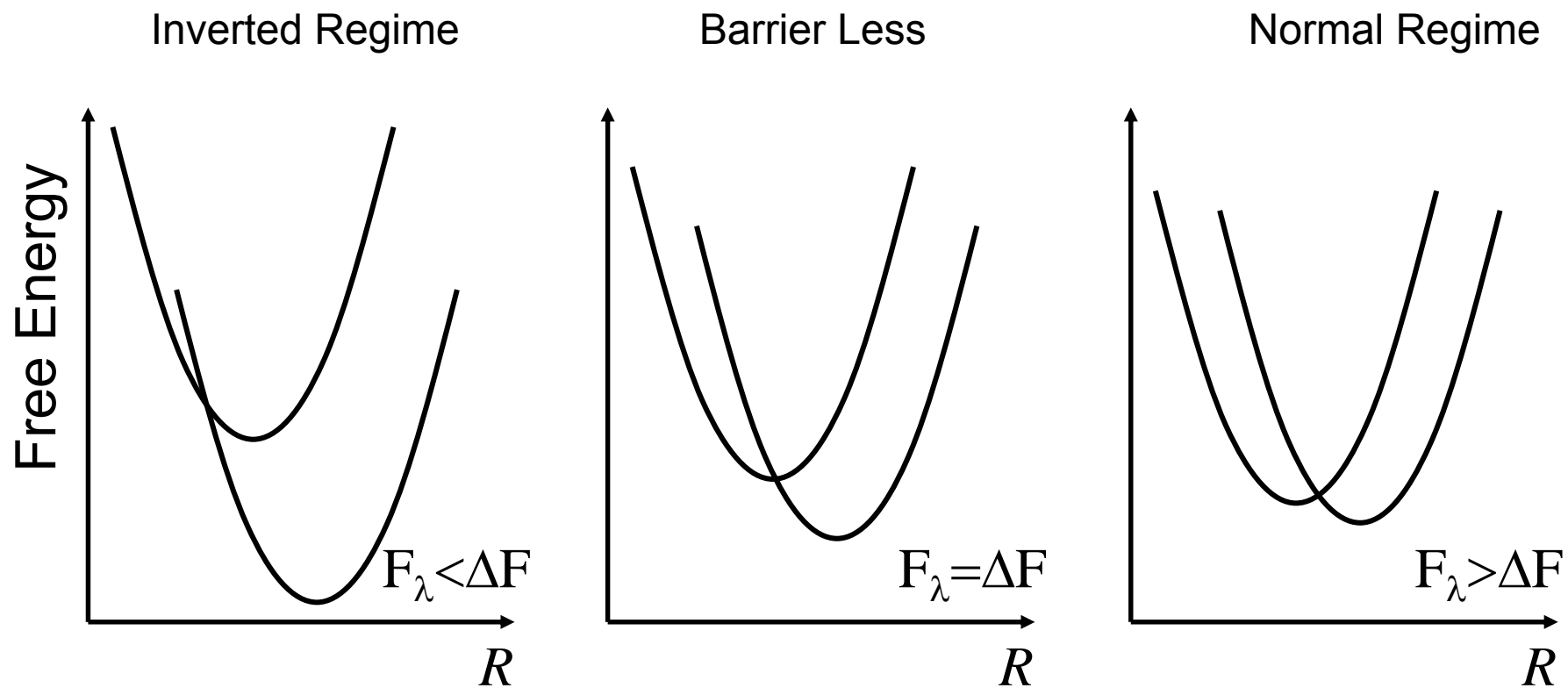
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# Marcus Theory of Electron Transfer

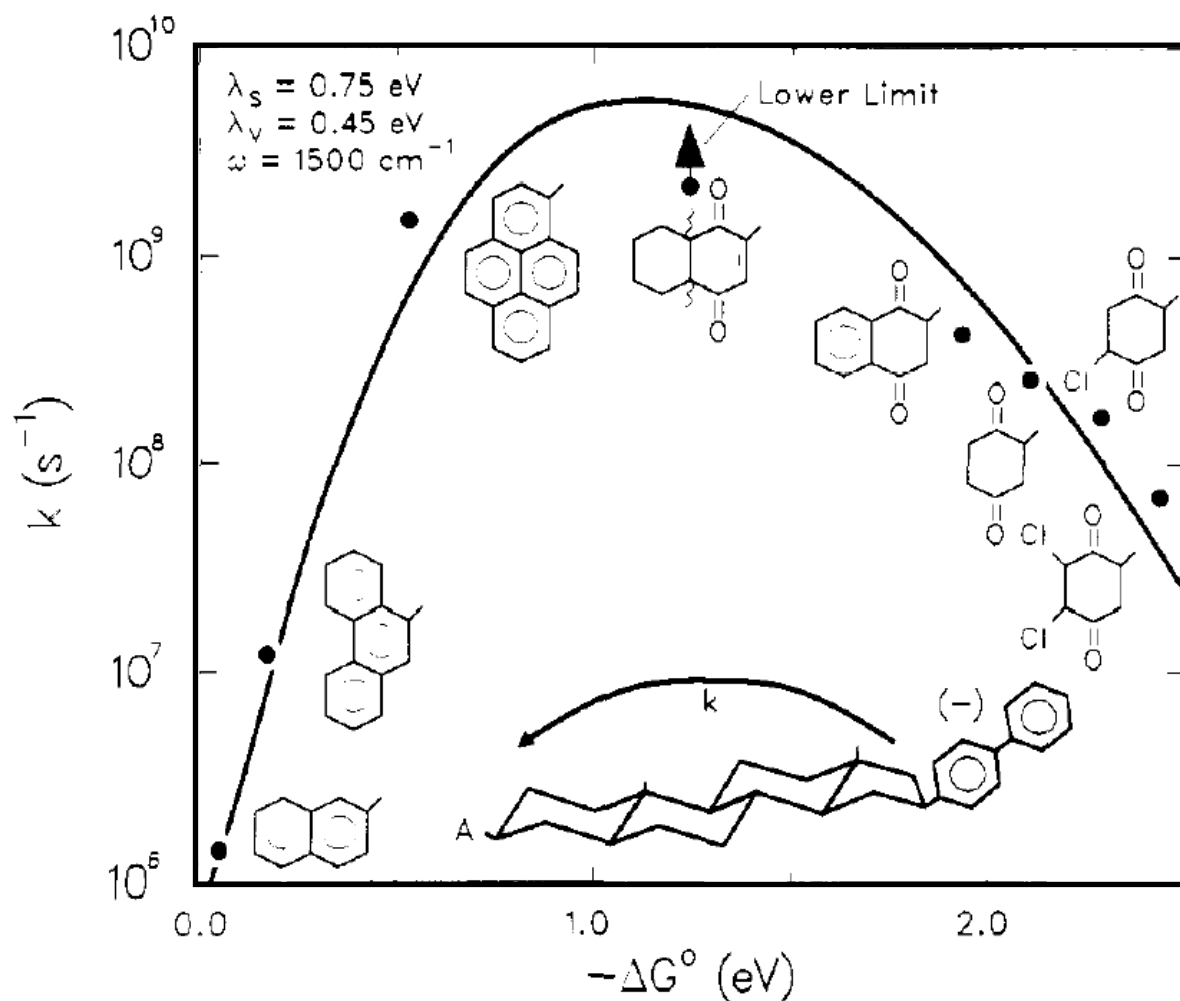


$$k_{ET} = V_{DA}^2 \sqrt{\frac{\pi}{\hbar^2 k_B T F_\lambda}} \exp\left(-\frac{(\Delta F - F_\lambda)^2}{4F_\lambda k_B T}\right)$$





# Marcus Parabola

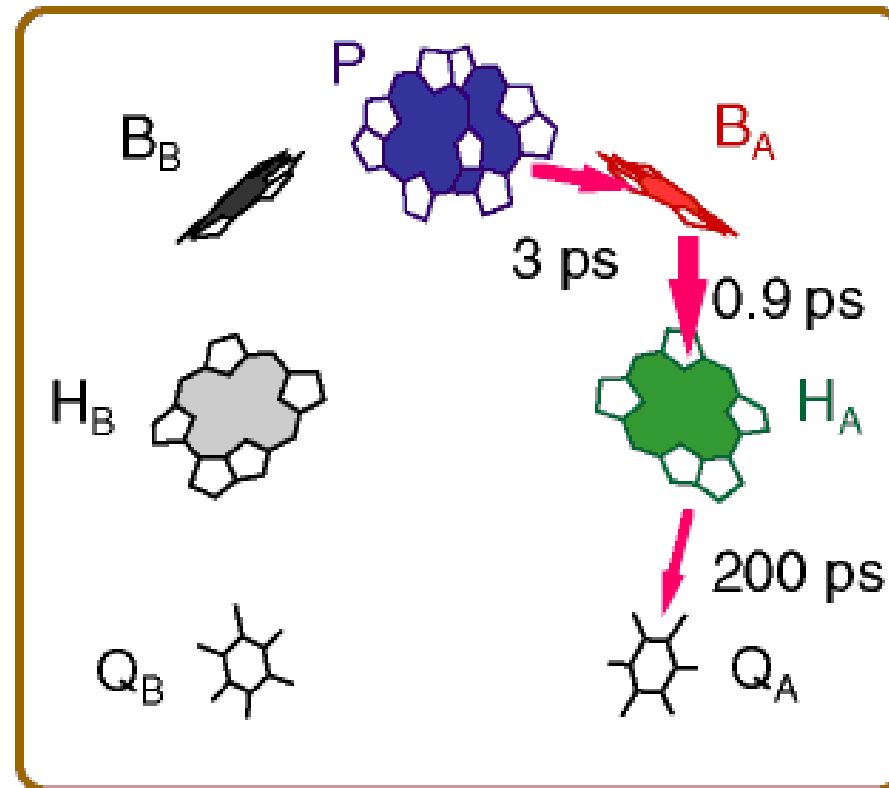


J. R. Miller, L. T. Calcaterra, G. L. Closs *Intramolecular long-distance electron transfer in radical anions. The effects of free energy and solvent on the reaction rates* *J. Am. Chem. Soc.*; **1984**; 106(10); 3047-3049.



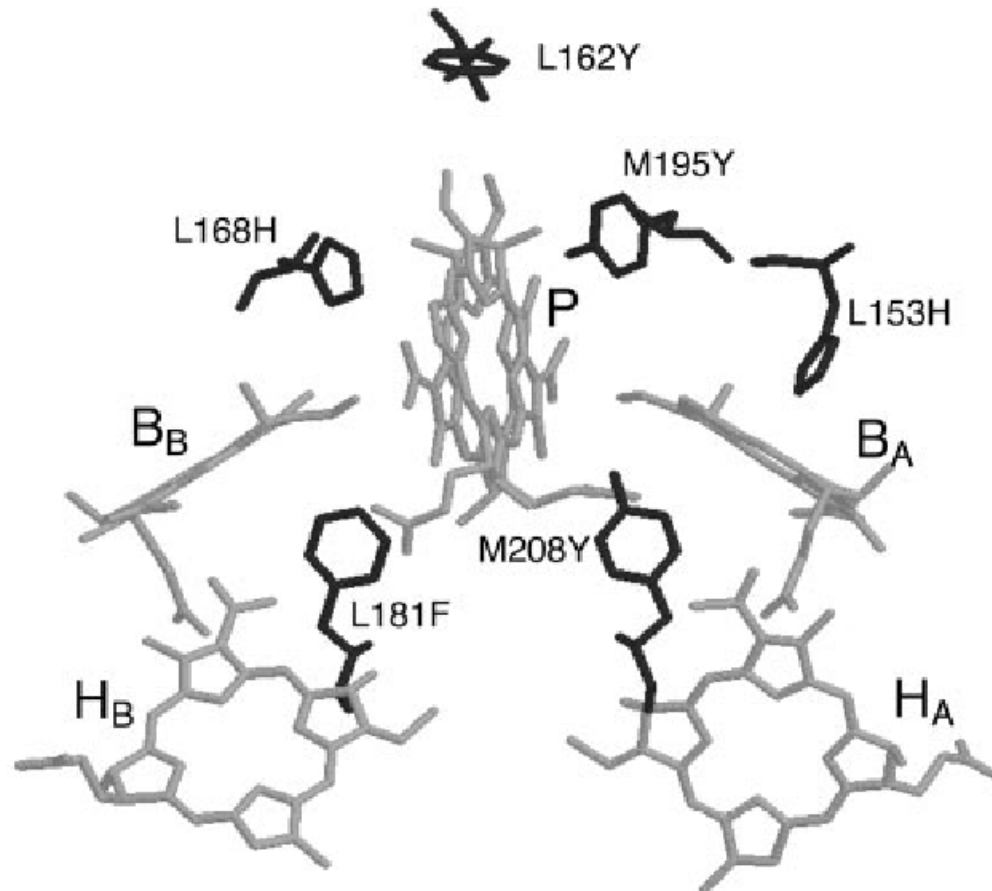
# Photochemical Reactions in Nature: Electron Transfer in Photosynthesis

## Der primäre Elektronentransfer im Reaktionszentrum





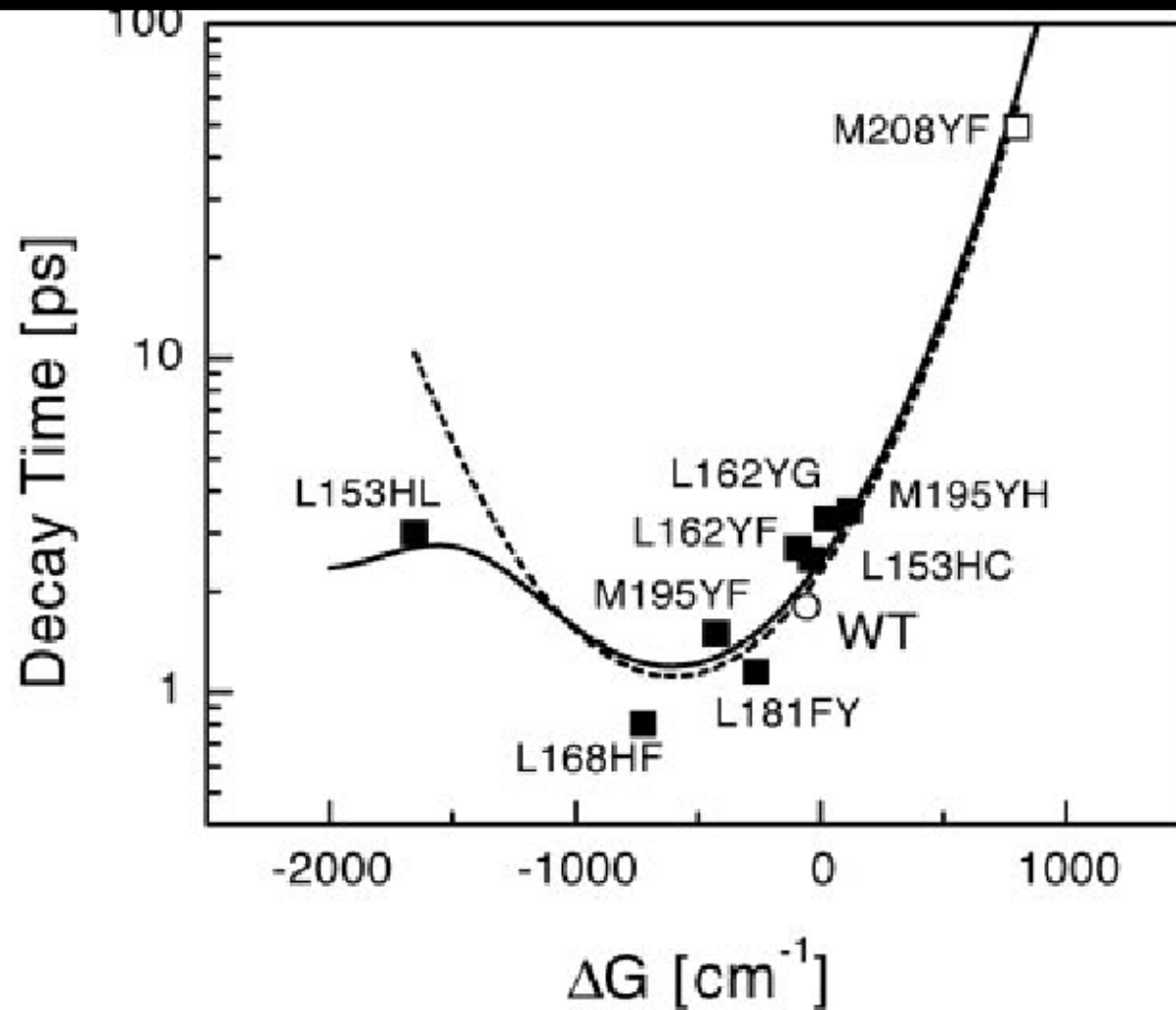
# Marcus Parabola



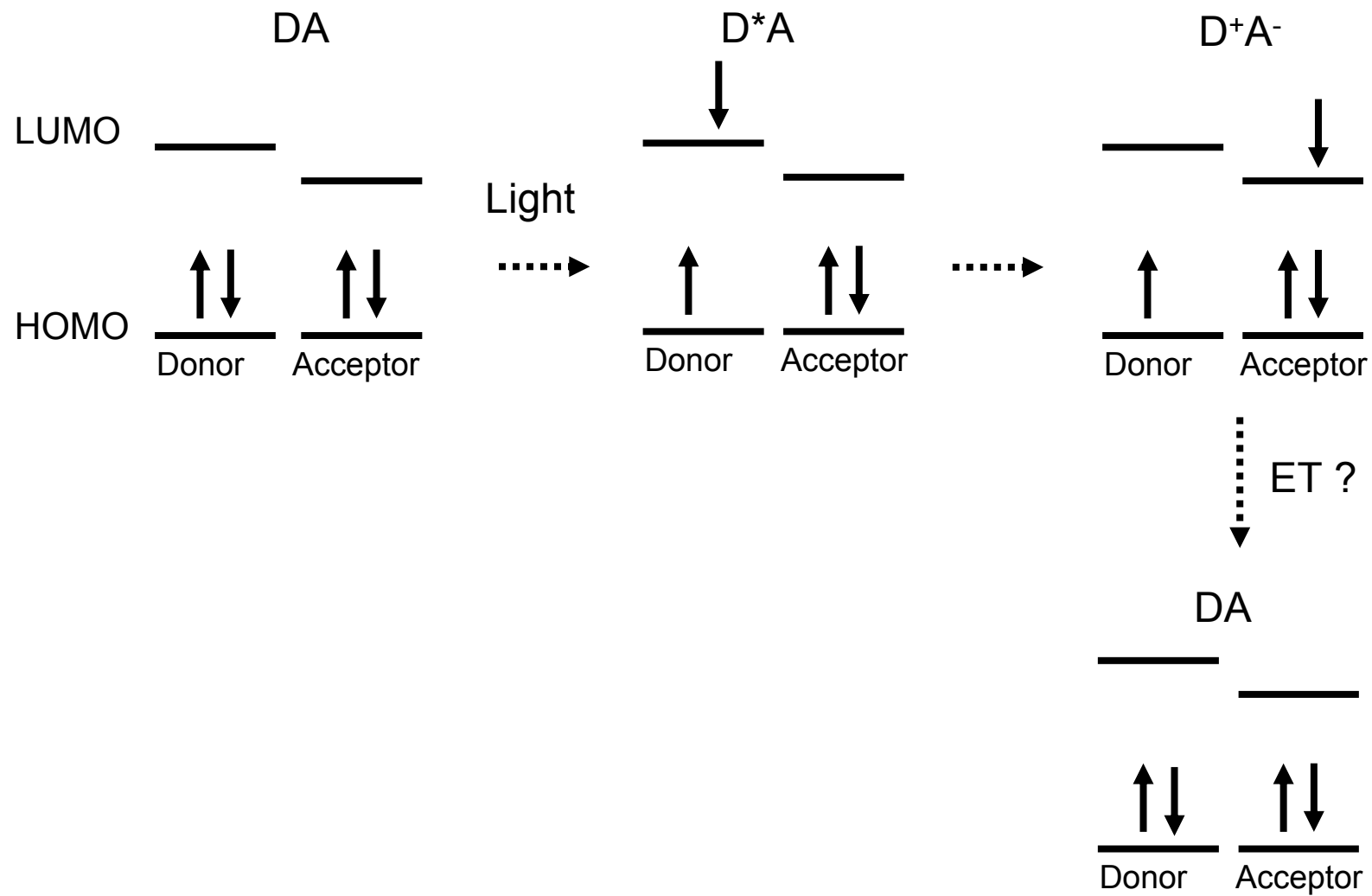
P. Huppman,\* T. Arlt,\* H. Penzkofer,\* S. Schmidt,\* M. Bibikova, B. Dohse, D. Oesterhelt, J. Wachtveit,\* and W. Zinth\* *Kinetics, Energetics, and Electronic Coupling of the Primary Electron Transfer Reactions in Mutated Reaction Centers of Blastochloris viridis* Biophys J, 2002, 3186-82



# Marcus Parabola

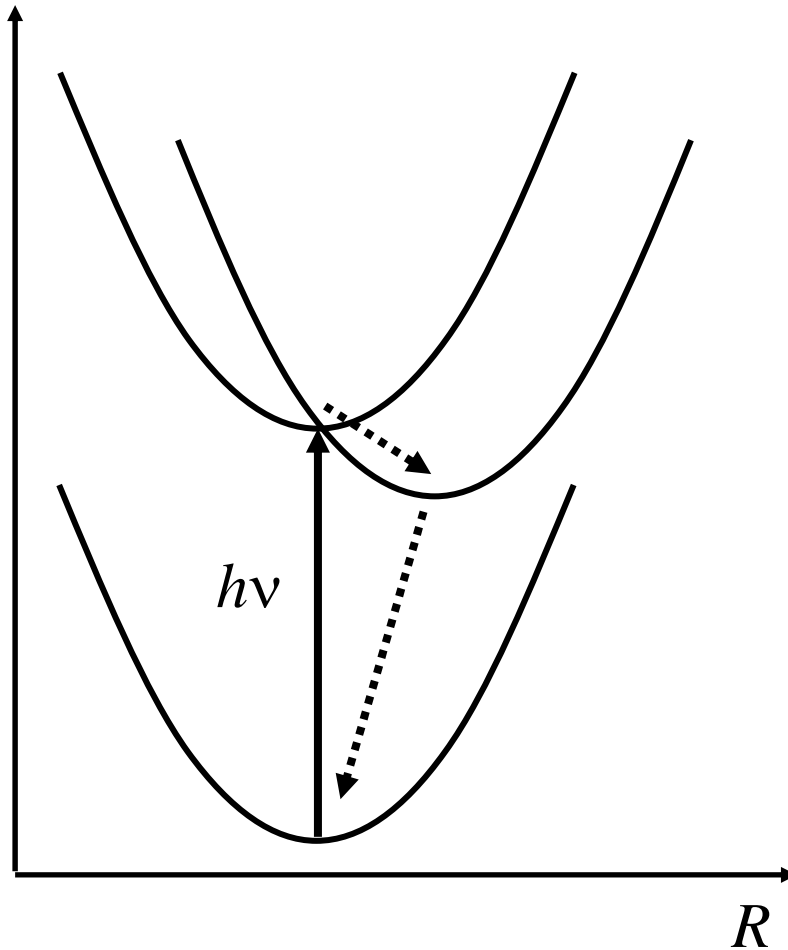


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# Supressing Back Electron Transfer

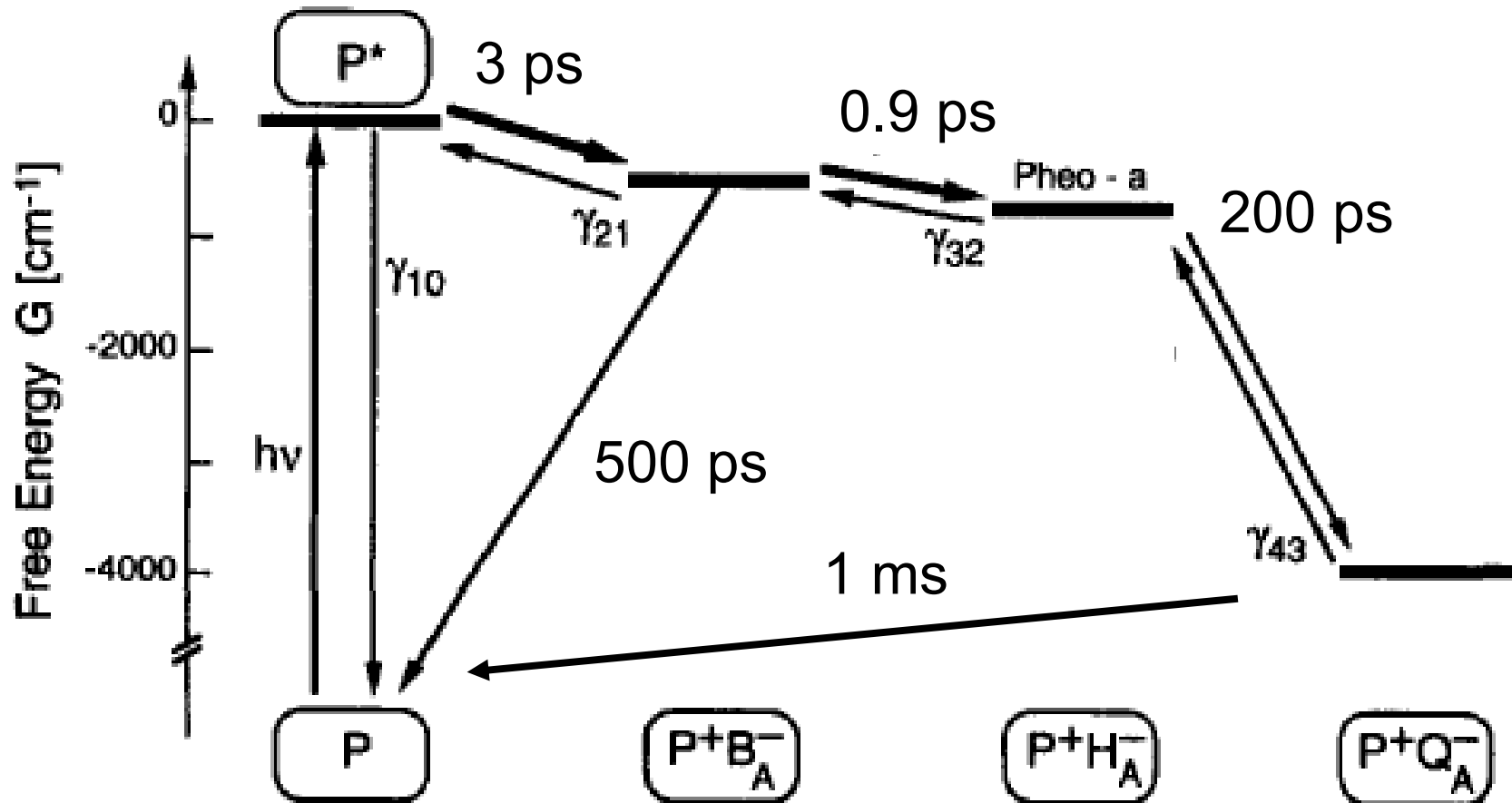


Forward ET:  $\Delta F = F_\lambda$  and small  
 $\Rightarrow$  barrier less

Backward ET:  $\Delta F \gg F_\lambda$  and large  
 $\Rightarrow$  strongly in the inverted regime



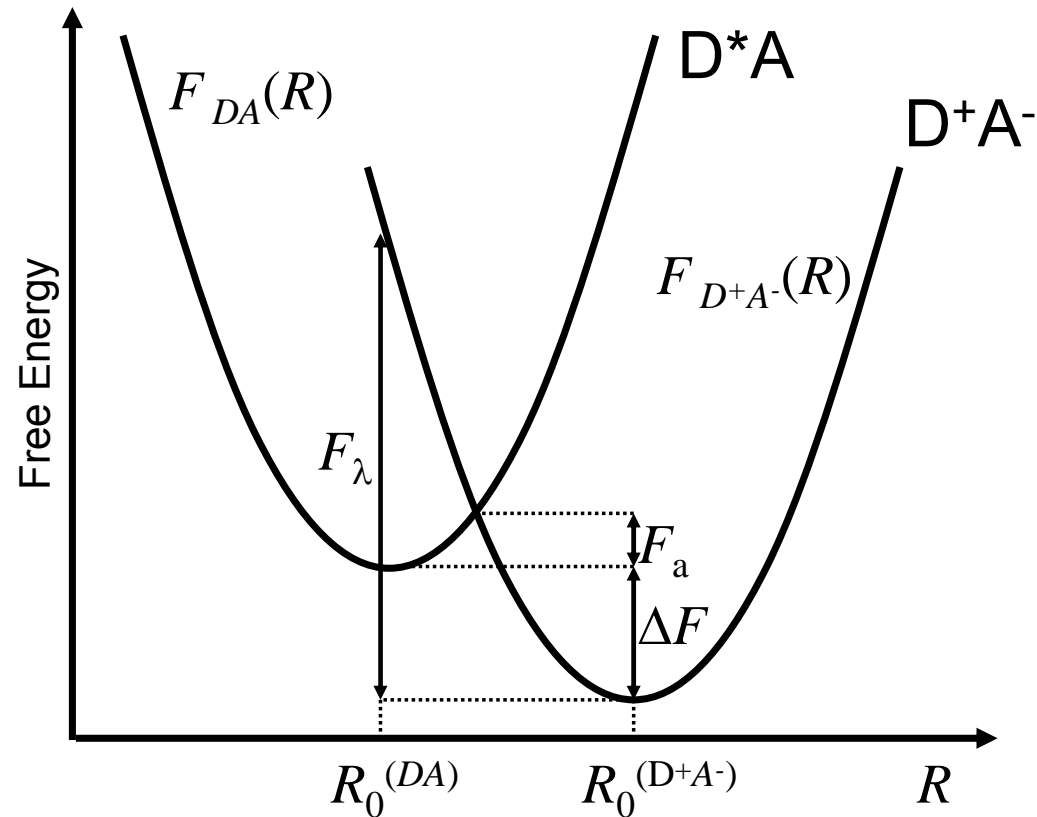
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Zinth et al. Spectrochimica Acta Part A 51 (1995) 1565-1578 and  
Feher et al. J. Phys. Chem. 1994,98, 3417-3423



# Marcus Theory of Electron Transfer

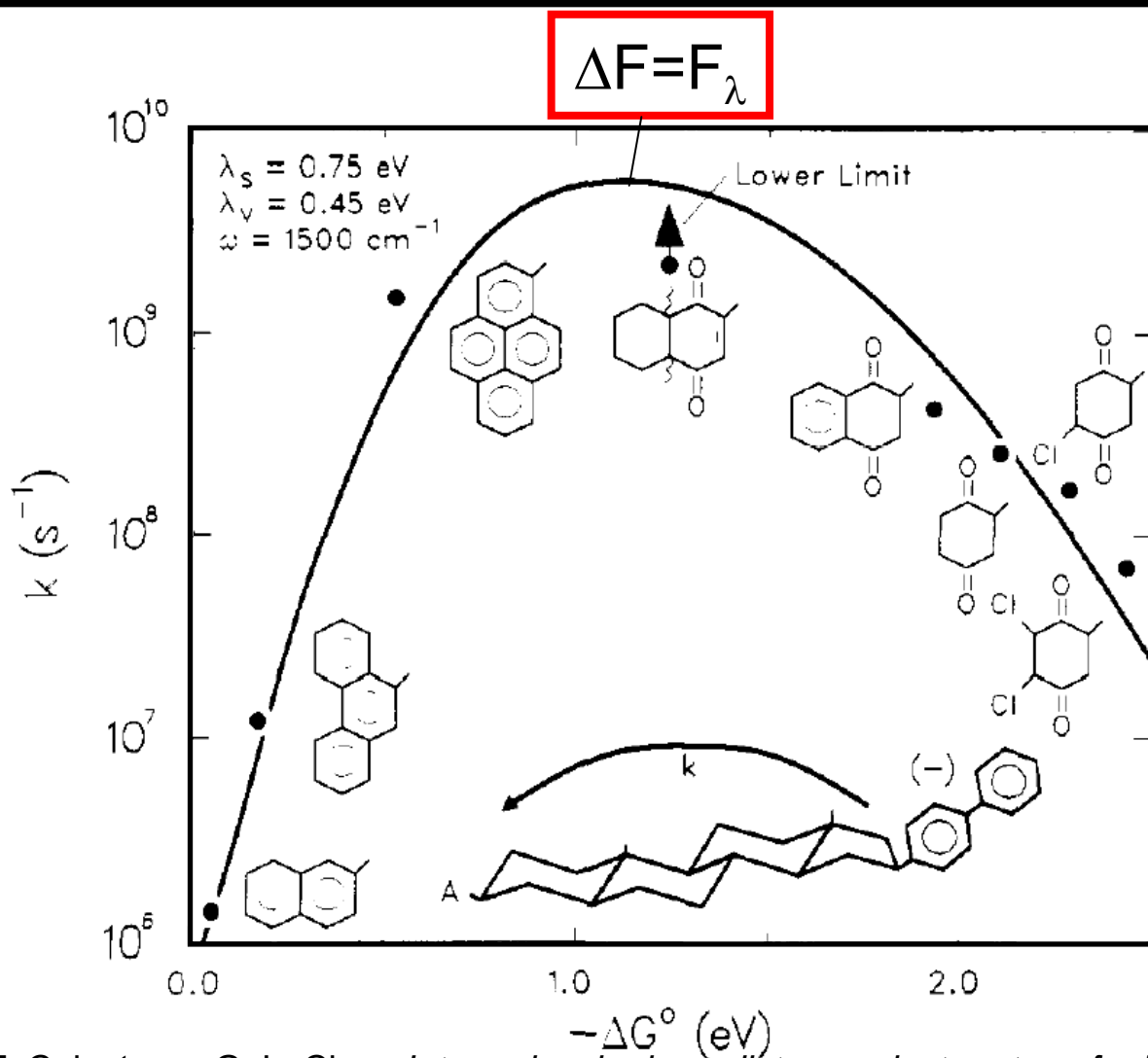


$$k_{ET} = V_{DA}^2 \sqrt{\frac{\pi}{\hbar^2 k_B T F_\lambda}} \exp\left(-\frac{(\Delta F - F_\lambda)^2}{4F_\lambda k_B T}\right)$$





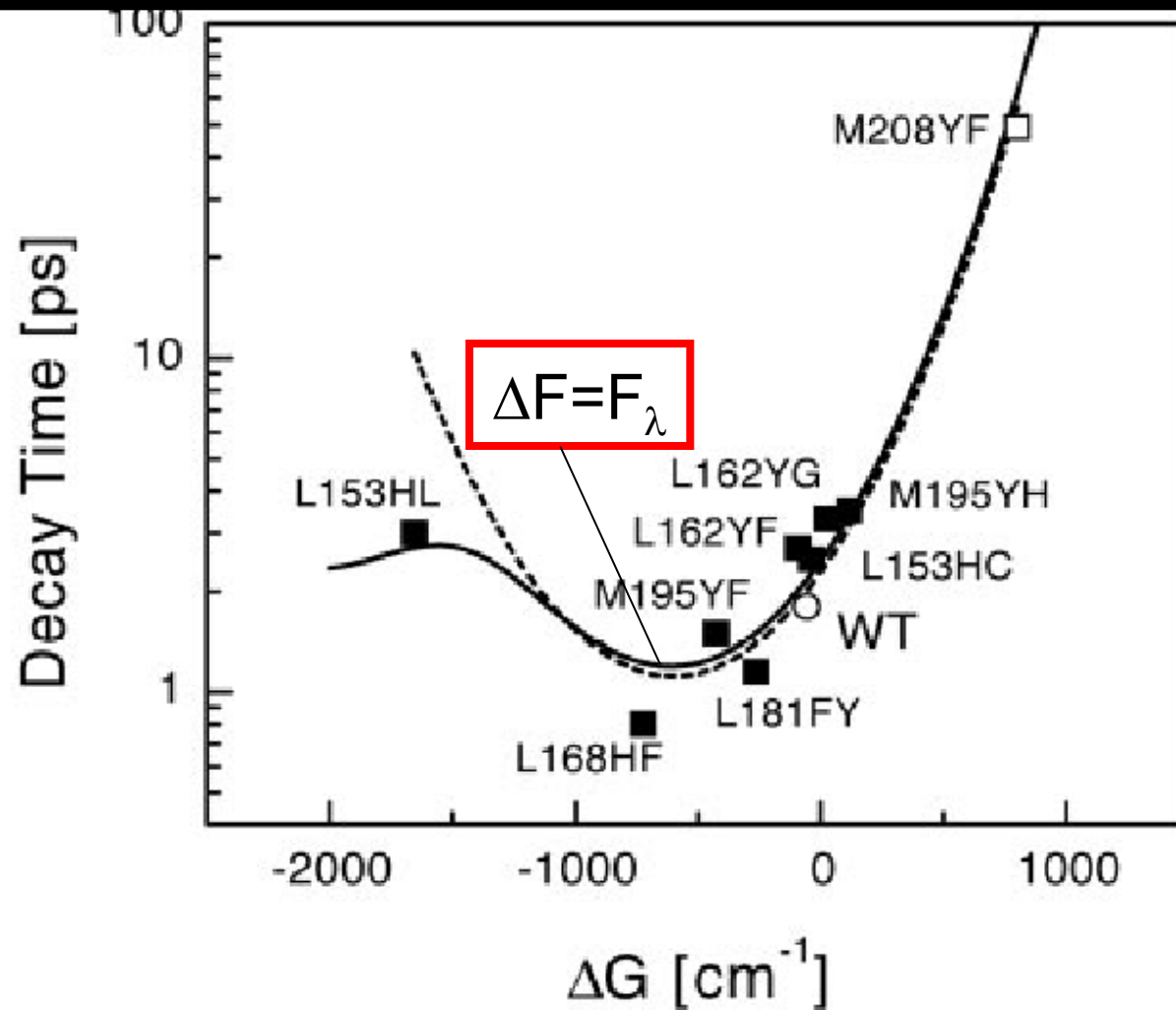
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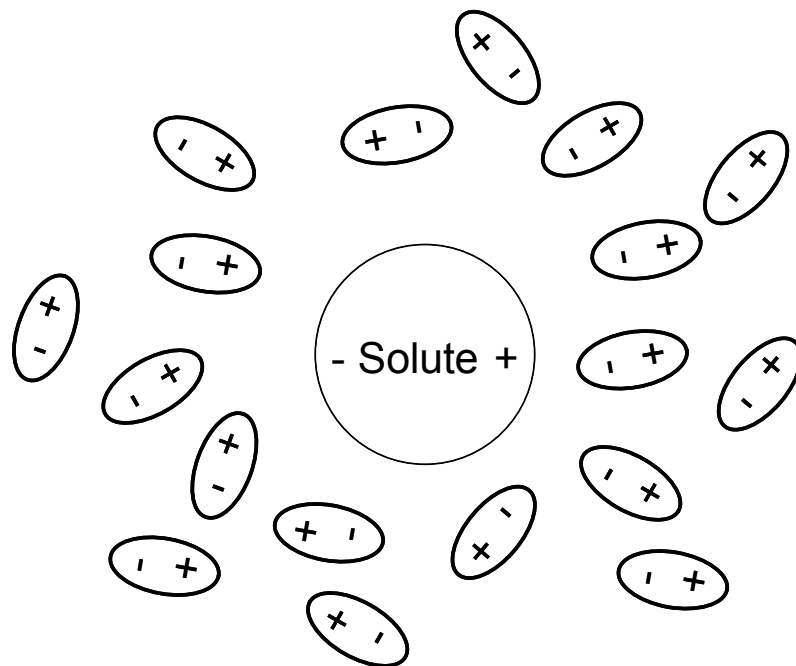


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# Solvation Energy

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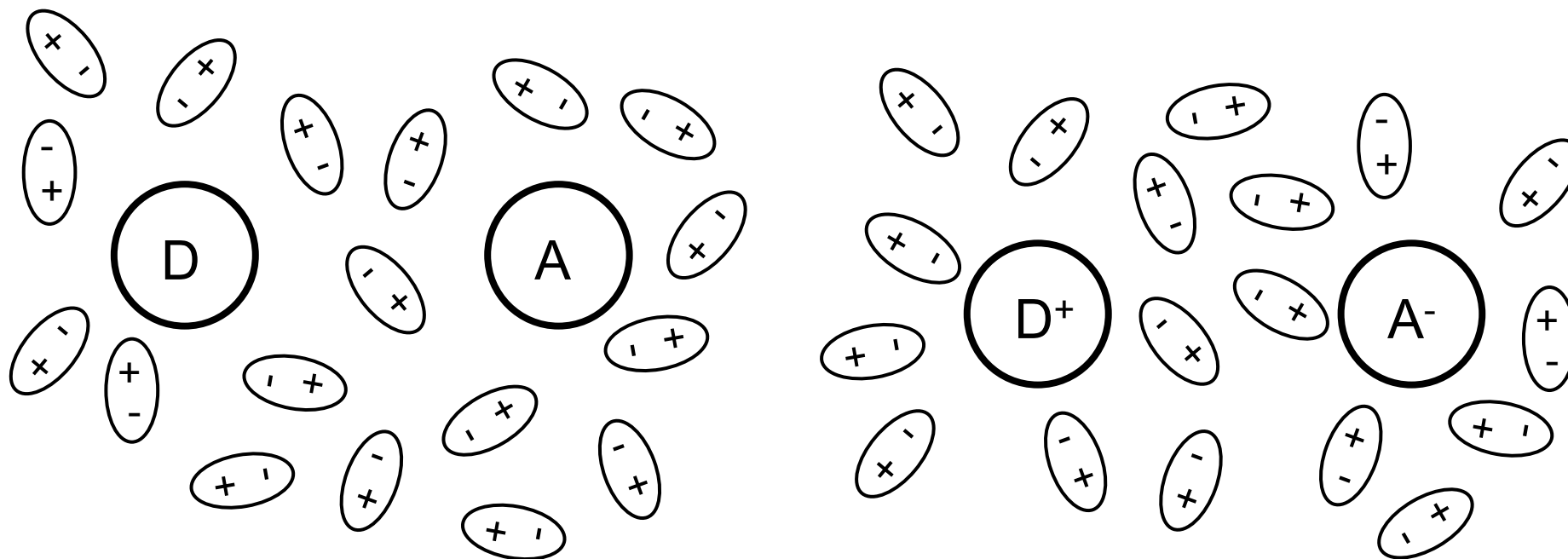


$$\Delta E = \frac{(\epsilon - 1)}{(2\epsilon + 1)r^3} \mu^2$$

Onsager's Reaction Field Model



# Solvation of a Charge Transfer Complex

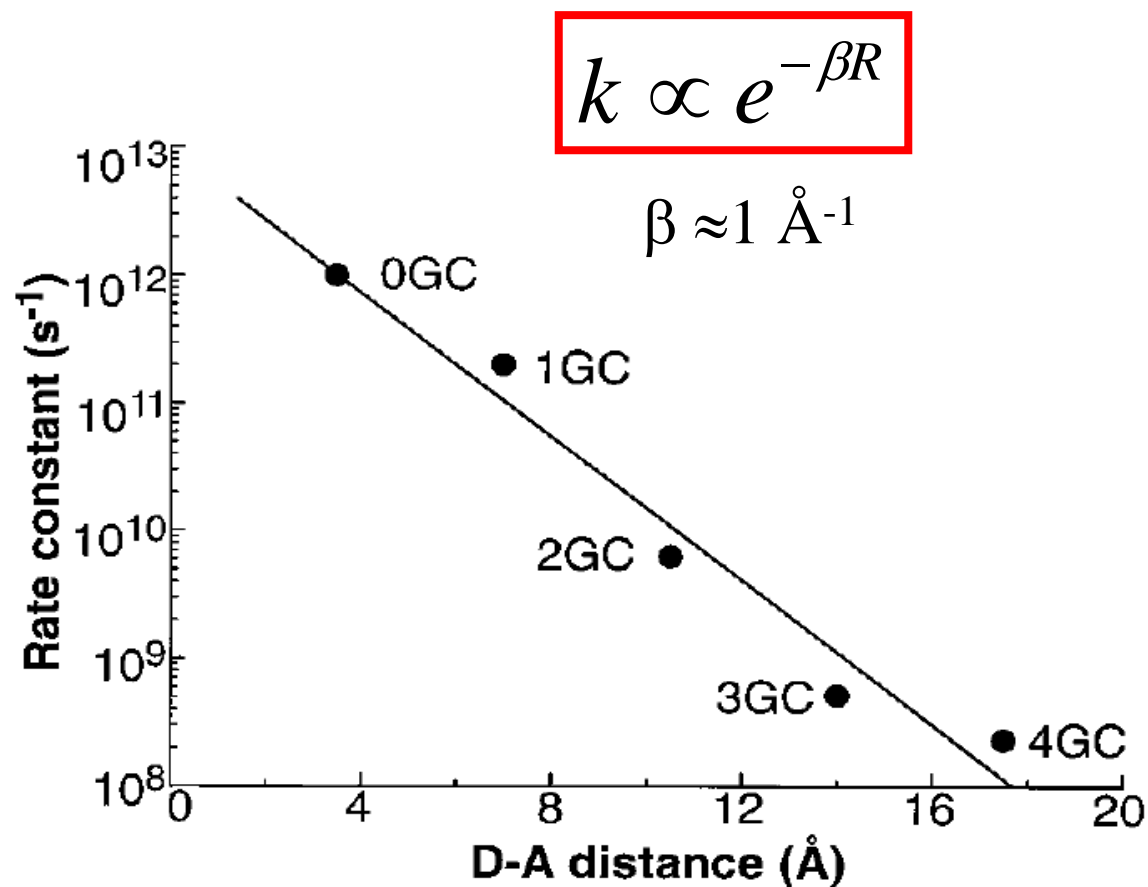
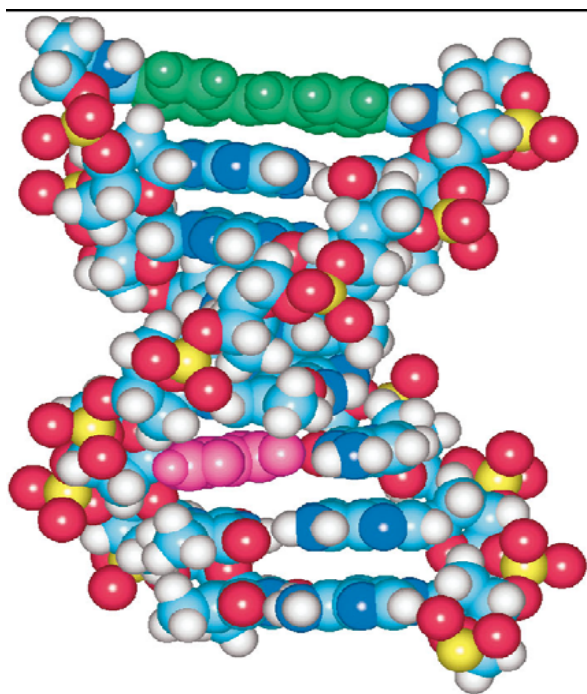


$$E_{\lambda} = \frac{1}{8\pi} \left( \frac{1}{\epsilon_{\infty}} - \frac{1}{\epsilon_r} \right) \left( \frac{e^2}{2R_D} + \frac{e^2}{2R_A} - \frac{e^2}{r_{DA}} \right)$$

in analogy to Onsager's Reaction Field Model



# Distance Dependence of Electron Transfer



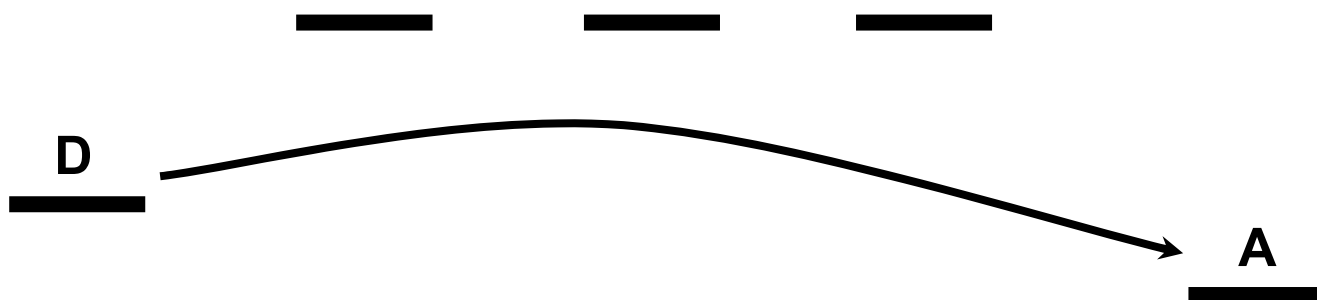
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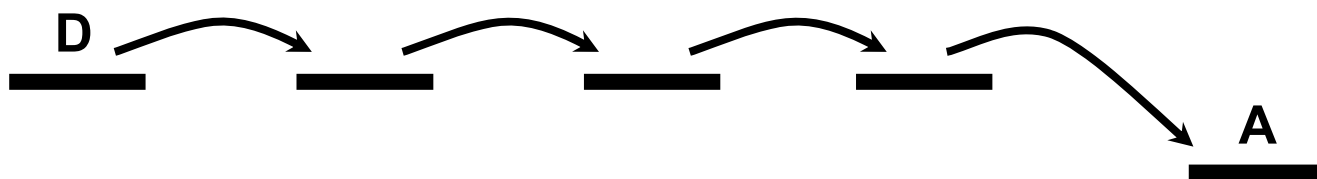
# Bridged Electron Transfer

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Superexchange

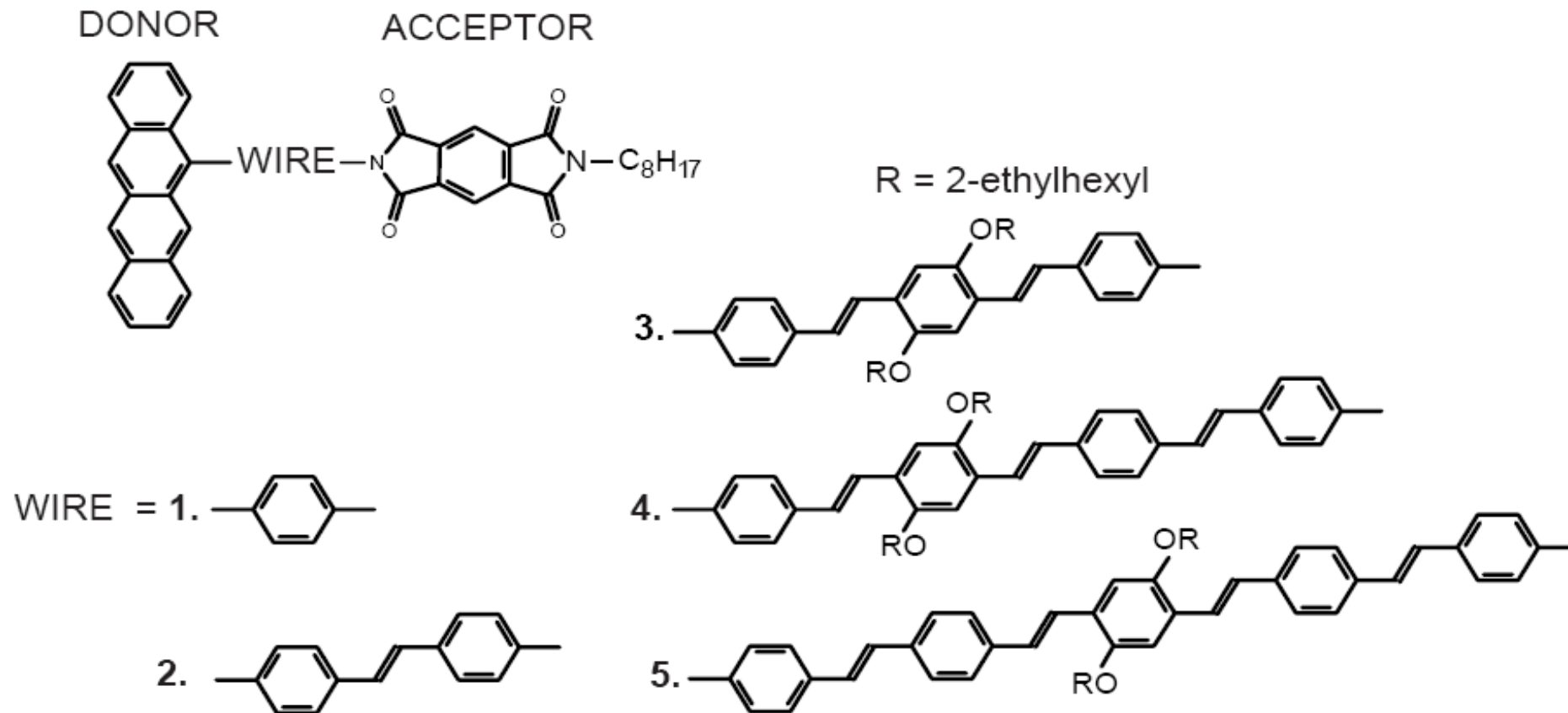


Hopping





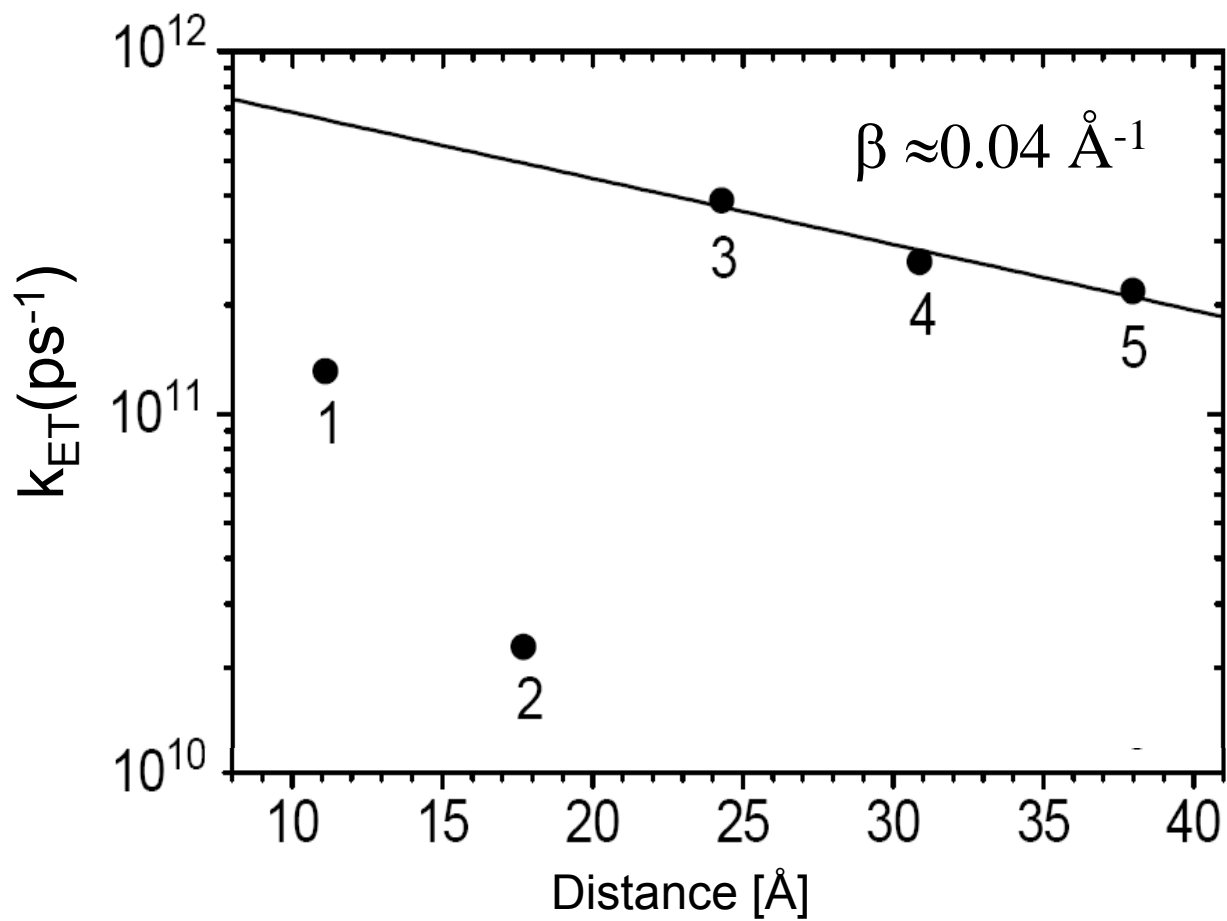
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W. B. Davis, W. A. Svec, M. A. Ratner, M. R., Nature 396, 60 - 63 (1998)



# Bridged Electron Transfer

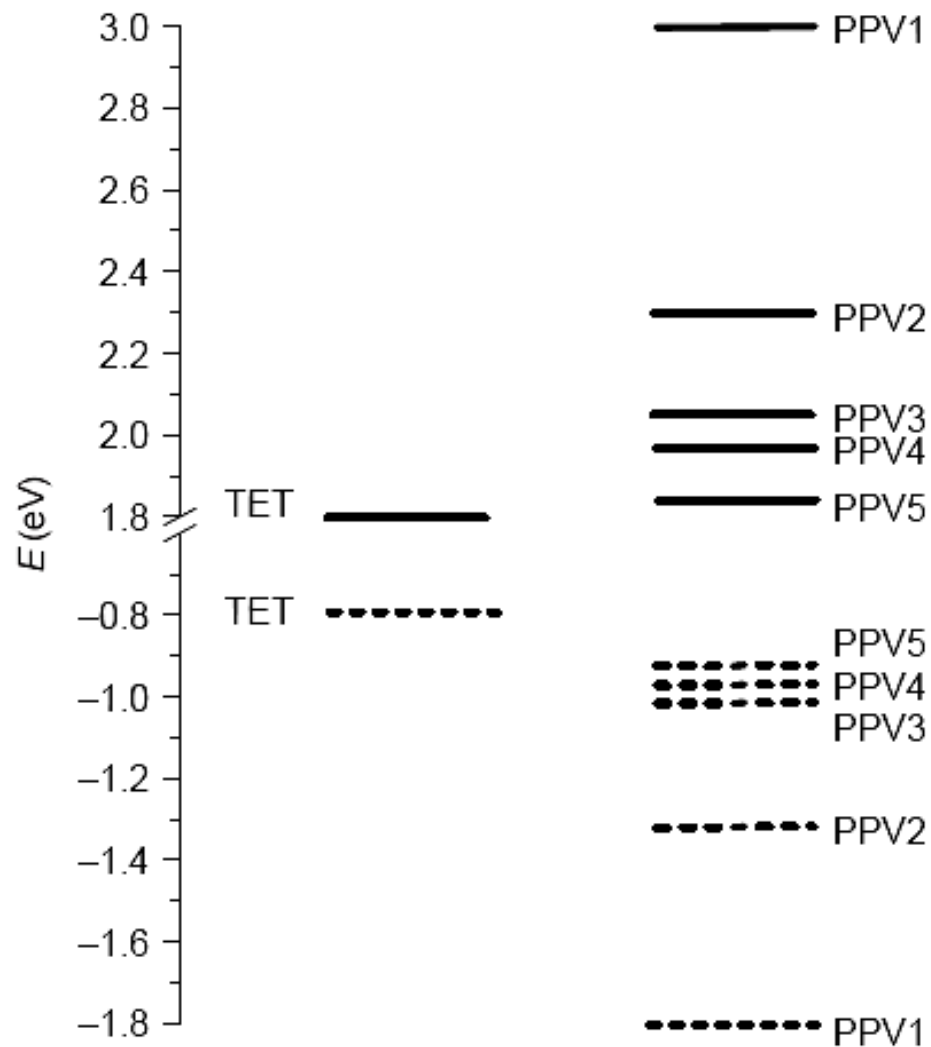


W. B. Davis, W. A. Svec, M. A. Ratner, M. R., Nature 396, 60 - 63 (1998)





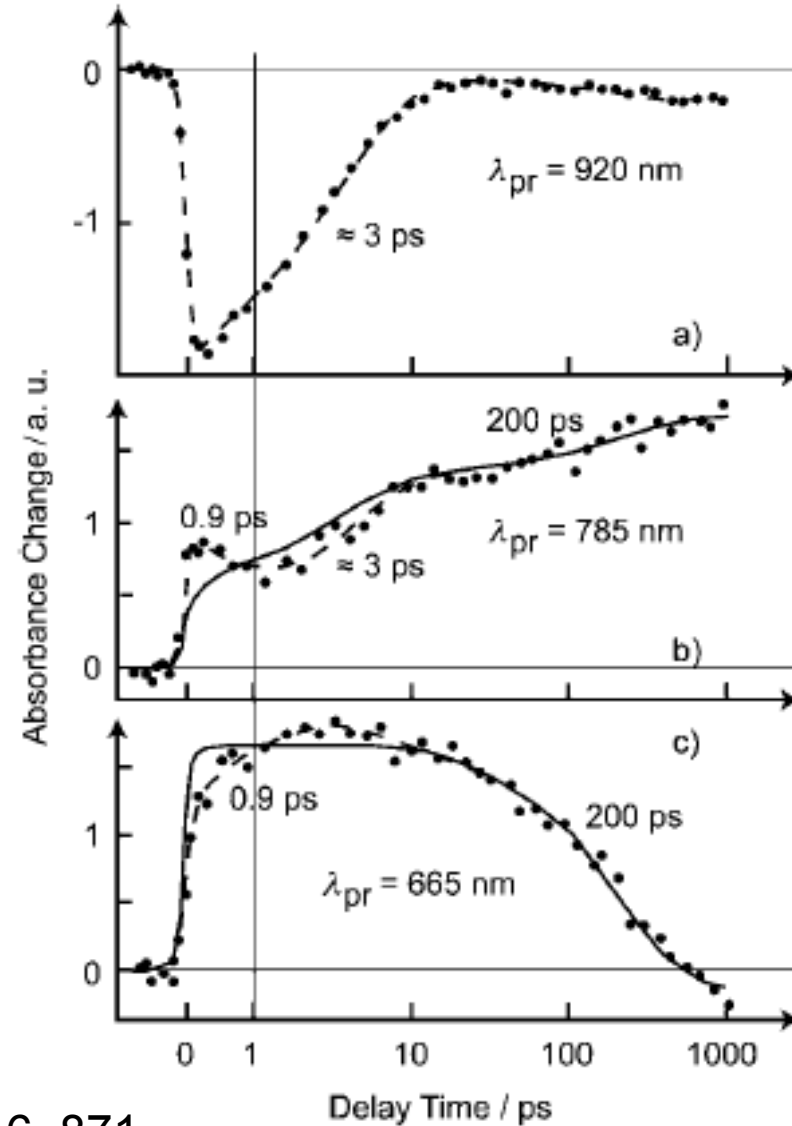
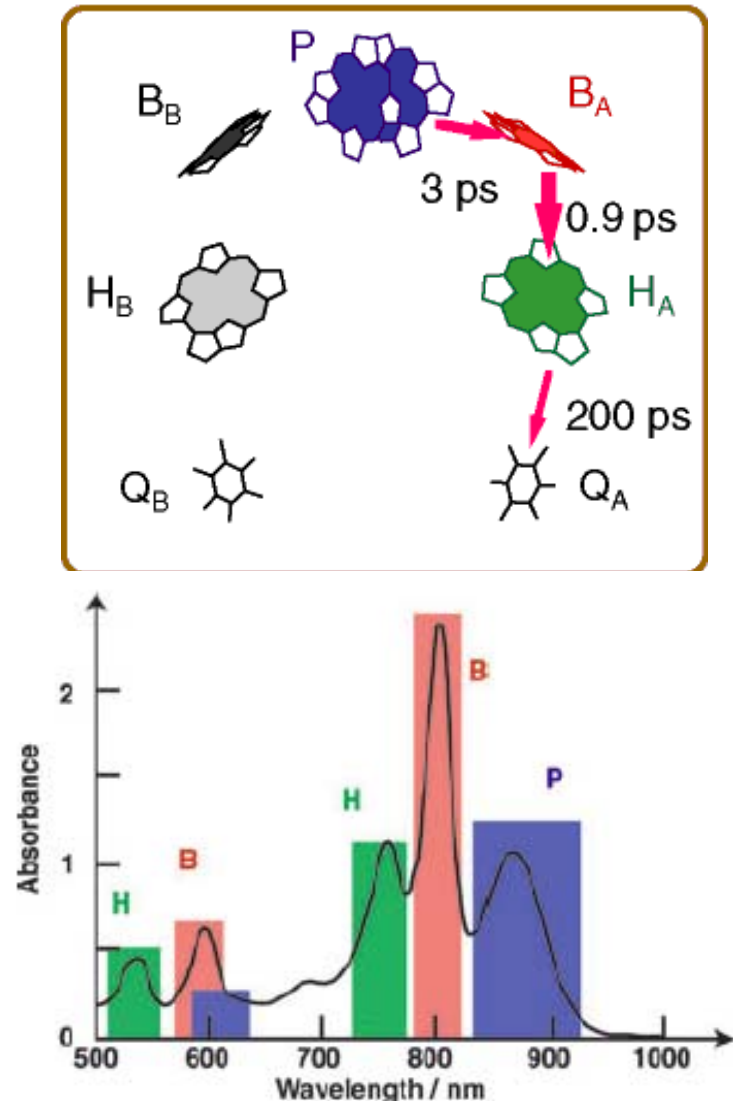
# Bridged Electron Transfer



W. B. Davis, W. A. Svec, M. A. Ratner, M. R., Nature 396, 60 - 63 (1998)



# Superexchange in Reaction Center?





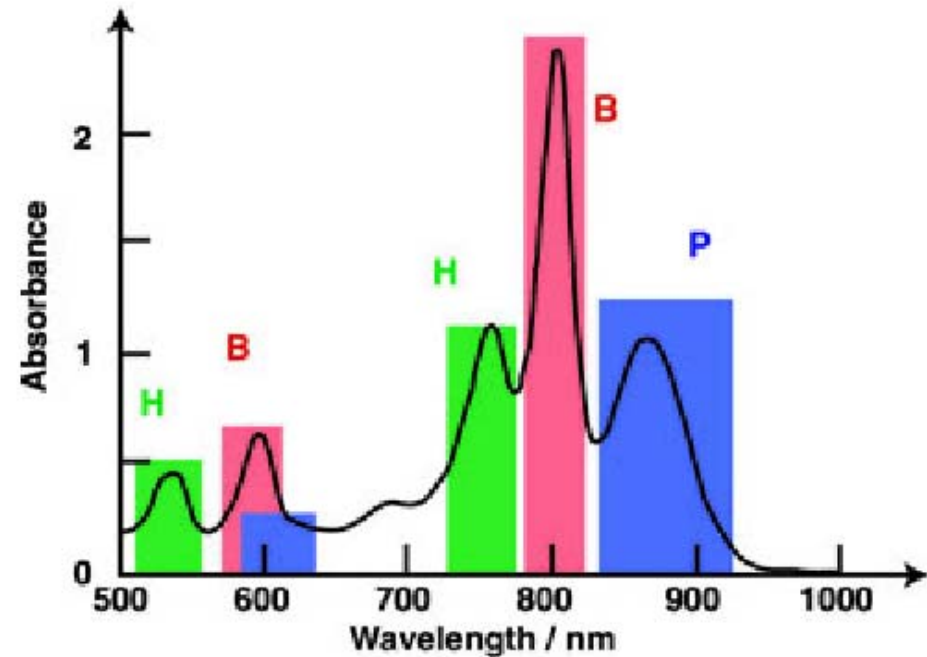
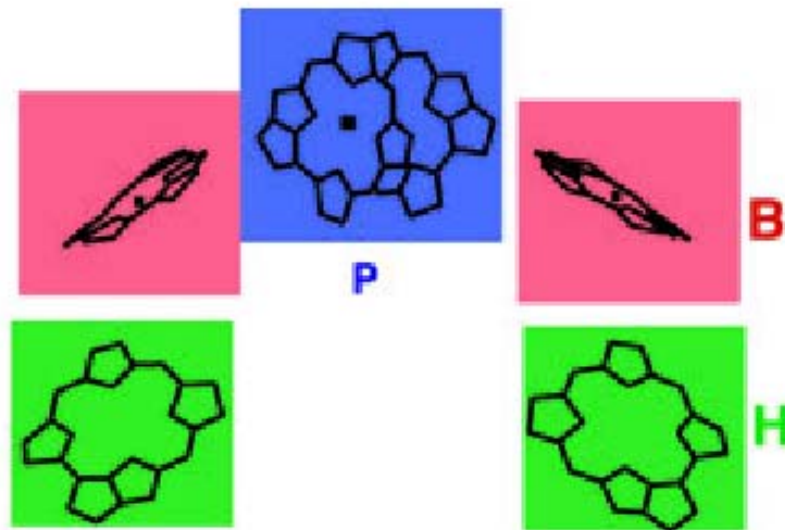
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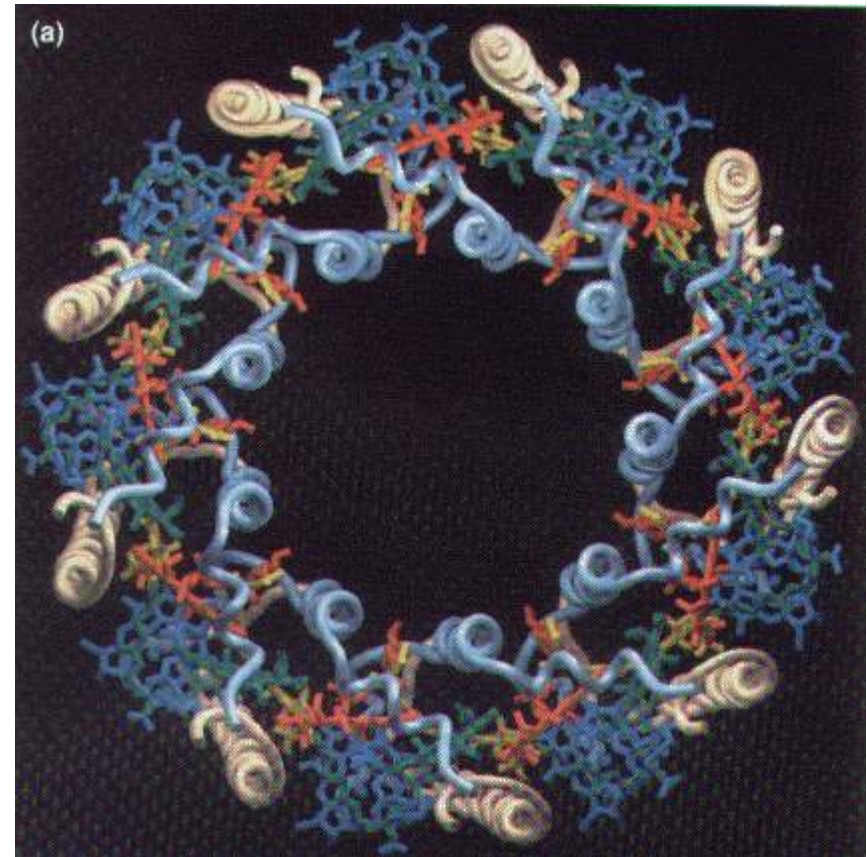
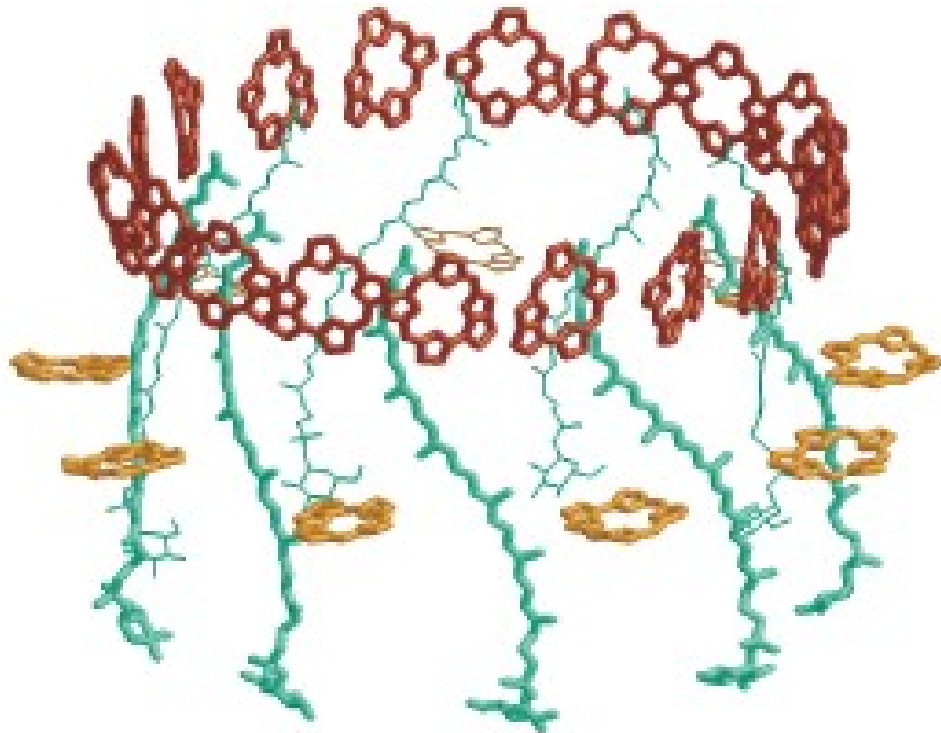


# Special Pair in Reaction Center



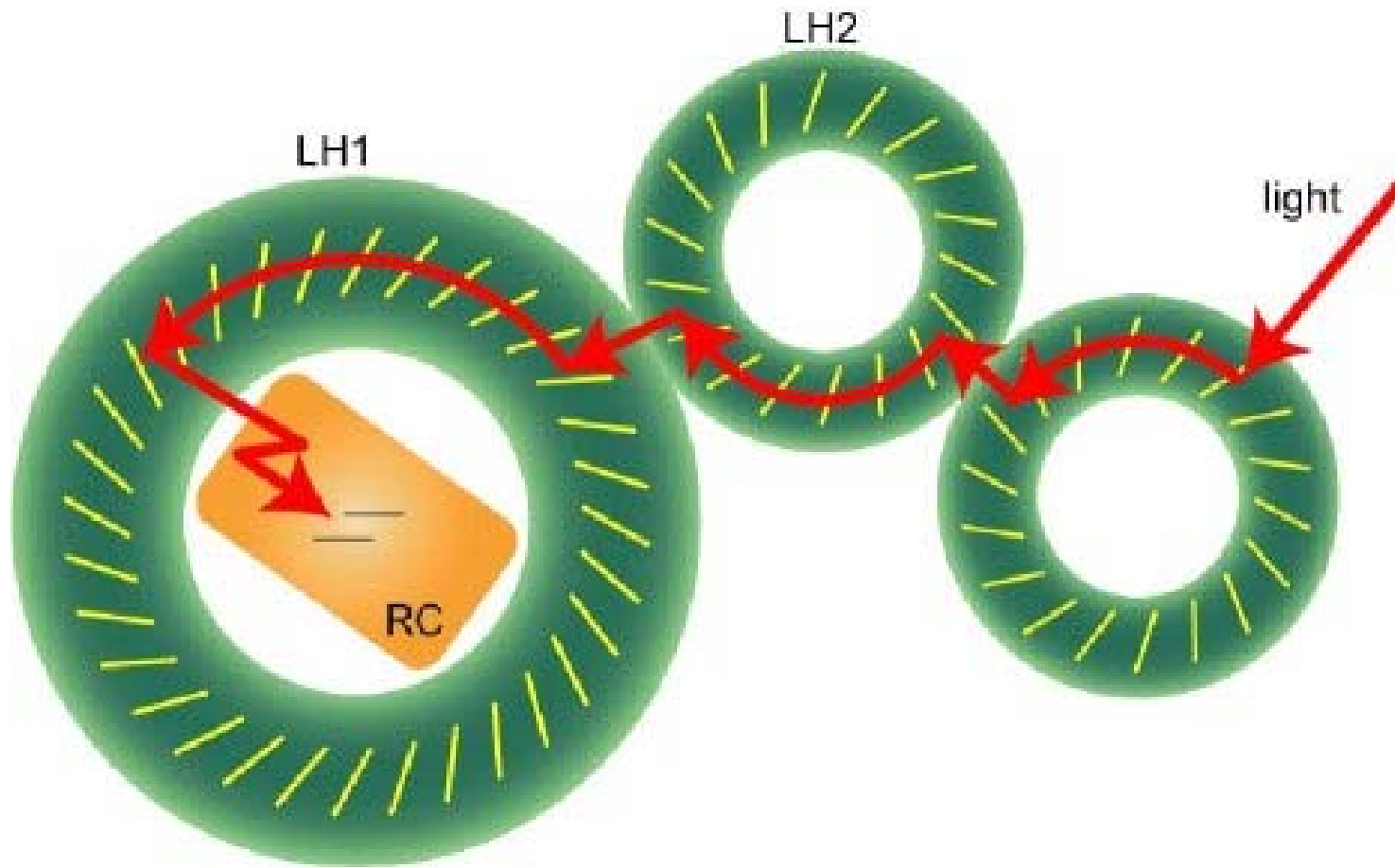


# LH II Antenna Complex



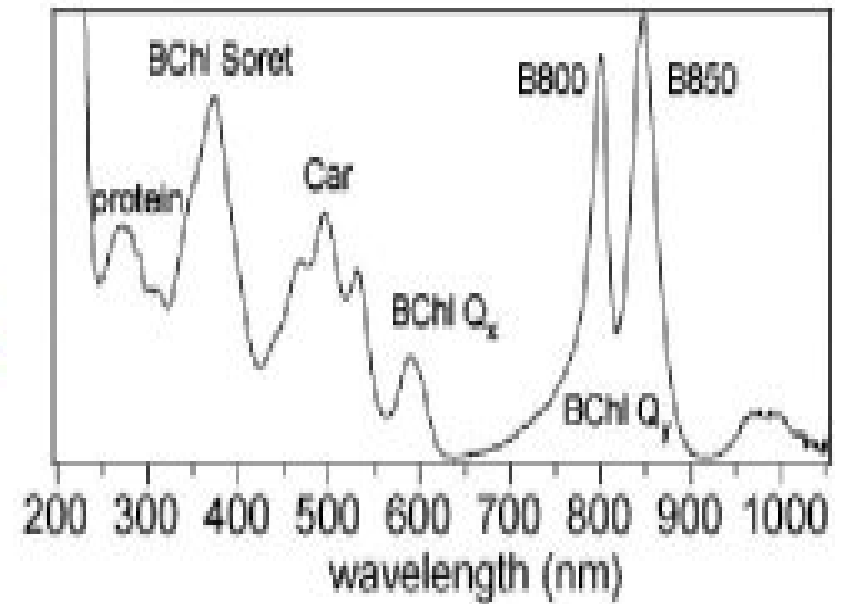
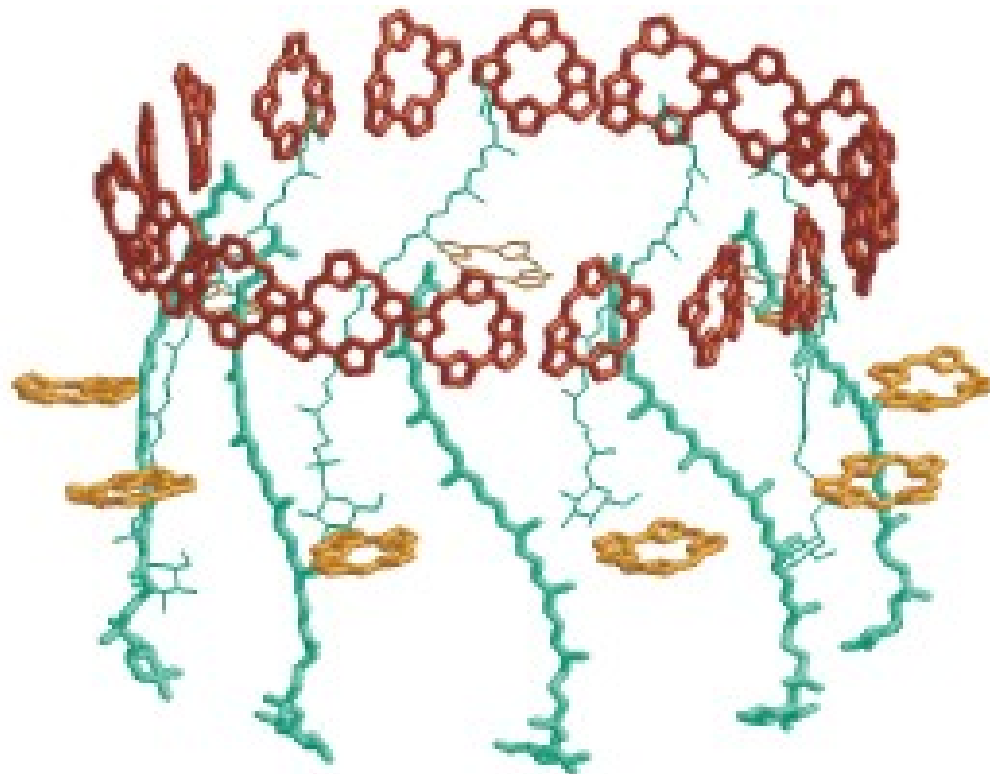


# LH II Antenna Complex



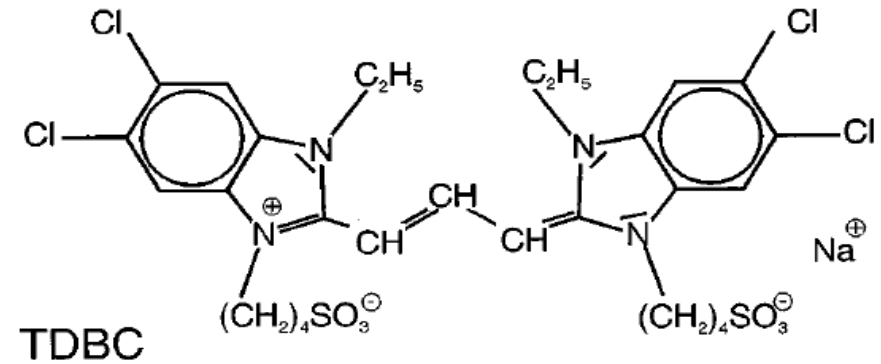
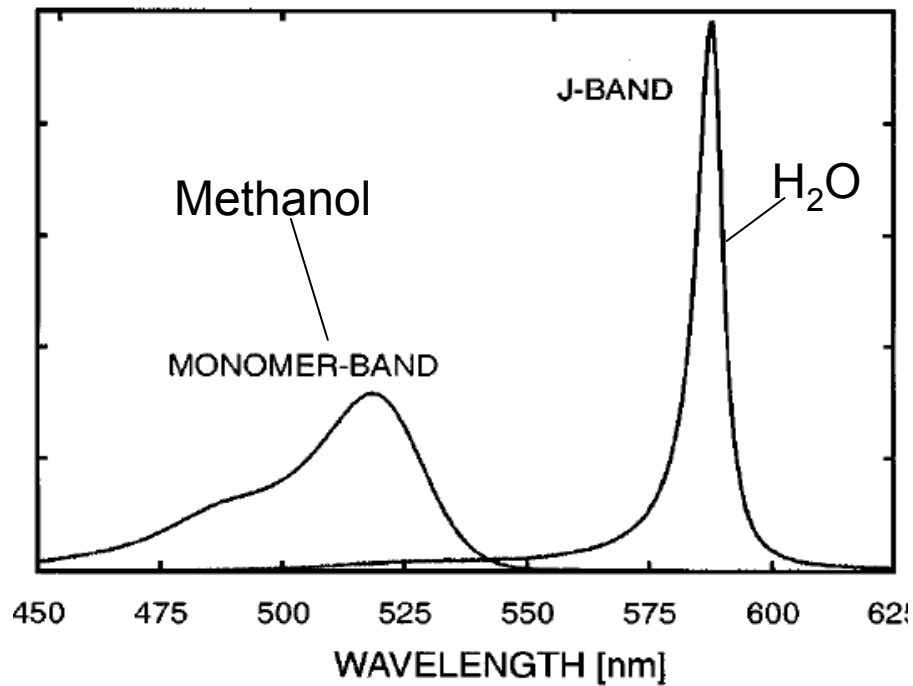


# LH II Antenna Complex





# J-Aggregates

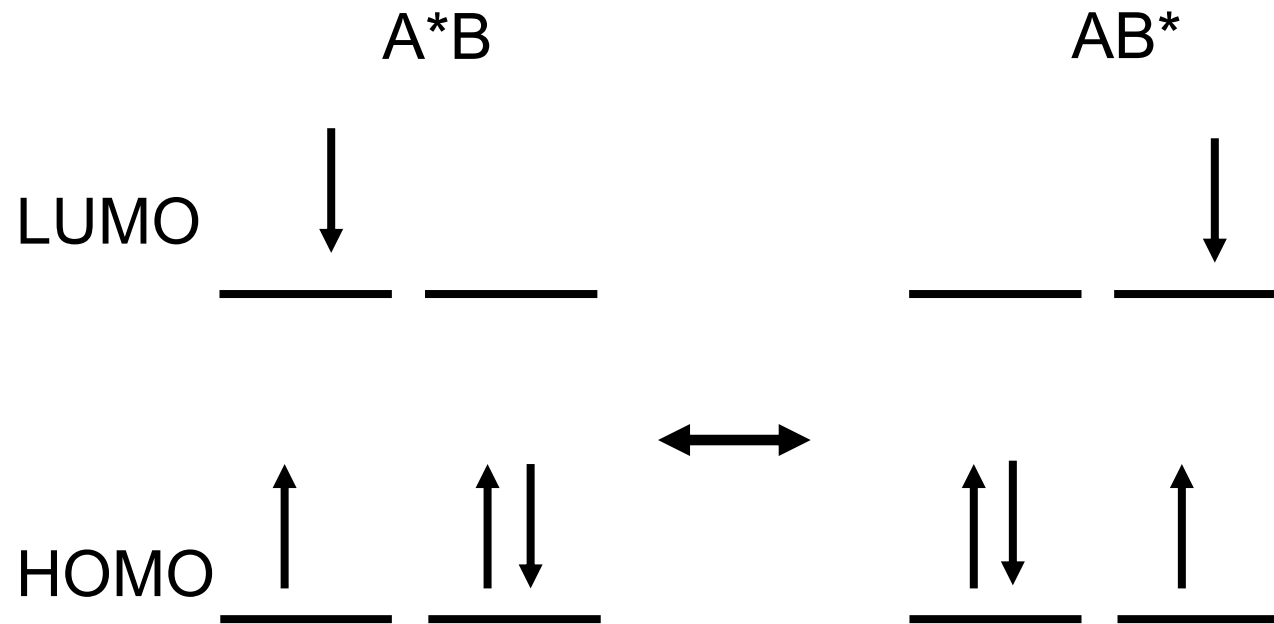


J. Moll, S. Daehne, J. R. Durrant and D. A. Wiersma, *Optical dynamics of excitons in J aggregates of a carbocyanine dye*, JCP 102, (1995) 6362





# Excitation (Exciton) Transfer

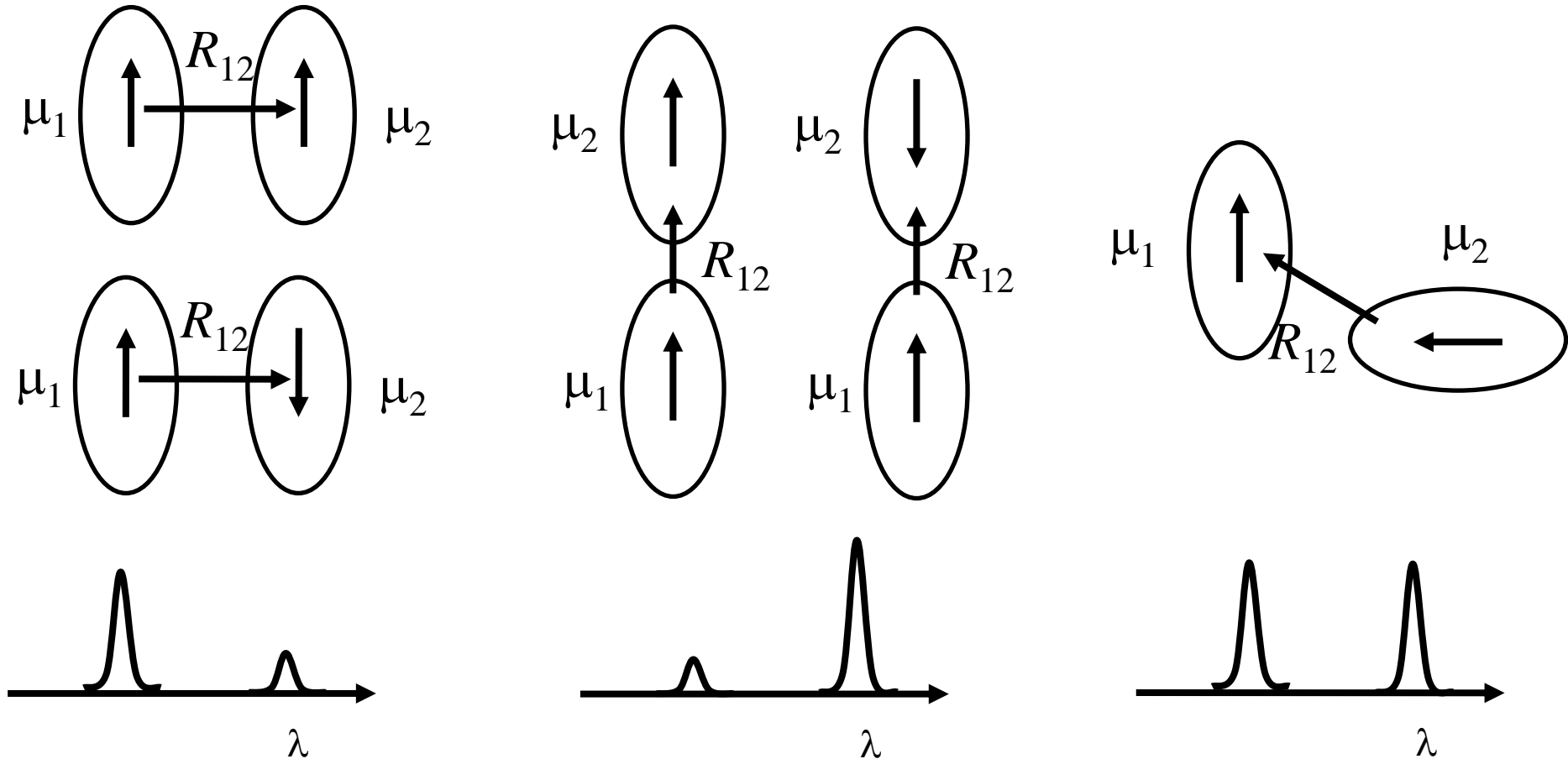


$$H_{ex} = \begin{pmatrix} E_1 & V_{12} \\ V_{12} & E_2 \end{pmatrix} \quad V_{12} \approx \frac{\vec{\mu}_1 \vec{\mu}_2}{R_{12}^3} - 3 \frac{(\vec{\mu}_1 \vec{R}_{12})(\vec{\mu}_2 \vec{R}_{12})}{R_{12}^5}$$



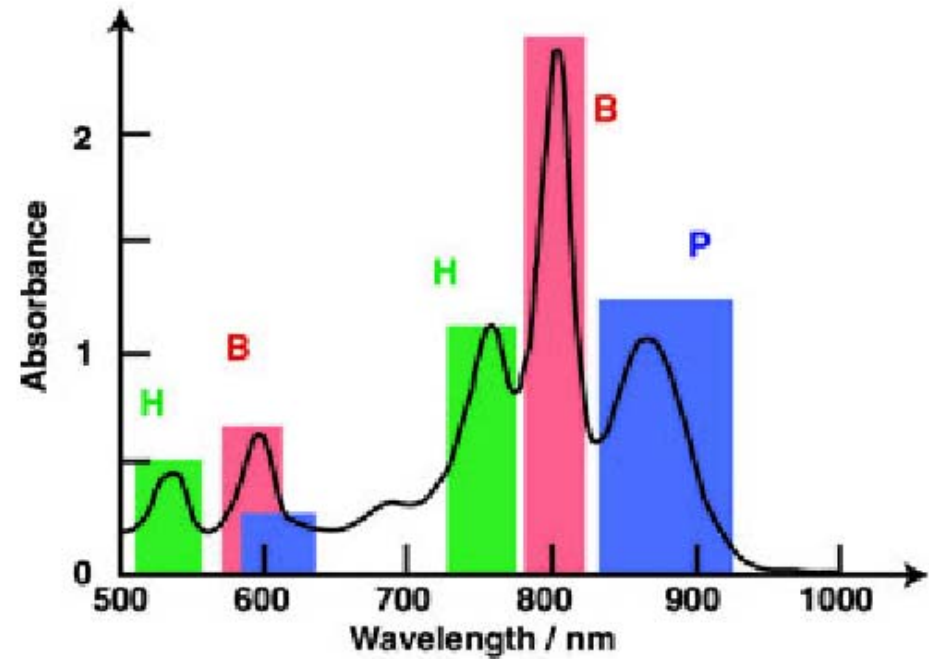
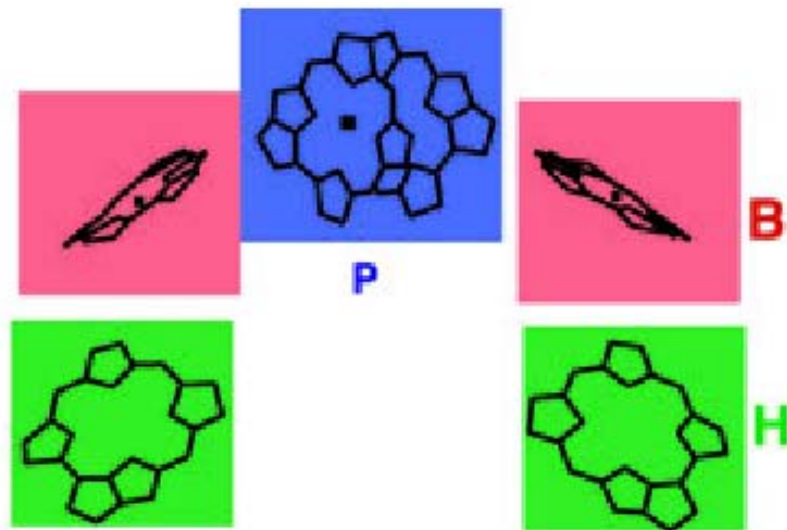
# Excitonic Coupling

$$V_{12} \approx \frac{\vec{\mu}_1 \vec{\mu}_2}{R_{12}^3} - 3 \frac{(\vec{\mu}_1 \vec{R}_{12})(\vec{\mu}_2 \vec{R}_{12})}{R_{12}^5}$$



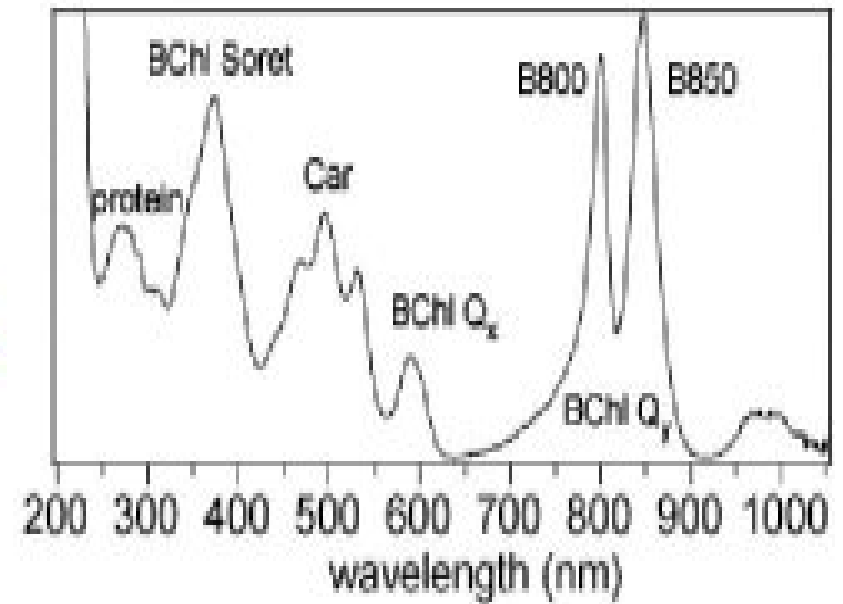
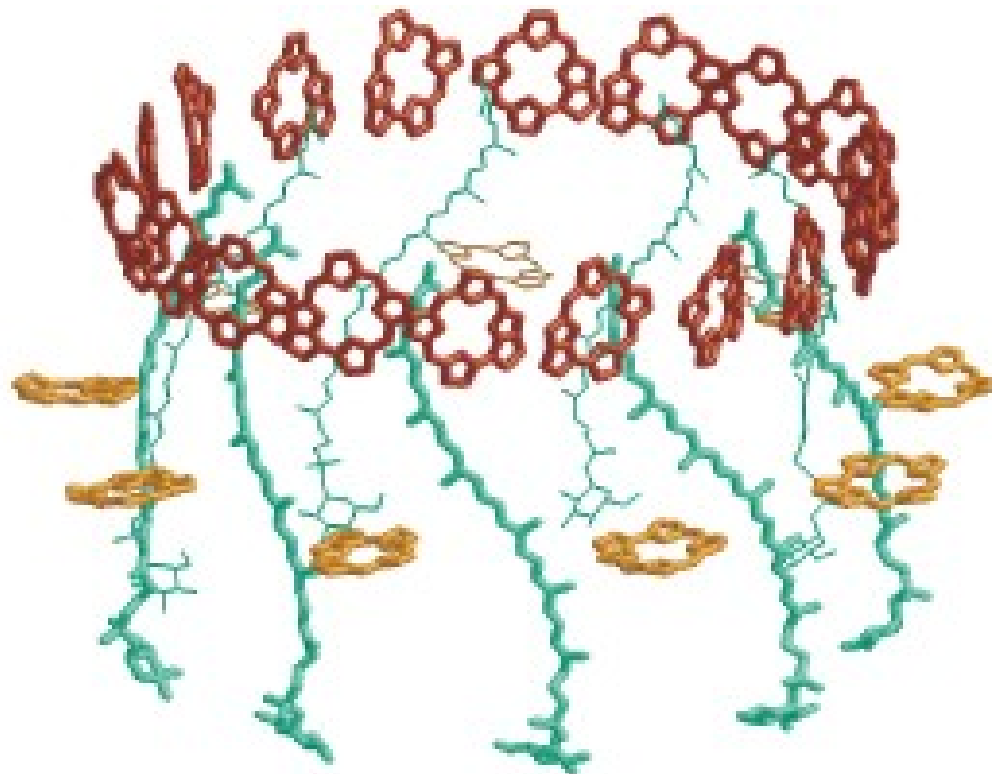


# Photosynthesis





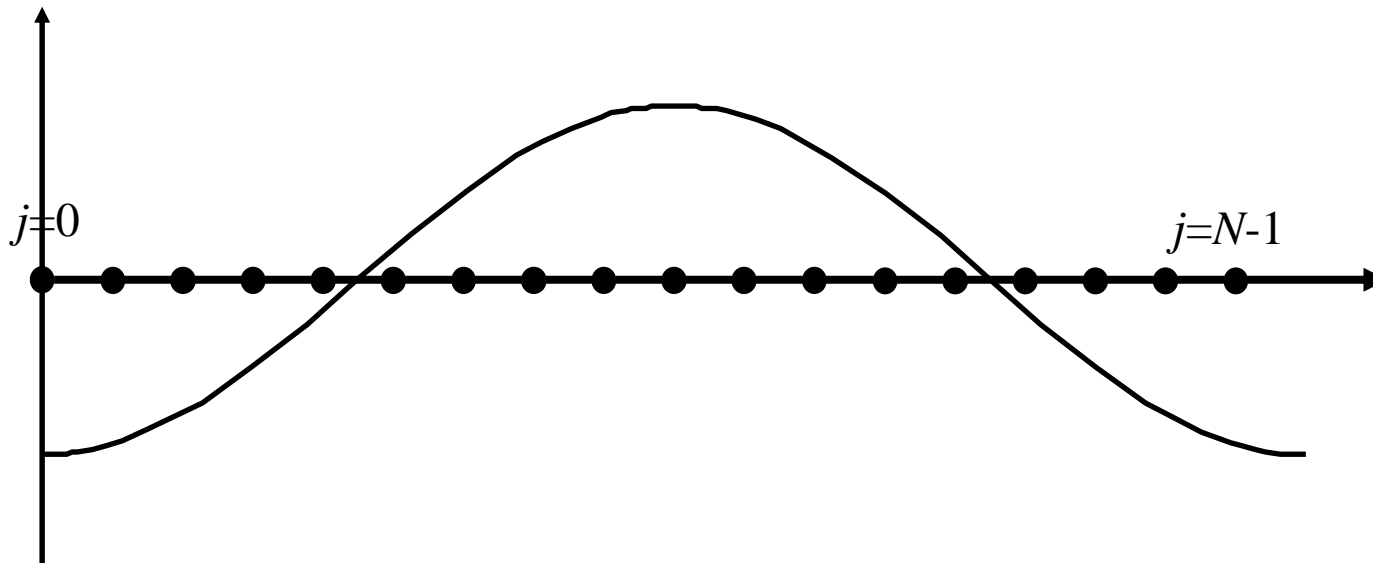
# LH II Antenna Complex





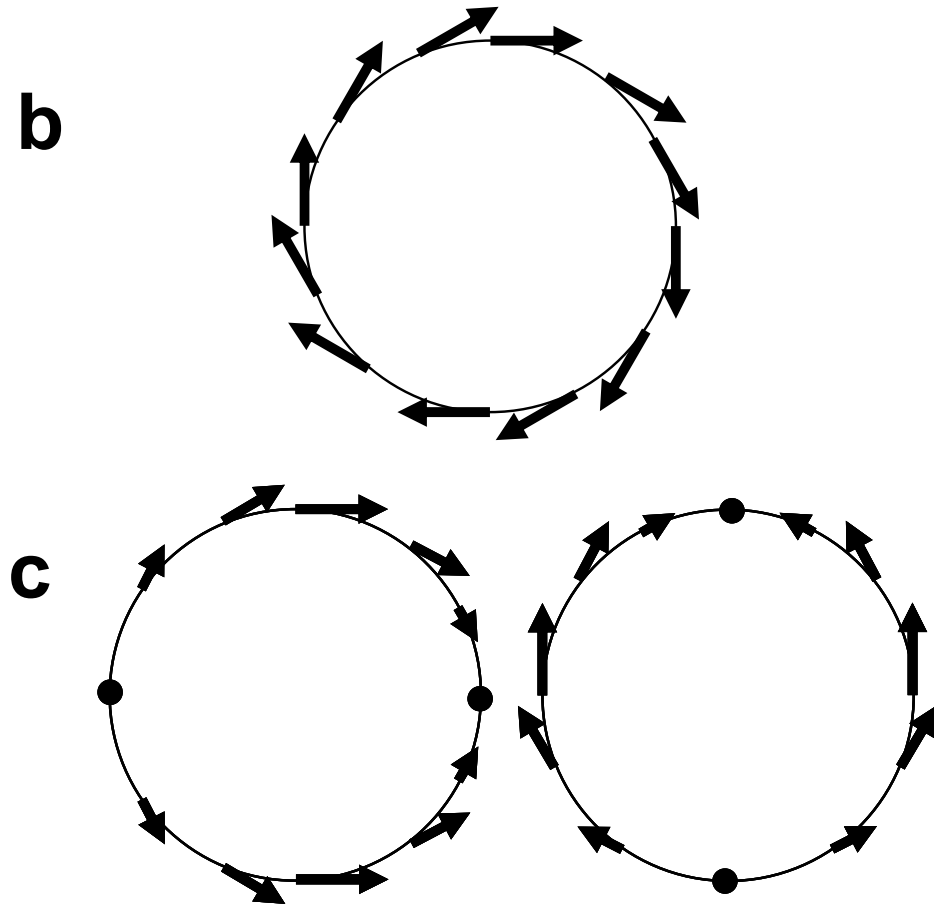
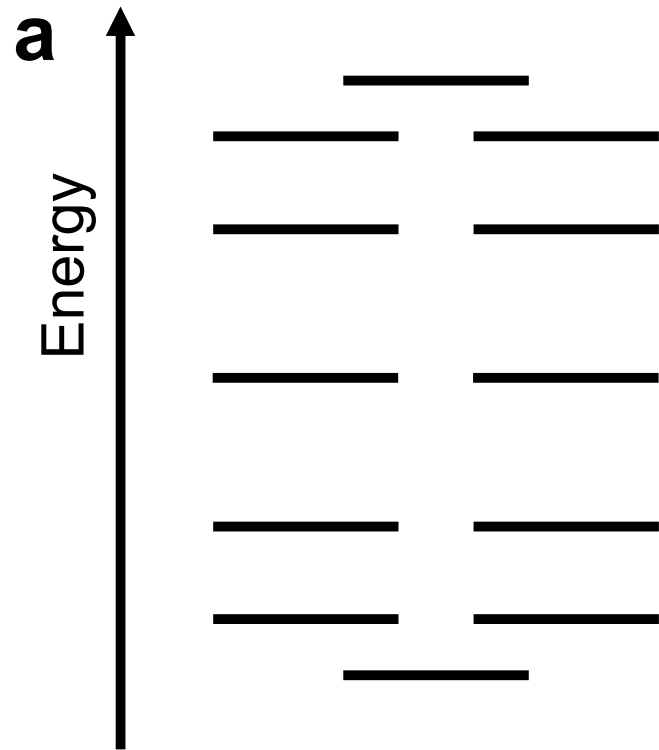
# Excitons in a Ring

$$\varepsilon_\alpha = \varepsilon_0 + 2J \cos \alpha = \varepsilon_0 + 2J \cos \frac{2\pi j}{N}$$





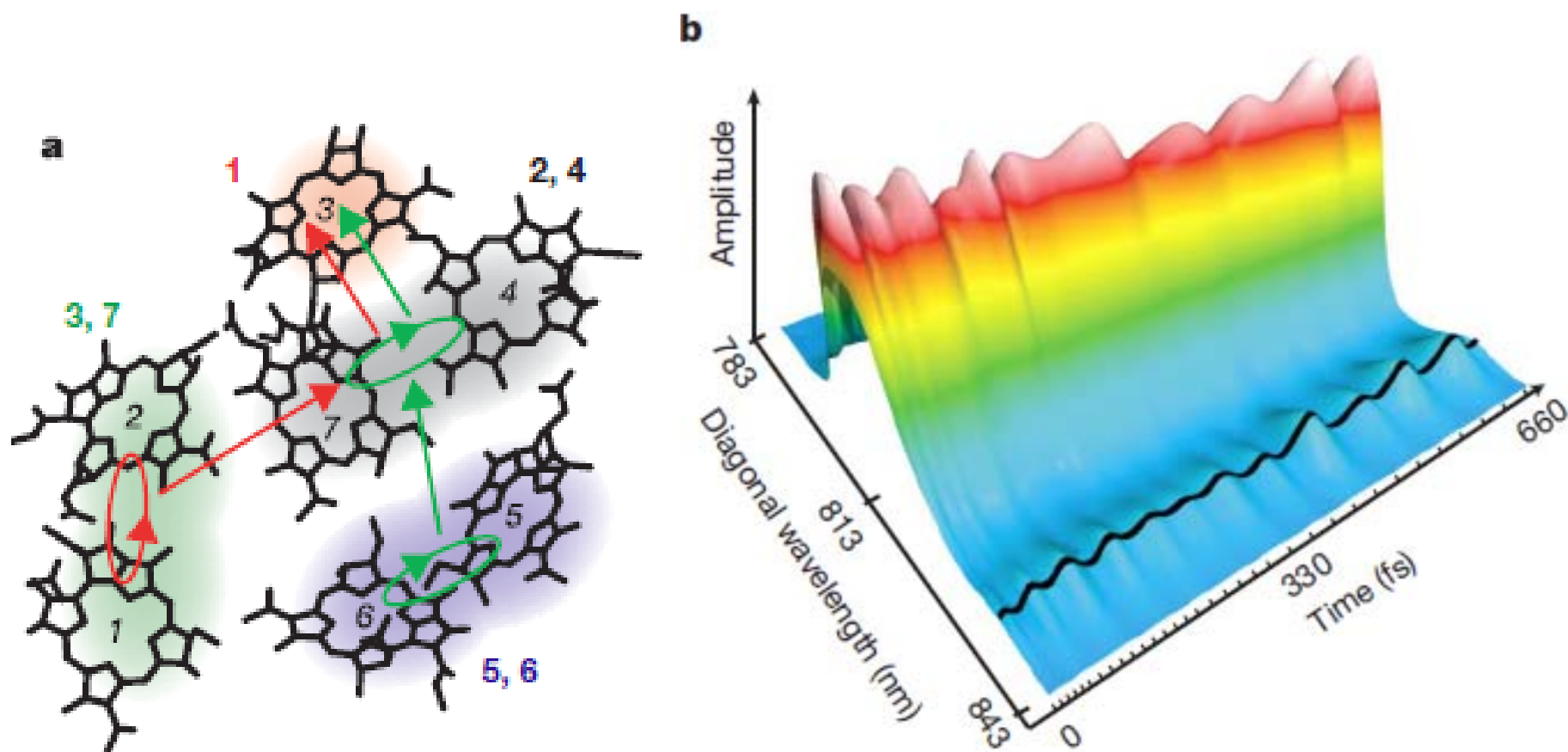
# Excitons in a Ring





# Coherent Transfer of Excitation Energy?

## FMO Complex

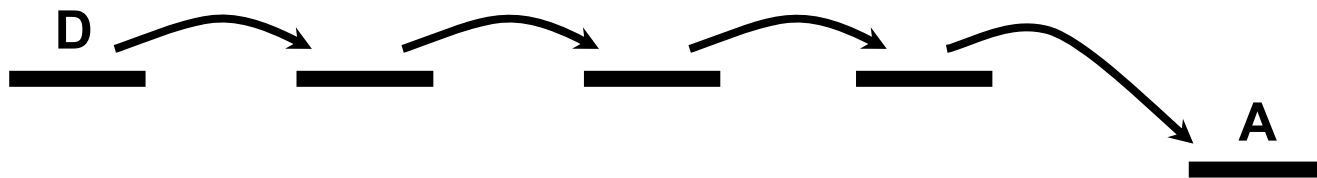


Fleming et al., Nature 434 (2005) 625 and Nature 446 (2007) 782



# Coherent versus Incoherent Transfer

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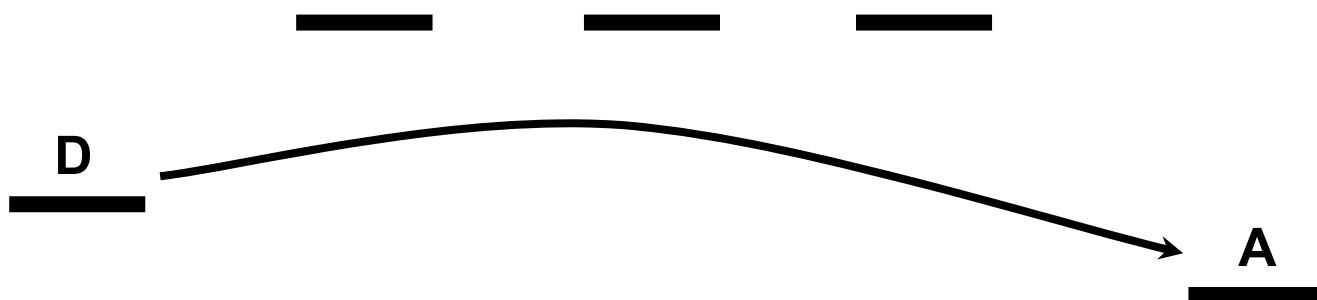




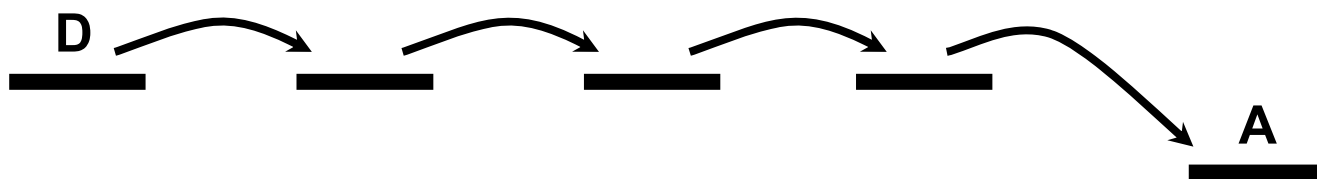
# Bridged Electron Transfer

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Superexchange

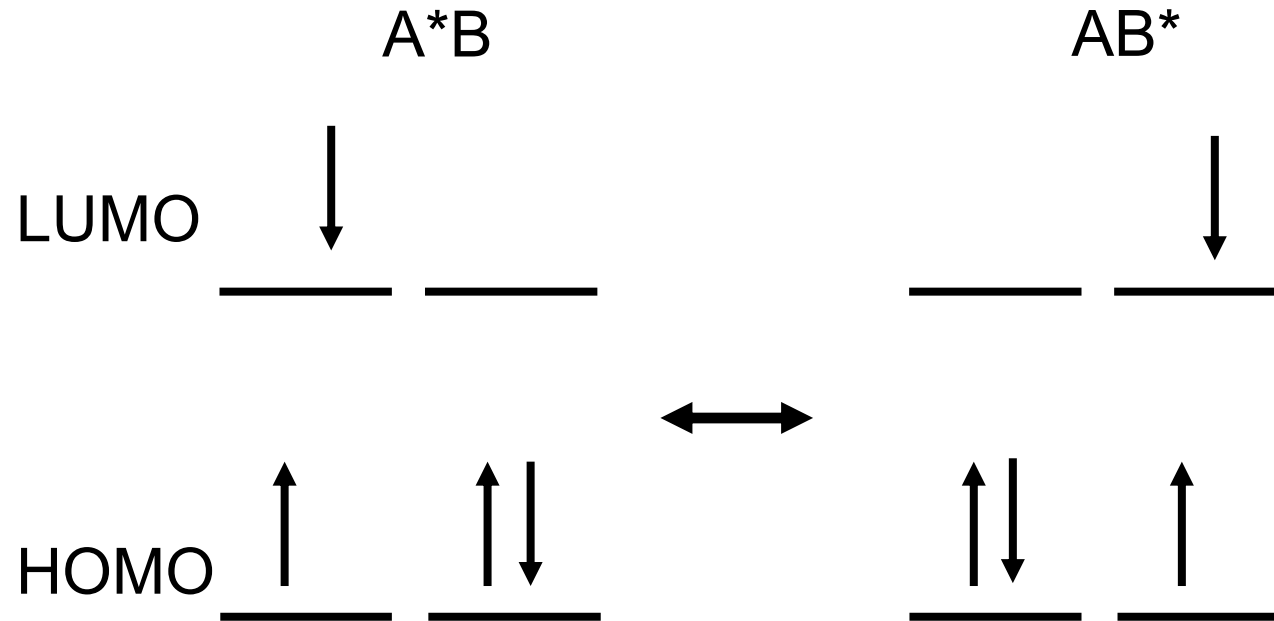


Hopping





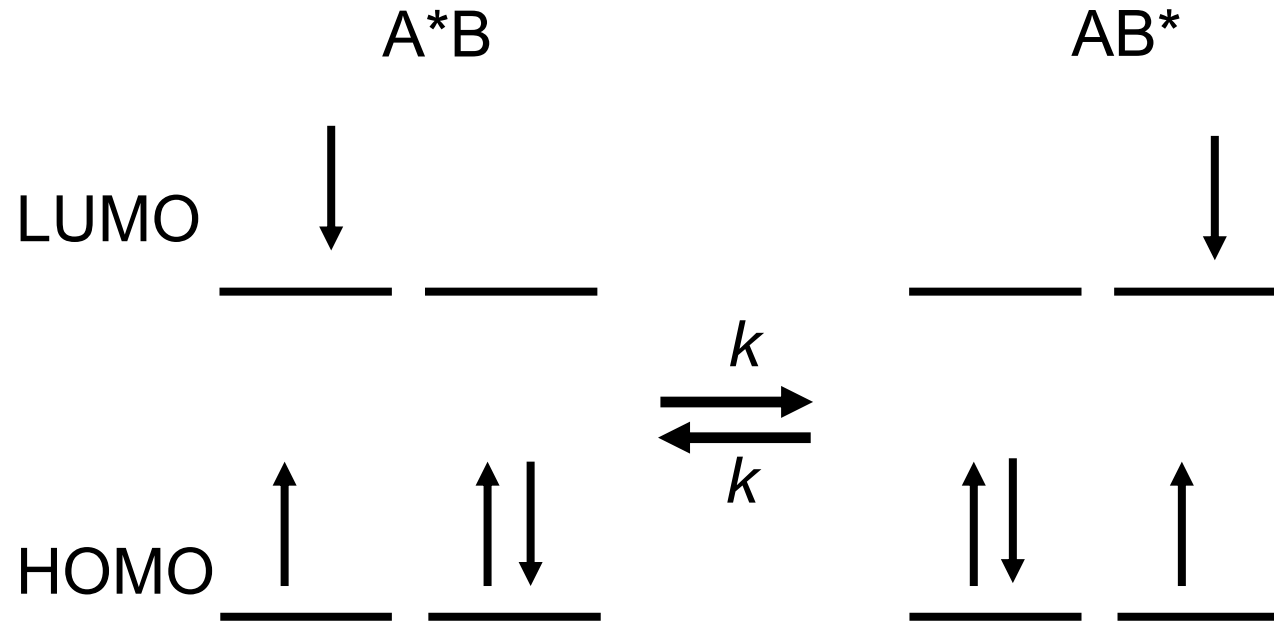
# Exciton Transfer: Coherent



$$V_{12} \approx \frac{\vec{\mu}_1 \vec{\mu}_2}{R_{12}^3} - 3 \frac{(\vec{\mu}_1 \vec{R}_{12})(\vec{\mu}_2 \vec{R}_{12})}{R_{12}^5}$$



# Förster Transfer: Incoherent



$$V_{12} \approx \frac{\vec{\mu}_1 \vec{\mu}_2}{R_{12}^3} - 3 \frac{(\vec{\mu}_1 \vec{R}_{12})(\vec{\mu}_2 \vec{R}_{12})}{R_{12}^5}$$



# Förster Transfer

Fermi Golden Rule

$$k_{DA} = \frac{2\pi}{\hbar} \int V_{DA}^2 f_D(\omega) f_A(\omega) \delta(E_{D1} - E_{D0} - \hbar\omega) \delta(E_{A1} - E_{A0} - \hbar\omega) d\omega$$

$$V_{DA} = \frac{|\mu_D||\mu_A|}{R_{DA}^3} \kappa \quad \Leftarrow \quad V_{DA} = \frac{\vec{\mu}_1 \vec{\mu}_2}{R_{12}^3} - 3 \frac{(\vec{\mu}_1 \vec{R}_{12})(\vec{\mu}_2 \vec{R}_{12})}{R_{12}^5}$$

Absorption and Emission Spectra

$$I_D(\omega) = \frac{4\pi\omega^3}{3c^3} |\mu_D|^2 \int f_D(\omega) \delta(E_{D1} - E_{D0} - \hbar\omega) d\omega$$

$$\alpha_A(\omega) = \frac{4\pi\omega}{3c} |\mu_A|^2 \int f_A(\omega) \delta(\hbar\omega - E_{A1} - E_{A0}) d\omega$$

$$k_{DA} = \frac{9c^4 \kappa^2}{8\pi R_{DA}^6} \int \frac{d\omega}{\omega^4} I_D(\omega) \alpha_A(\omega)$$



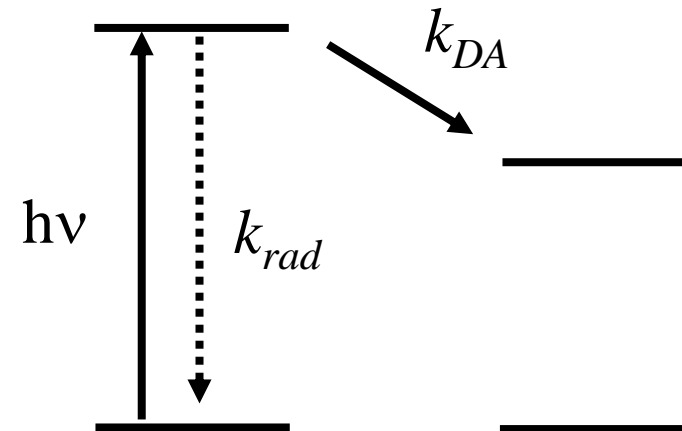
# Förster Transfer

$$k_{DA} = \frac{9c^4 \kappa^2}{8\pi R_{DA}^6} \int \frac{d\omega}{\omega^4} I_D(\omega) \alpha_A(\omega)$$

$$k_{DA} = k_{rad} \left( \frac{R_F}{R_{DA}} \right)^6$$

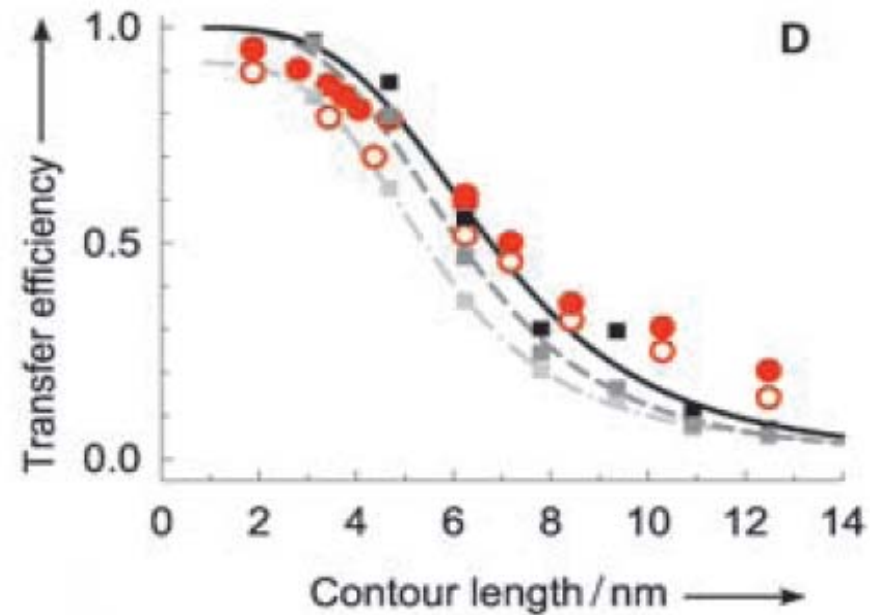
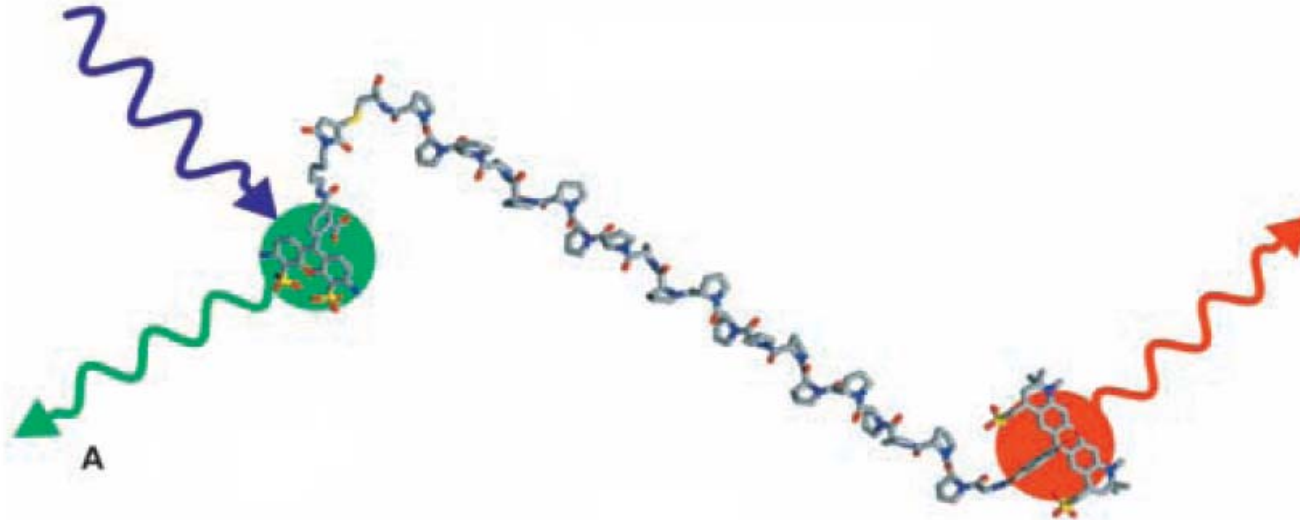
Förster Efficiency

$$\eta_{DA} = \frac{R_F^6}{R_{DA}^6 + R_F^6}$$





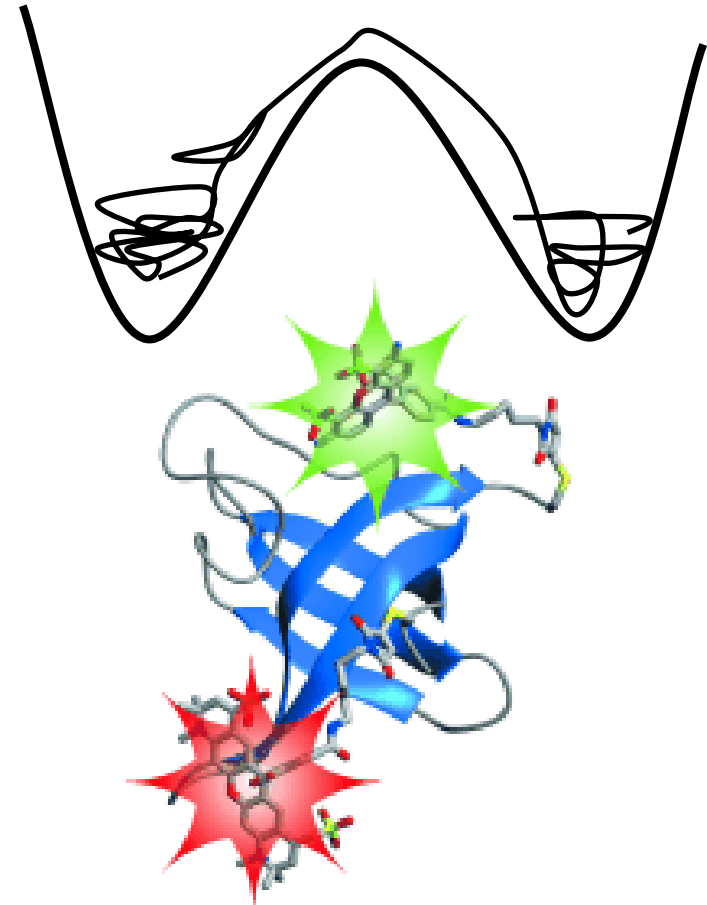
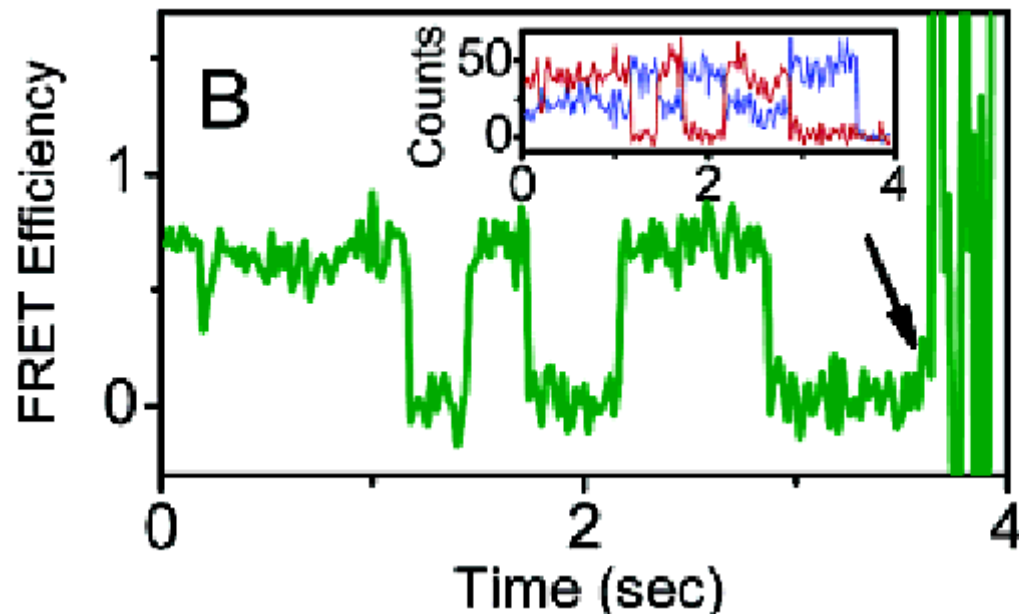
# Förster Transfer



Schuler B, Single-molecule fluorescence spectroscopy of protein folding, ChemPhysChem 6 (2005) 1206-1220



# Protein Folding: Single Molecule Spectroscopy



## Two-State Folding Observed in Individual Protein Molecules

Rhoades, E.; Cohen, M.; **Schuler, B.**; Haran, G.;

*J. Am. Chem. Soc.*; **2004**; 126; 14686-14687