



Contents lists available at ScienceDirect

Journal of Monetary Economics

journal homepage: www.elsevier.com/locate/jmonecoIntangibles, markups, and the measurement of productivity growth[☆]Nicolas Crouzet^{a,*}, Janice Eberly^b^a Kellogg School of Management, Northwestern University, 2211 Campus Drive, Evanston, IL, 60208, USA^b Kellogg School of Management, Northwestern University, and NBER, USA

ARTICLE INFO

Article history:

Received 28 December 2020

Revised 15 September 2021

Accepted 15 September 2021

Available online 20 September 2021

JEL classification:

E22

D24

O47

Keywords:

Productivity growth

Intangible capital

Markups

Mismeasurement

ABSTRACT

In recent years, measured TFP growth in the US has declined. We argue that two forces contributed to this decline: the mismeasurement of intangible capital, and rising markups. Markups affect input shares, while intangibles omitted from measures of investment affect measured capital growth, each potentially generating downward bias in measured TFP growth. Most importantly, when both forces are *simultaneously* present, their effects reinforce each other and amplify the downward bias in measured TFP growth. Using input-output data, we estimate that this mechanism could account for one-third to two-thirds of the decline in measured TFP growth.

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1. Introduction

Productivity is an enduring challenge in the U.S. economy and its measurement. Post-financial crisis, slow growth was initially put down to scarring or the aftermath of the crisis itself. But later work traces the explanation to weak productivity (Fernald et al., 2017). Moreover, they and others date weak productivity earlier than the financial crisis. That is, the weak growth in the U.S. economy following the financial crisis has its roots in a much earlier productivity slowdown. In this paper, we show how the presence of intangible capital and market power, which have also grown over this time period, leads to underestimates of productivity growth. The effect of either alone is relatively small, but together – as in Crouzet and Eberly (forthcoming) – their effect is magnified. Empirically reasonable values of markups and unmeasured capital can account for about half of the measured productivity slowdown in the 2000s.

The US productivity slowdown has been extensively debated and researched, focusing on whether it is a measurement problem or a real phenomenon, and if it is real, what has caused productivity to decline – especially when innovation seems so prevalent. While there are many reasons for productivity to be mismeasured, especially given the methodological and data challenges, most candidate explanations cannot generate the sustained magnitudes seen in the data. For example,

[☆] This paper was prepared for the 2020 JME-SNB-SCG conference, held on October 15, 2020. We thanks Susanto Basu, Antonio Ciccone, our discussant, Ricardo Reis, our editor, and an anonymous referee for comments that greatly helped improve the paper.

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Byrne et al. (2016) take into account mismeasured IT capital and nonmarket consumption (among other factors). These factors have an effect on measured productivity by changing the level of output, but they cannot account for more than a tiny fraction of the magnitude of slowing productivity growth over time.

Research has instead focused on how productivity growth can be so low in the face of apparently enormous innovation in digital technologies and the internet. Prominent among this work is Robert Gordon's research and book (Gordon, 2016) on *The Rise and Fall of American Growth*, arguing that recent innovation has not had the productivity enhancing impact of historical breakthroughs. Impact on the scale of penicillin, he argues, for example, has not occurred in the era of digital innovation.

Concurrent with this work on low productivity, research has expanded into explaining related aspects of the puzzle, such as the low level of investment in the US economy. Low capital investment is consistent with low productivity, but not consistent with observed high firm valuations and profitability, which would instead suggest that the returns to capital investment are high. A growing literature on the growth of market power in the U.S. economy (De Loecker et al., 2020) offers one explanation, since firms have less incentive to expand capacity when they have market power (Gutiérrez and Philippon, 2018).

At the same time that productivity has fallen and market power appears to have risen, intangible capital has also become a larger share of firms capital stocks while physical capital investment has declined (Alexander and Eberly, 2018). Crouzet and Eberly (2019) show that intangibles can explain 30 to 60 percent of the decline, when looking at firm-level and industry-level data, respectively. These explanations are not mutually exclusive and actually reinforce each other, as in Crouzet and Eberly, and the interaction of intangible capital with markups from market power can explain much the decline in observed investment in the U.S.

This paper brings market power and intangible capital together to examine the puzzle of low US productivity. Both phenomena violate the standard assumptions of productivity measurement.

We first show, in Section 2, how market power and omitted intangible capital would appear in an extension of a standard and general productivity measurement framework. We allow for purchases of some capital goods to be incorrectly classified as intermediates in the national accounts, instead of being treated as final spending and accordingly capitalized. Omitted intangible investment is one example, but our treatment is more general.

In this framework, markups alone generate a downward bias in TFP growth. They imply that the measured labor share is an overestimate of the true elasticity of output with respect to labor. When capital is growing faster than labor, this biases downward measures of TFP growth. However, this bias is not quantitatively large, even in extreme cases.

Omitted intangibles alone could also bias measured TFP growth: if the true stock of unmeasured capital is growing more slowly than the measured stock, measured TFP growth will be biased downward. In addition, omitting intangible investment makes the level of GDP too low, relative to true GDP; therefore, the measured labor share is *higher* than the elasticity of output to labor. This upward bias in the measured labor share can be large and increases with the amount of intangible investment omitted from GDP calculations. However, an upward bias in the labor share seems surprising empirically, since the measured labor share has been declining since at least the late 1990s.

Combining markups with omitted intangibles offsets this labor share effect, while preserving the potential for a negative bias in productivity growth. As discussed above, markups tend to make the measured labor share *lower*. Sufficiently high markups can then allow the framework to be consistent with both a large and growing amount of omitted intangible investment *and* a low measured labor share – potentially lower than the true elasticity of output to labor, thus adding to the overall TFP bias.

Aside from these two sources of measurement bias – the capital growth bias, and the labor share bias –, a third source of bias is that GDP growth itself might be mismeasured. This is the bias emphasized by many previous studies. To the extent that omitted intangible investment is growing faster than measured GDP, the true growth rate of GDP might be higher than its measured counterpart, leading to underestimates of true TFP growth.

In Section 2, we therefore develop further results using the balanced-growth version of a model to quantify the effects of the two main mechanisms that we are interested in: markups and omitted intangible capital.

This specialized framework has two key insights. First, while in the model, the *level* of output is mismeasured – it is too low –, its *growth rate* is correctly measured, because omitted and measured investment, in nominal terms, grow at the same rate on the balanced growth path. Thus, in our framework, mismeasurement of GDP growth is not a source of bias in productivity growth by construction, whereas it is the focus of much previous work.

Second, and most important, the model helps clarify under what conditions mismeasurement in the growth rate of capital may lead to underestimating TFP growth. Specifically, we show that this will occur when the price of unmeasured investment grows sufficiently quickly relative to the price of measured capital. This mechanism, on its own, can lead to a substantial downward bias in measured TFP growth, which we characterize analytically.

In Section 3, we then use data on omitted intangibles, in the balanced growth framework, to quantify the size of the combined biases in measured TFP growth. We use the annual Input-Output tables for the 1997–2018 period to measure annual expenditures on 61 commodities or services that are treated as intermediate purchases in national accounting. We then examine those for which reclassifying intermediate purchases as final expenditure on capital goods would have the largest impact on GDP.

Several service groups stand out. Professional, Scientific and Technical services, Administrative and Support services, and Management services, lead to large upward adjustments in measured GDP. We argue that purchases of these services could

plausibly represent investment in what the literature has called organization capital (Atkeson and Kehoe, 2005; Eifeldt and Papanikolaou, 2013): expenditures on workforce human capital, distribution systems and logistics, product design, and customer and brand capital. Importantly, since 1997, the price of these services rose faster than the deflator for personal consumption expenditures, consistent with the necessary condition, implied by the model, under which unmeasured capital would lead to a downward bias in TFP growth.

Using these data and our balanced growth model, we then estimate that the combination of markups and omitted intangibles can explain between one-third and two-thirds of the decline in U.S. productivity from the pre-1997 to the post-1997 period. Table 1 shows that productivity growth measured using the standard Solow residual, declined by 49bps, from 1.11% to 0.62% per year.¹ Our corrected measure of TFP growth, which adjusts for both intangibles and markups, instead declines from 1.11% to 0.95%, or only about one-third as much. Importantly, we also show that measurement bias was likely much smaller in the 1947–1996 period, a period which pre-dates the rise in both intangibles and in markups.²

Our results thus suggest that the decline in TFP growth was, at least in part, the reflection of growing mismeasurement driven by structural changes in the economy – the rise in markups, and the increasing importance of intangibles. Because total GDP growth, in our framework, is *not* mismeasured, this result has implications for understanding sources of GDP growth. For example, since our adjusted measures suggest that more of total GDP growth since the 2000s was driven by TFP growth, investment-specific technical change might have contributed less to GDP growth than previously thought.

The rest of the paper is organized as follows. Section 2 analyzes theoretically the biases that omitted intangibles and markups case generate in the measurement of GDP growth, starting with a general growth accounting framework, and then specializing the analysis to a balanced growth model. Section 3 applies this framework to the data, using measures of intermediate expenditures that should potentially be reclassified as intangible investment. Section 4 concludes.

Related research and contribution

Our work first relates to the literature on the measurement of productivity growth (Basu and Fernald, 2001; Hall, 1968; Jorgenson and Griliches, 1967; Solow, 1957). The closest papers in this literature study the rise in intangible capital. In particular, Corrado et al. (2009) also study how including omitted intangibles affects measures of GDP growth, labor productivity, and TFP growth. Our work complements theirs by first providing a general framework for describing biases in measured TFP growth, allowing in particular for markups; and, empirically, we focus on organization capital (Atkeson and Kehoe, 2005; Eifeldt and Papanikolaou, 2013), whereas Corrado et al. (2009) primarily focus on R&D capital. Heterogeneous price trends between these two types of intangible capital largely explain why we reach different conclusions on the sign of the bias in measured TFP growth created by intangibles. Our paper also closely relates to Basu et al. (2003), who study how unmeasured investments in capital that is complementary to information technology (IT) capital could affect TFP growth. We discuss the differences with that paper in more detail in Section 2.2.2.

As mentioned in the introduction, there is a recent literature focusing on the decline in measured TFP growth (Byrne et al., 2016; Cetto et al., 2016; Fernald et al., 2017). We contribute to this literature by arguing that growing mismeasurement due to intangibles and markups can explain a sizable fraction of this decline. In particular, Byrne et al. (2016) also re-estimate productivity growth for the US after 2005 including mismeasured intangibles. They find a relatively small effect. Our approaches differ in three main ways. First, they do not allow for markups, whereas our analysis shows that including them substantially increases the impact of mismeasured capital on TFP growth. Second, their measures of intangibles are drawn from Corrado et al. (2016), who rely on data beyond the use tables (including compensation of non-production workers) to estimate intangible investment. By contrast, we focus on the use tables to measure intangible investment, but also leverage the corresponding price indices for services and commodities. These price indices have been rising faster than those of measured capital goods, which contributes to the downward bias in TFP growth. Finally, their analysis is off the balanced growth path and allows for mismeasurement of GDP growth, whereas we focus on a balanced growth path where output growth (in consumption units) is correctly measured.

As noted above, our work also relates to the literature on investment-specific technical change, and in particular, to papers in this literature focusing on its impact on long-run growth (Greenwood et al. 1997). As noted, our results indicate that omitting some intangibles from measures of the capital stock can lead to overestimates of the contribution of investment-specific technical change to GDP growth – and, as a result, to underestimates of the contribution of TFP growth. Ongoing work by Gourio and Rognlie (2020) also argues that existing measures may overstate the trend decline in the relative price of investment goods, but they highlight issues of aggregation across existing measures of heterogeneous capital goods, while we explore the possibility that investment in certain types of capital is not well measured.

Our results also connect with the recent literature on the implications of rising rents. Consistent with our findings, this literature documents a significant rise in the pure profit share and in markups, especially after 2000 (Barkai, 2020). We show that rising markups also have quantitatively sizable implications for measuring of TFP growth.

¹ Appendix A.2.1 provides more details on the construction of these figures.

² Because our goal is to study the impact of misclassification of intangibles on TFP growth, we use a sample split coinciding with a breakpoint for the trend in misclassified intangible investment relative to GDP. We use the year 1997 because the ratio of unadjusted GDP to GDP adjusted for omitted intangibles stabilized around that year, after a long period of decline, as highlighted in the top panel of Fig. 3. In Section 3.4 and Appendix A.2.4, we discuss how our results change if we use different breakpoints. We generally find positive but smaller effects for later breakpoints; for instance, with a breakpoint in 2000, markups and intangibles explain one-half of the observed decline in TFP growth, instead of two-thirds with the 1997 breakpoint.

Finally, recent work has highlighted how, when intermediate input use is not symmetric across industries or firms and firms have markups, aggregate TFP may also include terms reflecting allocative (in)efficiencies. This is highlighted, in particular, by Basu and Fernald (2001) and Baqaee and Farhi (2020). In our framework, aggregate TFP, absent markups and absent the measurement issues we highlight, is equal to aggregate technology, so there is no scope for allocative inefficiency. These asymmetries could augment our mechanism by providing a separate way in which factor use may depress measured TFP. Relatedly, Bils et al. (2020) study how mismeasurement in revenue and inputs can affect the allocative efficiency component of TFP. Our analysis differs from theirs in several dimensions. First, their focus is on the misallocation component of TFP, and how it compares across countries. In our paper, we do not study the contribution of misallocation to aggregate TFP, in the sense that there is no wedge between the marginal revenue product of inputs and their marginal cost. Second, their focus is on differences in the level of sectoral TFP; instead, our focus is on the growth rate of aggregate TFP. Finally, while they consider mismeasurement that is random (and similar to classical measurement error), in our paper, mismeasurement is due to investment expenditures being misclassified as intermediate purchases. This is important because in our case, mismeasurement can be addressed by reclassifying intermediate expenditures.

2. Theory

This section studies conditions under which Solow residuals can be biased downward relative to true TFP growth. We focus on markups, omitted intangibles, or the combination of the two, as a source of such bias. Throughout the paper, we use a value added production function. Appendix A.1.2 shows that our results on the value added Solow residuals hold in a model where the underlying production function uses intermediate inputs.³

2.1. General results

We start by deriving results on measurement bias that rely on minimal assumptions.

2.1.1. The standard methodology

The Solow residual (Basu and Fernald, 2001; Jorgenson and Griliches, 1967) is defined as:

$$\frac{d\hat{Z}_t}{\hat{Z}_t} = \frac{d\hat{Y}_t}{\hat{Y}_t} - \hat{s}_{L,t} \frac{d\hat{L}_t}{\hat{L}_t} - (1 - \hat{s}_{L,t}) \frac{d\hat{K}_t}{\hat{K}_t} \tag{1}$$

where $d\hat{Y}_t/\hat{Y}_t$ growth rate of real output, $d\hat{L}_t/\hat{L}_t$ and $d\hat{K}_t/\hat{K}_t$ are the growth rates of real capital and labor inputs, and $\hat{s}_{L,t} = \frac{W_t \hat{L}_t}{\hat{N}_t}$ is the labor share of value added, with $\hat{N}_t = \hat{P}_t \hat{Y}_t$ denoting nominal value added.⁴ In words, measured TFP growth is the gap between the growth rate of real output, and a weighted sum of the growth rates of capital and labor inputs.⁵ The input weights are payments to each input relative to total value added, with the labor share $s_{L,t}$ measured directly from payments to labor, and the capital share computed as a residual. Such a measure produces an unbiased estimate of TFP growth under four assumptions:

A1 : Production follows $Y_t = Z_t F(K_t, L_t)$, where F is homogeneous of degree 1.

A2 : Labor input is given by: $L_t = \arg \min_{\tilde{L}_t} W_t \tilde{L}_t$ s.t. $Z_t F(K_t, \tilde{L}_t) \geq Y_t$.

A3 : The price of output is equal to its marginal cost: $P_t = MC_t$, where MC_t is the Lagrange multiplier on the output constraint $Z_t F(K_t, \tilde{L}_t) \geq Y_t$.

A4 : There is no measurement error in growth rates for inputs and output, $d\hat{X}_t/\hat{X}_t = dX_t/X_t$ for $X \in \{Y, K, L\}$, and there is no measurement error in levels for the labor income share: $\hat{s}_{L,t} = s_{L,t}$.

Under A1, growth in total factor productivity is given by:

$$\frac{dZ_t}{Z_t} = \frac{dY_t}{Y_t} - (1 - \epsilon_{L,t}) \frac{dK_t}{K_t} - \epsilon_{L,t} \frac{dL_t}{L_t}, \tag{2}$$

where $\epsilon_{L,t}$ is the elasticity of output with respect to labor. Under A2, $\epsilon_{L,t}$ is related to the labor cost share by:

$$\epsilon_{L,t} = \frac{F_L(K_t, L_t)L_t}{F(K_t, L_t)} = \frac{W_t L_t}{MC_t Y_t}. \tag{3}$$

³ The Appendix also explores the link between TFP growth and the gross output Solow residual.

⁴ Throughout the paper, we use the hat notation in reference to measured variables. This helps distinguish them from their unbiased values, which we denote without the hat. Additionally, we use the notation dX_t/X_t for the continuous-time growth rate $\dot{X}_t/X_t = \lim_{dt \rightarrow 0} (1/dt)(X_{t+dt} - X_t)/X_t$. In discrete-time data, we approximate it using the log-growth rates $\log(X_{t+dt}/X_t)$.

⁵ Throughout, we express output in units of consumption, so that P_t represents the price of consumption goods. We follow this convention in order to be consistent with the model we study later in this section. Correspondingly, in all our empirical measures of Solow residuals, output is expressed in consumption units. We provide details on measures of output growth in consumption units, and a comparison with chained GDP growth, in Appendix A.2.1; the two measures imply similar declines in Solow residuals after 1997, as shown in Appendix Table A2. Appendix A.1.1.3 discusses the biases which using chained GDP growth would add to our basic exercise. See also Oulton (2007) for a discussion of chained GDP Solow residuals in models where the price of investment relative to consumption goods is not 1.

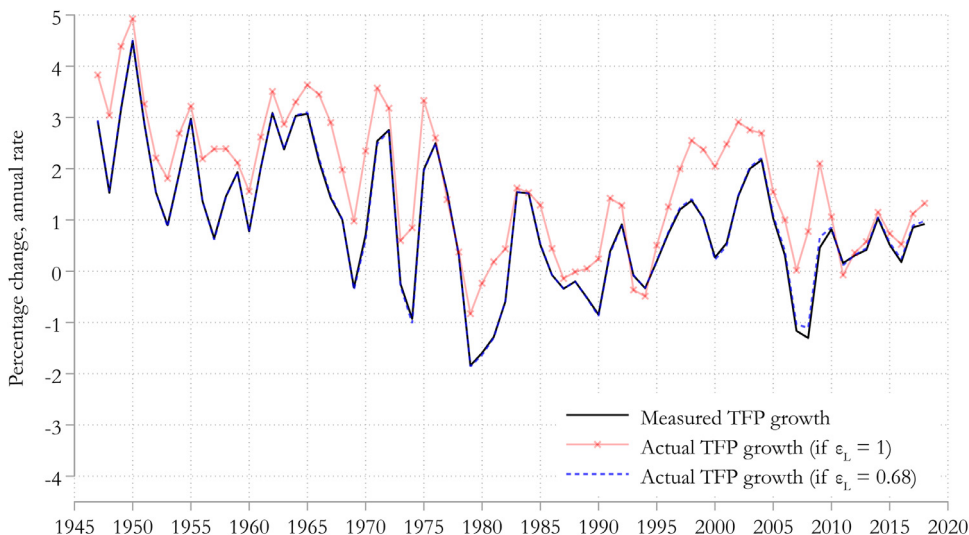


Fig. 1. Measured TFP growth, unadjusted and adjusted for markups. The solid black line is annual TFP growth, constructed as $d\hat{Z}_t/\hat{Z}_t = d\hat{Y}_t/\hat{Y}_t - \hat{s}_{L,t}d\hat{L}_t/\hat{L}_t - (1 - \hat{s}_{L,t})d\hat{K}_t/\hat{K}_t$, where $d\hat{Y}_t/\hat{Y}_t$ is output growth, $\hat{s}_{L,t}$ is the measured labor share of income, $d\hat{L}_t/\hat{L}_t$ is labor input growth, and $d\hat{K}_t/\hat{K}_t$ is capital input growth, all obtained as annual average from the quarterly data of Fernald (2014). The solid red line is TFP growth adjusted for markups, assuming that $\epsilon_{L,t} = 1$: $(d\hat{Z}_t/\hat{Z}_t)^{(adj)} = d\hat{Z}_t/\hat{Z}_t + (1 - \hat{s}_{L,t})(d\hat{K}_t/\hat{K}_t - d\hat{L}_t/\hat{L}_t)$ i.e. the upper bound (in absolute value) for the bias in measured TFP growth. The dashed blue line TFP growth adjusted for markups, when the output elasticity of labor is assumed to be given by the sample average of the labor income share prior to 1995: $(d\hat{Z}_t/\hat{Z}_t)^{(adj)} = d\hat{Z}_t/\hat{Z}_t + (\hat{s}_{L,t} - \hat{s}_{L,t}) (d\hat{K}_t/\hat{K}_t - d\hat{L}_t/\hat{L}_t)$, with $\hat{s}_{L,t} = 0.68$. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Under A3, the labor cost share is equal to its income share:

$$\epsilon_{L,t} = \frac{W_t L_t}{MC_t Y_t} = \frac{W_t L_t}{P_t Y_t} = \hat{s}_{L,t}. \tag{4}$$

Therefore, the elasticities in Equation (2) can be derived from the labor income share.⁶ Finally, under A4, all the variables involved in the right-hand side of Equation (2) are correctly measured, so that the resulting TFP growth measure is unbiased.

2.1.2. Bias due to markups

Assume that A3 is relaxed, and let: $\mu_t = \frac{P_t}{MC_t}$. We will consider the situation where the price-cost markup is larger than 1, so there may be pure profits: $\mu_t \geq 1$.⁷ In this case, the measured labor share is an underestimate of the output elasticity of labor: $\hat{s}_{L,t} \leq \mu_t \hat{s}_{L,t} = \epsilon_{L,t}$. Additionally, A1 implies that $\epsilon_{L,t} \leq 1$; $\mu_t \leq \hat{s}_{L,t}^{-1}$. We then have the following result.

Result 1. When $\mu_t \geq 1$, the bias in measured TFP growth is given by:

$$\frac{d\hat{Z}_t}{\hat{Z}_t} - \frac{dZ_t}{Z_t} \equiv \Delta_t = -\hat{s}_{L,t}(\mu_t - 1) \left(\frac{dK_t}{K_t} - \frac{dL_t}{L_t} \right). \tag{5}$$

Moreover, when $dK_t/K_t > dL_t/L_t$, $\Delta_t \leq 0$, and the bias is bounded (in absolute value) by $|\Delta_t| \leq (1 - \hat{s}_{L,t}) \left(\frac{dK_t}{K_t} - \frac{dL_t}{L_t} \right)$, with the upper bound reached when $\epsilon_{L,t} = 1$, i.e. only labor is used in production.

With markups, the true elasticity of output to labor, $\epsilon_{L,t}$, is higher than the measured labor income share $\hat{s}_{L,t}$. As a result, the true elasticity of output to capital, $1 - \epsilon_{L,t}$, is lower than $1 - \hat{s}_{L,t}$, the (residual) capital income share. When capital grows faster than labor (the empirically relevant case, as indicated by Table 1), the latter effect dominates, and the Solow residual is biased downward.

Fig. 1 reports time series for measured and adjusted TFP growth, and Appendix Table A1 reports estimates of the size of this bias. First, we assume that the true elasticity of output to labor is 1, so that the bias is at its upper bound. In this case, measured TFP growth is approximately $\hat{\Delta}_t = 0.80\%$ lower than true TFP growth. However, this gap is roughly the same in the pre- and post-1997 periods and cannot explain a substantial decline in estimated TFP growth. Using a more plausible Cobb-Douglas labor share, so when $\epsilon_{L,t} = \hat{s}_{L,t} = 0.68$, the pre-1997 average of the labor income share, the bias is only $\hat{\Delta}_t = 0.09\%$

⁶ An alternative approach is to directly measure cost shares, which are correct measures of output elasticities even with markups, but this requires proxies for the (generally unobservable) user costs of capital.

⁷ Note that μ_t a value-added markup, as MC_t is the marginal cost of value added.

on average in that case. Moreover, the increase in $\bar{\Delta}_t$ from pre- to post-1997 is positive but small – less than 1/5th of the observed decline in measured TFP growth.

2.1.3. Bias due to omitted intangibles

Assume now that A3 holds, but A4 is relaxed: there is measurement error in input and output quantities because of omitted intangible capital. Let B_t denote nominal investment expenditures contributing to the growth of the stock of unmeasured intangible capital. In national accounts, these investment expenditures will be recorded, but treated as intermediate goods purchases, as opposed to purchases of final investment goods. Therefore, measured output \hat{Y}_t and actual output Y_t will be related through:

$$\hat{N}_t = P_t \hat{Y}_t = P_t Y_t - B_t, \tag{6}$$

where recall that P_t is the price of consumption goods, and Y_t is assumed to be expressed in units of the consumption good, so that $P_t Y_t$ is measured total nominal output.

The omission of intangibles, both as a stock and a flow, impacts measured TFP growth in three ways. First, the growth rate of output might be mis-measured; namely:

$$\frac{d\hat{Y}_t}{\hat{Y}_t} = \frac{dY_t}{Y_t} + \left(\frac{1}{b_t} - 1\right) \left(\frac{dY_t}{Y_t} - \frac{d\tilde{B}_t}{\tilde{B}_t}\right), \tag{7}$$

where: $b_t \equiv \frac{P_t \hat{Y}_t}{P_t Y_t} \leq 1$ is the ratio of measured (or unadjusted) to actual (or adjusted) output, and $\tilde{B}_t = B_t/P_t$. Second, because the level of output is mismeasured, the labor share might be mismeasured. Specifically, the measured labor share of income is always an *overestimate* of the elasticity of output with respect to labor: $\hat{\epsilon}_{L,t} = \frac{W_t L_t}{P_t \hat{Y}_t} = \frac{W_t L_t}{P_t Y_t} \frac{1}{b_t} = \frac{\epsilon_{L,t}}{b_t} > \epsilon_{L,t}$. A3 holds, so the true labor income share $W_t L_t/P_t Y_t$ is equal to the elasticity of output to labor. However, because of omitted intangible investment, which biases measured output downward, the measured labor income share $W_t L_t/(P_t \hat{Y}_t)$ is higher than the true labor income share. Note that this is the opposite effect from markups. Third, the measured growth rate of capital might be incorrect: $\frac{d\hat{K}_t}{\hat{K}_t} \geq \frac{dK_t}{K_t}$. The following result summarizes these different sources of bias.

Result 2. When intangibles are omitted ($b_t < 1$), the bias in measured TFP growth is:

$$\begin{aligned} \Delta_t &= \Delta_t^{(1)} + \Delta_t^{(2)} + \Delta_t^{(3)} \\ \Delta_t^{(1)} &\equiv \left(\frac{1}{b_t} - 1\right) \left(\frac{dY_t}{Y_t} - \frac{d\tilde{B}_t}{\tilde{B}_t}\right) && \text{(output growth bias)} \\ \Delta_t^{(2)} &\equiv \hat{\epsilon}_{L,t} (1 - b_t) \left(\frac{d\hat{K}_t}{\hat{K}_t} - \frac{dL_t}{L_t}\right) && \text{(labor share bias)} \\ \Delta_t^{(3)} &\equiv (1 - \epsilon_{L,t}) \left(\frac{dK_t}{K_t} - \frac{d\hat{K}_t}{\hat{K}_t}\right) && \text{(capital growth bias)}. \end{aligned} \tag{8}$$

Three points stand out. First, the sign of the bias introduced by capital growth is ambiguous in general: it depends on the growth rate of the measured capital stock relative to the growth rate of the true capital stock. Nevertheless, when measured (real) capital input \hat{K}_t is growing faster than actual (real) capital input, the simple Solow residual will tend to underestimate true output growth.

Second, and most important, as noted above, there is mismeasurement in the elasticity of output with respect to labor, as in the case of markups; but it has the *opposite* sign as with markups. Intuitively, this is because measured output is too low, so that the measured labor share is too *high* relative to the elasticity of output with respect to labor, or equivalently, the measured capital share is too *low* relative to the elasticity of output with respect to capital. When capital is growing faster than labor, this biases measured TFP upward.

A third and equally important point is that, since the measured labor income share is $\hat{\epsilon}_{L,t} = \epsilon_{L,t}/b_t$, if the elasticity of output with respect to labor is constant, $\epsilon_{L,t} = \epsilon_L$, but there is a growing amount of omitted intangible investment, so that b_t is falling, then the measured labor income share should rise. By contrast, the measured labor share of income has declined since at least the late 1990s. Thus, on its own, a rising amount of omitted intangible capital, even if produces downward bias in the Solow residual, would likely have counterfactual implications for the measured labor share.

2.1.4. Bias with both markups and intangibles

The previous discussion shows that markups alone imply that the simple Solow residual underestimates true TFP growth, by making the measured labor income share *lower* than the elasticity of output with respect to labor. The magnitude of the bias in measured TFP growth, however, appears to be relatively small. On the other hand, omitted intangibles could also generate a downward bias in measured TFP growth, if their omission makes the growth rate of capital inputs too high. But omitting intangibles makes the labor income share *higher* than the elasticity of output with respect to labor, potentially

offsetting some of the downward bias. Thus, alone, neither mechanism appears to be sufficient to generate a negative and large bias in measured TFP growth. Because they work through different channels, however, combining the two is potentially more powerful than either alone.

Result 3. With omitted intangibles ($b_t < 1$) and markups ($\mu_t > 1$), the bias in measured TFP growth can again be decomposed as:

$$\Delta_t = \Delta_t^{(1)} + \Delta_t^{(2)} + \Delta_t^{(3)}. \tag{9}$$

The output growth bias $\Delta_t^{(1)}$ and the capital growth bias $\Delta_t^{(3)}$ have the same expression as in Result 2, and the labor share bias $\Delta_t^{(2)}$ is given by:

$$\Delta_t^{(2)} = -\hat{s}_{L,t}(\mu_t b_t - 1) \left(\frac{d\hat{K}_t}{\hat{K}_t} - \frac{dL_t}{L_t} \right). \tag{10}$$

This result has two implications. First, the measured labor share is given by $\hat{s}_{L,t} = \frac{\epsilon_{L,t}}{\mu_t b_t} \geq \epsilon_{L,t}$. With both markups and intangibles, the measured labor share need not be an upper bound for the elasticity of output with respect to labor, so that rising intangibles need not lead to a rising labor share. Second, all three sources of bias described in Result 3 could now potentially be negative and contribute to measured TFP growth being lower than actual TFP growth. To determine their signs, we next turn to a more specialized model.

2.2. Results in a balanced growth model

We next derive expressions for the measurement biases in the context of a balanced growth model where we allow for both markups and mismeasured capital.

2.2.1. Model elements

Description Here, we briefly summarize key model elements; Appendix A.1.1 provides details. A representative firm chooses inputs in order to minimize total production costs. There are three inputs: labor L_t , and two types of capital: $K_{1,t}$ (which represents measured capital), and $K_{2,t}$ (which represents omitted intangibles). The production function is:

$$Y_t = Z_t (K_{1,t}^{1-\eta} K_{2,t}^\eta)^{1-\alpha} L_t^\alpha; \tag{11}$$

where $1 - \alpha$ is the elasticity of output with respect to labor, and η is the Cobb-Douglas share of omitted intangibles in total capital, with $\eta = 0$ corresponding to no omitted intangibles.

Capital and labor are rented by the firm on perfectly competitive markets from a representative household that owns them. The household's budget constraint is:

$$R_{1,t}K_{1,t} + R_{2,t}K_{2,t} + W_t L_t + \Pi_t = P_t C_t + Q_{1,t} I_{1,t} + Q_{2,t} I_{2,t}, \tag{12}$$

where $R_{n,t}$ is the user cost of capital of type n , W_t is the wage rate, Π_t are profits rebated by the firm to the household, C_t is consumption, P_t is the price of consumption goods, $I_{n,t}$ is investment in capital of type n , and $Q_{n,t}$ is price of capital of type n . The model is set in continuous time; labor and the prices of capital goods evolve exogenously and deterministically, according to $dL_t = g_L L_t dt$ and $dQ_{n,t} = g_{Q_n} Q_{n,t} dt$, $n = 1, 2$, and the law of motion for each capital type is given by $dK_{n,t} = (I_{n,t} - \delta_n K_{n,t}) dt$, $n = 1, 2$, where δ_n are capital-specific depreciation rates. The household's objective is $U = \int_{t \geq 0} e^{-\rho t} \frac{C_t^{1-\sigma}}{1-\sigma} dt$, with $\rho > 0$ and $\sigma \geq 1$. Finally, we allow for a constant wedge between the price of consumption goods, P_t , and their marginal cost of production, MC_t : $P_t = \mu MC_t$, $\mu \geq 1$. Pure profits are then $\Pi_t = (\mu - 1) MC_t Y_t$. In equilibrium, we will normalize $P_t = 1$, so that prices and quantities will be expressed relative to consumption.⁸ Thus, this setup satisfies assumptions A1 (constant returns) and A2 (cost minimization), and violates assumption A3 when $\mu > 1$, and assumption A4 when $\eta > 0$.

Balanced growth path Along the unique balanced growth path of the model, output growth dY_t/Y_t is constant, and given by:

$$g = g_L + \frac{1}{1-\alpha} g_Z - \frac{\alpha}{1-\alpha} g_Q, \tag{13}$$

where g_Q is a weighted average of the growth rate of the prices of the two types of capital goods, $g_Q = (1 - \eta)g_{Q_1} + \eta g_{Q_2}$. Each capital stock $K_{n,t}$ grows at rate $g_{K_n} = g - g_{Q_n}$, while the growth rate of the total capital stock $K_t = K_{1,t}^{1-\eta} K_{2,t}^\eta$ is $g_K = g - g_Q$. Additionally, the risk-free rate along the balanced growth path is given by $r = \rho + \sigma g$. A complete characterization of the balanced growth path is reported in Appendix A.1.1.

⁸ In particular, output Y_t is expressed in consumption units. Appendix A.1.1.3 discusses how dY_t/Y_t relates, in the model, to chained GDP growth as defined in national accounts.

2.2.2. An analytical characterization of the bias

We assume that labor L_t and payments to labor $W_t L_t$ are correctly measured, but that intangible investment – that is, investment in $K_{2,t}$ – is treated as intermediate expenditure in the expenditure-side measure of output, so that: $\hat{Y}_t = Y_t - Q_{2,t} I_{2,t}$ and $\hat{K}_t = K_{1,t}$.⁹ Mirroring the discussion in Section 2.1, the balanced growth path has three key features that affect the measurement of TFP growth.

First, output growth is measured accurately. Recall that measured and actual output differ because investment in capital of type 2 is treated as an intermediate expenditure, and not a purchase of final product: $\hat{Y}_t = Y_t - Q_{2,t} I_{2,t}$. However, along the balanced growth path, expenditures on all final products – including expenditure on intangibles, $Q_{2,t} I_{2,t}$ – grow at rate g . Therefore, there is no bias in the measured growth rate of output by construction.¹⁰

Second, there is bias in the level of measured output. This, in turn, affects the measured labor share. Specifically, the ratio of measured to actual output is constant along the balanced growth path, and given by:

$$b_t = b = \frac{\hat{Y}_t}{Y_t} = 1 - \frac{\alpha \eta g + \delta_2 - g_{Q_2}}{\mu r + \delta_2 - g_{Q_2}}. \tag{14}$$

As a result, the measured labor share is:

$$s_L = \frac{W_t L_t}{P_t \hat{Y}_t} = \frac{1 - \alpha}{b \mu} \geq 1 - \alpha = \epsilon_L. \tag{15}$$

Third, the growth rate of capital is mis-measured, because only the stock of capital of type 1, $K_{1,t}$ is measured, and it may not grow at the same rate as omitted capital $K_{2,t}$:

$$\frac{dK_t}{K_t} - \frac{d\hat{K}_t}{\hat{K}_t} = \eta(g_{Q_2} - g_{Q_1}); \tag{16}$$

that is, measured capital growth is higher than actual capital growth, if and only if, prices of omitted intangibles are growing faster than prices of measured capital.

Result 4. The bias in measured TFP growth along the balanced growth path is constant:

$$\Delta_t = \Delta = \Delta^{(1)} + \Delta^{(2)} + \Delta^{(3)} \tag{17}$$

where:

$$\Delta^{(1)} = \alpha \eta \frac{g + \delta_2 - g_{Q_2}}{\mu(r - g) + (\mu - \alpha \eta)(g + \delta_2 - g_{Q_2})} (g - g) = 0 \tag{1 (output growth bias)}$$

$$\Delta^{(2)} = \frac{-(\mu - 1)(r + \delta_2 - g_{Q_2}) + \alpha \eta (g + \delta_2 - g_{Q_2})}{\mu(r - g) + (\mu - \alpha \eta)(g + \delta_2 - g_{Q_2})} (g_Z - g_{Q_1} - \alpha \eta (g_{Q_2} - g_{Q_1})) \tag{labor share bias}$$

$$\Delta^{(3)} = -\alpha \eta (g_{Q_2} - g_{Q_1}) \tag{capital growth bias}$$

In balanced growth, there is no bias due to mismeasurement of output growth: $\Delta^{(1)} = 0$; so the bias is the sum of the labor share and the capital biases $\Delta = \Delta^{(2)} + \Delta^{(3)}$.

Two limiting cases are useful to consider. First, assume that there are no omitted intangibles: $\eta = 0$, but markups are positive, $\mu > 1$. Then, the capital growth bias is zero; all mismeasurement comes from the downward bias that markups create in the labor share. The value of the bias is given by $\Delta^{(2)} = -\frac{\mu - 1}{\mu} (g_Z - g_Q)$, reflecting the fact that it depends on the growth rate of the capital-to-labor ratio, which is given by $(g_Z - g_Q)/(1 - \alpha)$. The bias is positive whenever capital grows faster than labor, or $g_Z > g_Q$ in the model.

The other limiting case is $\eta > 0$ (omitted intangibles) but $\mu = 1$ (no markups). In Appendix A.1.1.4, Result 5, we show analytically that the measurement bias will be negative, if and only if, the relative price of omitted capital is growing sufficiently fast, i.e. g_{Q_2} is sufficiently large. The reason for this is simple: a higher growth rate of intangible capital prices implies a lower growth rate of the stock of omitted intangibles, $K_{2,t}$, and therefore, a lower growth rate of the true stock of capital K_t , relative to the measured stock, $\hat{K}_t = K_{1,t}$.¹¹

⁹ Output in the income approach would also be underestimated, as measured gross operating surplus of firms would be $Y_t - Q_{2,t} I_{2,t} - W_t L_t$ instead of $Y_t - W_t L_t$.

¹⁰ Outside of the balanced growth path, the growth rate of measured output could differ from the true growth rate of output. This assumption could be relaxed, for instance by studying transitional dynamics between steady-state. It is likely that accumulation of intangibles along the transition of the model from low- to high- η steady states (steady-states with low and high levels of the omitted capital) would further exacerbate the negative bias in measured TFP growth, as investment in omitted intangibles would be high along that transition path.

¹¹ Note, however, that along the balanced growth path, expenditures on intangible capital goods $Q_{2,t} I_{2,t}$, or the value of the intangible capital stock in consumption units, $Q_{2,t} K_{2,t}$, are growing at the same rate as measured capital; so, this mechanism does not require a shrinking ratio of intangible capital (at cost) to measured capital (at cost).

These results relate to Basu et al. (2003), who study a model with unmeasured investment in capital that is complementary with IT capital. They show that in balanced growth, the bias in measured TFP growth must be positive. By contrast with our model, they do not allow for markups, and assume that the price of unmeasured capital and output are constant and equal to one another. This corresponds to $g_{Q_1} = g_{Q_2} = 0$ and $\mu = 1$ in our model. In this case, using Result 4, the measurement bias in TFP growth boils down to the labor share bias: $\Delta^{(2)} = \alpha\eta(g + \delta_2)/(r - g + (1 - \alpha\eta)(g + \delta_2))g_Z$, which is strictly positive in the balanced growth path, consistent with their result.

2.2.3. How large can the bias be?

Beyond the cases $\eta = 0$ and $\mu = 1$, it is not possible to characterize the sign of the bias analytically, so we provide a numerical illustration. First, we set $\rho = 0.04, \sigma = 1, \delta_2 = 0.20$.¹² Second, for different values of η and α , we compute productivity growth g_Z required to match the post-1997 values of output growth, labor growth, capital growth, and the measured labor share. Finally, we construct the implied markup and ratio of measured to actual GDP.¹³

The results are reported in Fig. 2; the top panel focuses on results when the Cobb–Douglas capital share is $\alpha = 0.32$, consistent with the pre-1997 value of the measured labor share.¹⁴ The left graph on the top panel indicates that, with $\eta = 0.5$ and $g_{Q_2} = 2\%$, the balanced growth model can fit the post-1997 data on output growth, input growth, and the labor share – and thus on measured TFP growth –, without requiring a decline in true TFP growth relative to the pre-1997 period.

In order to do this, the model requires two additional forces. First, omitted investment in intangibles must represent approximately 11% of measured GDP. Second, the markup must be substantially above 1. Why is this? We fixed the Cobb–Douglas share of labor to $1 - \alpha = 0.68$, but the post-1997 data, the measured labor income share is, on average, lower: $\hat{s}_L = 0.64$. Imagine that there were no markups: $\mu = 1$. The model-implied measured labor share would then be given by $(1 - \alpha)/b$. If $b < 1$ (that is, with omitted intangibles), this value would be larger than 0.68, and thus larger than the measured labor share. Thus, markups are required in order to offset the upward bias of the measured labor income share.

3. Empirics

This section assesses, empirically, whether the combined effect of omitted intangible investment and markups creates a large negative bias in measured TFP growth.

3.1. Methodology

We use two approaches, meant to answer different questions. The first approach provides an estimate of the rate of relative price growth of omitted intangibles, g_{Q_2} , necessary to explain a given gap between true and measured TFP. The second approach instead uses empirical proxies for g_{Q_2} to estimate this gap directly. Since the first approach only uses data on expenditures on omitted intangibles, and not on prices, it can be applied more broadly.

First approach: computing required relative price growth Given measured expenditures M on a particular type of intermediate commodity or service, we construct:

$$\hat{b} = \frac{\text{Measured GDP}}{\text{Adjusted GDP}} = \frac{PY}{PY + M} \tag{18}$$

This ratio captures mismeasurement in the level of GDP if recorded intermediate expenditures on the commodity or service were in fact (misclassified) intangible investment. Using the model, we then solve for the price growth rate g_{Q_2} , such that for any \tilde{g}_Z :

- (1) true TFP growth in the model, g_Z , is given by $g_Z = \tilde{g}_Z$;
- (2) the ratio of measured to adjusted GDP in the model, b is given by $b = \hat{b}$;
- (3) the model matches measured values of output growth \hat{g} , labor growth \hat{g}_L , capital growth \hat{g}_K , and the labor share \hat{s}_L , and therefore of the Solow residual \hat{g}_Z .

Intuitively, this approach produces the growth rate g_{Q_2} , such that all of the gap between true TFP growth \tilde{g}_Z and the Solow residual \hat{g}_Z is due to mismeasurement. Appendix A.2.2 shows that there is a unique such value for g_{Q_2} .

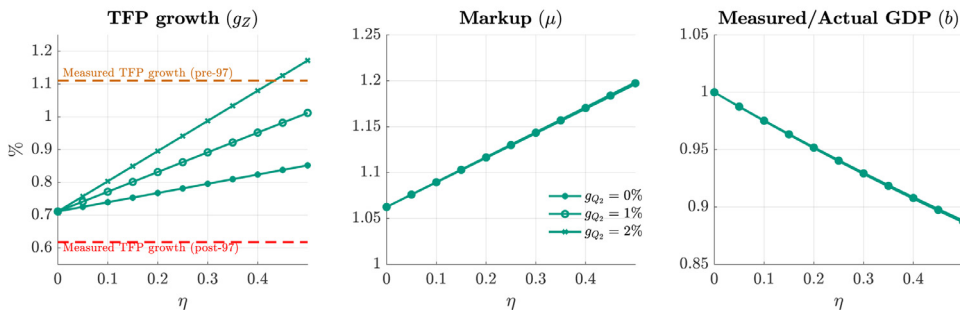
In the application below, for true TFP growth \tilde{g}_Z , we use the pre-1997 empirical average of the Solow residual, while we use post-1997 averages of other measured variables. Thus, this approach will produce the value of g_{Q_2} necessary for measurement error to entirely account for the observed decline in TFP growth from pre- to post-1997 (assuming that the Solow residual properly measures TFP growth before 1997). Finally, this approach requires calibrating certain parameters; as in the previous section, we use $\sigma = 1, \rho = 0.04$, and $\delta_2 = 0.20$. Moreover, we set $\alpha = 0.32$, the measured capital share before 1997.

¹² See, for instance, Li and Hall (2020) for evidence on the high depreciation rates of intangibles.

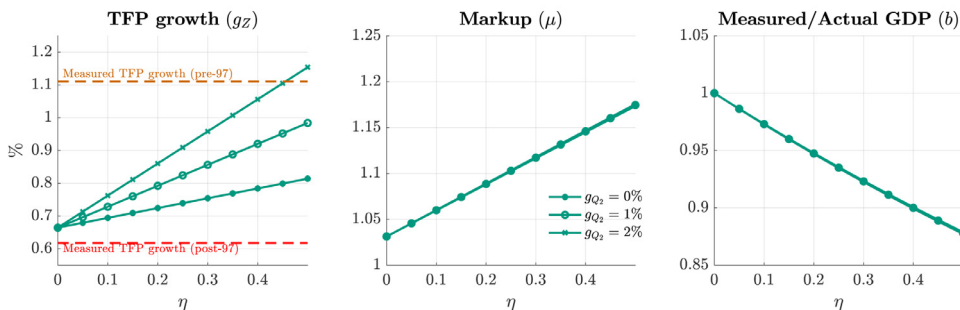
¹³ The corresponding values are given by: $g_Z = \hat{g} - (1 - \alpha)\hat{g}_L - \alpha\hat{g}_K + \alpha\eta(g_{Q_2} - (\hat{g} - \hat{g}_K))$, $\mu = \frac{1-\alpha}{s_L} + \alpha\eta \frac{\hat{g} + \delta_2 - g_{Q_2}}{\rho + \hat{g} + \delta_2 - g_{Q_2}}$ and $b = 1 - \frac{\alpha\eta}{\mu} \frac{\rho + \hat{g} + \delta_2 - g_{Q_2}}{\hat{g} + \delta_2 - g_{Q_2}}$.

¹⁴ The middle and bottom panel report results for higher values of α ; these imply somewhat smaller values for true TFP growth, but also somewhat lower markup values.

Implied moments for $\alpha = 0.32$



Implied moments for $\alpha = 0.34$



Implied moments for $\alpha = 0.36$

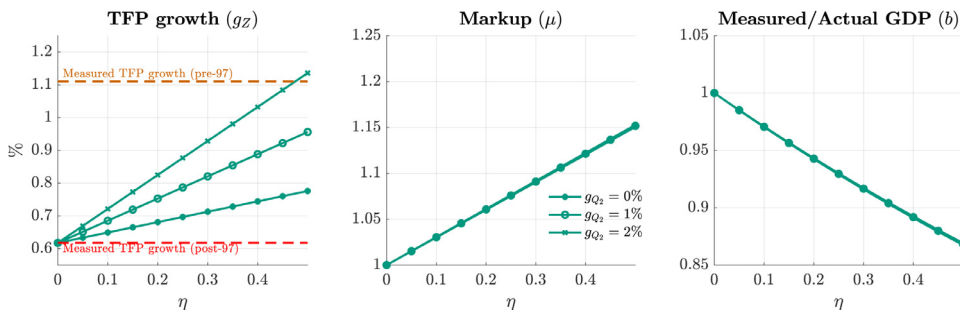


Fig. 2. Numerical examples from the balanced growth model. The top panel corresponds to a calibration with $\alpha = 0.32$, while the middle and bottom panels correspond to $\alpha = 0.34$ and $\alpha = 0.36$, respectively. In each panel, the left graph reports the true value of productivity growth g_z required for the balanced growth model to match measured average values of output growth \hat{g} , labor growth \hat{g}_L , measured capital growth \hat{g}_K , and the labor share \hat{s}_L , in the post-97 sample, as a function of η , the Cobb–Douglas share of omitted intangibles. Implied TFP growth g_z is reported for different values of the growth rate of omitted capital prices, g_{Q_2} (the different green lines). The dashed red line is the average simple Solow residual post-97, while the dashed orange line is the average simple Solow residual pre-97. The middle and right graphs of each panel report the implied markups μ and share of measured to actual capital b . In these latter two graphs, the three distinct lines, corresponding to the different levels of g_{Q_2} , are not visible because they overlap. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

Second approach: adjusting Solow residuals First, given a measure of expenditures M on a particular intermediate commodity or service, we again define \hat{b} as in Equation (18). Next, we obtain an empirical proxy for \hat{g}_{Q_2} . Finally, we use the relationships implied by the balanced growth model in order to compute the value of η , the Cobb–Douglas intangible share, μ , the markup, and g_z , true TFP growth, that are consistent with measured values of output growth \hat{g} , labor growth \hat{g}_L , capital growth \hat{g}_K , and the labor share \hat{s}_L .¹⁵ Intuitively, this approach computes an “adjusted” Solow residual that correctly measures TFP growth in the model, while also ensuring that the model matches the empirical value of the simple Solow

¹⁵ These are given by $\eta = \frac{1-\hat{b}}{\hat{s}_L} \frac{1-\alpha}{\alpha} \frac{\hat{r} + \delta_2 - \hat{g}_{Q_2}}{\hat{g} + \delta_2 - \hat{g}_{Q_2}}$, $\mu = \frac{1-\alpha}{\hat{b}\hat{s}_L}$, and $g_z = \hat{g} - (1-\alpha)\hat{g}_L - \alpha\hat{g}_K + \alpha\eta(\hat{g}_{Q_2} - (\hat{g} - \hat{g}_K))$.

residual \hat{g}_Z . We can then assess whether the “adjusted” Solow residual, g_Z , fell less than the simple Solow residual \hat{g}_Z after 1997. The difference is a measure of the bias introduced by intangibles and markups in the measurement of TFP growth.¹⁶

3.2. Data sources

Our data comes from two main sources. First, we use the benchmark Input-Output accounts (Lawson et al., 2002) to measure intermediate expenditures of different types of commodities and services.¹⁷ This data covers the 1997–2018 period. We use more specifically the Commodity Use tables, aggregated at the Summary level, which provides detail for 61 different commodities and services, after excluding non-comparable imports, used and second-hand goods, and government-provided services and commodities. In each year and for each commodity or service, we collapse the amount used as intermediate input (as opposed to final product) across all industries. This provides a measure of M ; we then compute the associated ratio of measured to adjusted GDP, \hat{b} , as in Equation (18).¹⁸

Second, we obtain information on prices from the GDP-by-industry tables.¹⁹ These data provide annual measures of gross output, intermediate input use, and value added, at the industry level, for the period 1997–2018, along with associated price deflators. Industries in this data follow an identical classification as the 61 groups of commodities and services described in the Input-Output tables, so that industry price deflators can be merged to the Input-Output account data on commodities and services.²⁰ For each commodity and service, we then compute $\hat{g}_{Q_2} = \hat{g}_{Q_2^{nom}} - \hat{g}_{PCE}$, where \hat{g}_{PCE} is the annual change in the implicit deflator for personal consumption expenditure.²¹

The data sources on expenditures and prices overlap on both their time and commodity/service coverage, but they are limited to the 1997–2018 period. In Section 3.3.3 below, we extend our analysis to the pre-1997 period, using the historical Input-Output accounts for the 1947–1962 and 1962–1996 periods. Other data sources are described in Appendix A.2.3.

3.3. Results

This section discusses the results from our two empirical approaches.

3.3.1. First approach: Computing required relative price growth

The magnitude of GDP adjustments Table 2 reports the time-series averages of the ratios of unadjusted to adjusted GDP, \hat{b} , defined as in Equation (18). The averages reported are computed when intermediate use of a single commodity or service group (among the 61 reported in the Use table) is reclassified as intangible investment in isolation. Among the groups with the 10 largest adjustments, 3 service groups are of particular interest.

The largest adjustment is associated with the Professional, Scientific and Technical Services (PSTS) group. Reclassifying intermediate expenditures on these services as intangible investment implies that actual GDP is approximately 6% larger than measured GDP. This group comprises service activities that can be purchased externally by firms, such as accounting, consulting, design, or computer services. The two other service groups of interest are Administrative and Support Services, and Management of Companies and Enterprises. The former group measures the use of outsourced business support services (such as personnel administration and training). The latter group measures the service output of establishments that administer other establishments in a company.²²

Our core argument is that intermediate expenditures on these types of services could in fact represent purchases of investment goods by firms, which would then be misclassified in national accounts. The type of capital created by these purchases is intangible, in that it does not have a physical presence. Indeed, these purchases could lead to the accumulation of various forms of organization capital (through consulting, advertising, design, management and personnel-related services), none of which are embodied in physical assets. These expenditures lead to capital accumulation to the extent that the corresponding inputs are not used up in production entirely within the year of their purchase.

Taken together, omitting these forms of investment could have large effects on GDP. The first column of Table 3 shows that reclassifying the three service groups mentioned above leads to a cumulative adjustment in the level of GDP in the order of 11%. Accordingly, investment rates adjusted for these omissions are higher than, and diverging from, measured investment rates. Fig. 3 reports the time series for both the ratio of unadjusted to adjusted GDP, and for the implied ratio

¹⁶ As for the first methodology, this approach requires calibrating the values of $(\sigma, \rho, \delta_2, \alpha)$; we use the same values as reported above.

¹⁷ The data are available at apps.bea.gov/industry/iTables20Static20Files/AllTablesSUP.zip. These data were produced following the 2018 comprehensive update of the Industry Economic accounts (Howells et al., 2018).

¹⁸ We adjust our basic output measure, total final product use across all commodities, by subtracting imports from the Commodity Supply tables at the same level of disaggregation; the resulting measure matches, by construction, total value added.

¹⁹ The data are available at apps.bea.gov/industry/iTables20Static20Files/AllTables.zip.

²⁰ The tables provide price indices for more a disaggregated industry classification, but we only use the data at the same level of aggregation as the Input-Output accounts.

²¹ The GDP-by-industry tables also provide price deflators for gross output, which have similar signs, on average, than value added deflators, but are somewhat smaller in magnitude. From the standpoint of the model, value added deflators should be used, and so we focus on this measure for the remainder of the results.

²² These establishments are likely to be headquarters or core firm locations where organization and strategic planning services are produced. The output of these establishments is reported in isolation in the benchmark IO accounts.

Table 1

Solow residuals before and after 1997. The Solow residual is constructed as $\hat{g}_Z = \hat{g} - \hat{s}_L \hat{g}_L - (1 - \hat{s}_L) \hat{g}_K$, where \hat{g} is the average growth rate of output in consumption units (defined as nominal business value added divided by the deflator for personal consumption expenditures), \hat{s}_L is the average measured labor income share, \hat{g}_L is the average growth rate of labor input, and \hat{g}_K is the average growth rate of capital input. Utilization-adjusted TFP growth is constructed as $\hat{g}_Z = \hat{g} - \hat{s}_L \hat{g}_L - (1 - \hat{s}_L) \hat{g}_K - \hat{g}_u$, where \hat{g}_u is the average growth rate of utilization. Input and utilization data are from the Fernald (2014) quarterly dataset; more detail on the measurement of the growth rate of output in consumption units is reported in Appendix A.2.1.

	1947–1996	1997–2018	Change
GDP growth (p.p.)	3.36	2.44	−0.92
Labor growth (p.p.)	1.52	0.98	−0.54
Capital growth (p.p.)	3.80	3.32	−0.48
Labor share of income	0.68	0.64	−0.04
TFP growth (p.p.)	1.11	0.62	−0.49
TFP growth (utilization-adjusted; p.p.)	1.13	0.66	−0.47

Table 2

Intermediate commodities or services producing the largest GDP adjustments. The table reports the 10 commodity or service groups with the smallest value of unadjusted GDP to adjusted GDP, where the latter is computed using data from the Use tables of the benchmark Input-Output accounts. For each commodity or service, the first column is the average value of $\hat{b}_t = P_t Y_t / (P_t Y_t + M_t)$, where $P_t Y_t$ is total GDP at producer prices, and M_t is the nominal value of intermediate input use of the commodity or service. The average is computed over the 1997–2018 period, for each commodity or service group. The second column reports average values for the relative price growth of omitted capital, computed using price deflators from the GDP-by-industry tables, as described in Section 3.2. The third column is the share of the commodity or service in total GDP. We compute the contribution of each commodity to GDP by using the final expenditure data by commodity provided in the Use tables, and subtracting imports of the commodity or service, the latter obtained from the Supply tables. Total GDP is the sum of GDP across all goods and services. The contribution of oil and gas extraction is negative because in many sample years, imports are larger than total domestic use for that commodity. The top panel reports services, while the bottom panel reports commodities. Intermediate services the purchases of which plausibly represents omitted intangible investment are highlighted in bold.

	\hat{b}	\hat{g}_{Q_z} (%)	GDPshare (%)
<u>Services</u>			
Professional, scientific, and technical services	0.940	0.59	3.63
Other real estate	0.952	−1.75	0.77
Administrative and support services	0.964	0.20	0.31
Insurance carriers and related activities	0.972	−0.21	1.84
Credit intermediation and related activities	0.973	1.06	1.42
Management of companies and enterprises	0.974	1.54	0.02
<u>Commodities</u>			
Chemical products	0.962	1.31	2.67
Oil and gas extraction	0.972	2.09	−1.25
Petroleum and coal products	0.973	3.78	1.89
Food and beverage and tobacco products	0.976	1.12	5.55

Table 3

Required rate of growth of relative prices, g_{Q_z} , in order to fully account for the post-1997 decline in measured TFP growth. These results are constructed using the first approach described in Section 3.1, which only uses data on intermediate expenditures on commodities or services. The first column reports the average ratio of unadjusted GDP to GDP adjusted for omitted intangible investment, \hat{b} , defined as in Equation (18). The second column reports the rate of relative price growth g_{Q_z} , which would be necessary for measurement bias to account for the entirety of the decline in measured TFP growth after 1997, while the third and fourth columns report the Cobb-Douglas share of omitted intangible capital η and the implied level of markups μ . Each line reports the results when a different set of intermediate service expenditures are reclassified as intangible investment. See Section 3.1 for more details on the methodology used to construct g_{Q_z} , η and μ .

Service groups included	Average, 1997–2018			
	\hat{b}	g_{Q_z} (%)	η	μ
Professional serv.	0.94	2.08	0.25	1.13
Professional serv. + Management	0.92	1.21	0.36	1.15
Professional serv. + Management + Administrative serv.	0.89	0.60	0.50	1.19
Organization Capital (Compustat)	0.91	1.05	0.39	1.16

of nominal investment to GDP after adjusting for omitted intangibles. For instance, adjusting for Professional Services leads to an upward revision of approximately 5% in the ratio of nominal investment to nominal GDP.²³

For reference, Table 2 also reports the adjustment factor \hat{b} implied by reclassifying seven other commodities and service groups (those remaining among the 10 groups with the largest GDP adjustments). However, it is difficult to argue that these inputs represent misclassified investment; Chemical Products, for instance, tend to be used up in production within the year of their purchase. Hence, not all intermediates are candidates to be capitalized, in particular if they are clearly used as materials inputs.

Finally, *own-account* investment in organization capital, for instance through worker training, or branding and marketing expenses, could also contribute to the stock of organization capital. The distinction between externally purchased and own-account intangible investment is moot in our model because we assume away internal capital adjustment costs. However, in the Use tables, only externally purchased intangibles will be captured. (This is with the exception of one important component of own-account spending on organization capital, managerial compensation, which is isolated in the Use table as intermediate inputs purchased from the Management of Companies and Enterprises sector, and will therefore be captured by our baseline approach.) In Section 3.4 and Appendix A.2.4, we use firm-level data on organization capital spending that includes own-account investment, and show that the magnitudes we obtain for the adjustments to GDP are in the upper range of those implied by the Use tables.

Results Using these GDP adjustments, Table 3 then reports the values of relative price growth of omitted capital, g_{O_2} , that would be required to explain the *entirety* of the decline in measured TFP growth from bias generated by intangibles and markups. The implied relative price growth ranges from 0.6 to 2.1% p.a., with lower estimates corresponding to more intermediate expenditures being reclassified as investment.

Two points are worth noting. First, the required relative price growth is positive; that is, the price of omitted capital must be rising, relative to the price of final goods, in order for the bias to be positive, as discussed in Section 2. In Section 3.3.1, we argue that, for the three service groups we focus on, this is empirically plausible. Second, these adjustment lead to high markups. For instance, when adjusting for the PSTS group, the implied value-added markup corresponds to a pure profit share of value added in the order of 11.5%. As highlighted in the previous section, in order to simultaneously accommodate a low labor share \hat{s}_l and a substantial underestimation of GDP, markups must be elevated.

3.3.2. Second approach: Adjusting solow residuals

Relative price growth in the data Are relative price growth rates for omitted intangibles in the order of 0.6% to 2.1% realistic? The second column of Table 2 reports average price growth rates for the 10 commodities or service groups with the 10 largest GDP adjustments. For the three key service groups discussed above and highlighted in Table 2, our empirical proxies for \hat{g}_{O_2} are all positive. However, their magnitudes are not as large as the values discussed in the previous section: the highest rate of relative price increase is 1.5% per year, for Management Services. Thus the bias generated will not be sufficient to fully explain the decline in measured TFP growth. So we next discuss *how much* of this decline our mechanism can account for, given these proxies for \hat{g}_{O_2} .

Results Fig. 4 reports the implied rate of growth of TFP (as well as a red line indicating the average simple Solow residual \hat{g}_z the post-1997 sample) when adjusting for the 61 commodity and service groups individually. Adjustments of individual service or commodities groups have a positive, though relatively small overall effect on measured TFP growth. Among the largest adjustments is obtained for the PSTS group; alone, it adds approximately 0.1% to overall TFP growth, or 1/5th of the gap between pre- and post- 1997 TFP growth.²⁴

Table 4 reports the implied growth rates, Cobb-Douglas intangible shares, and markups, when adjusting for the three key groups of services highlighted earlier in the discussion. The first two lines report the unadjusted Solow residual for the pre- and post-1997 periods; as highlighted in the introduction, it declines by 49bps, from 1.11% to 0.62% per year.

The third line reports the average growth rate of TFP obtained when adjusting only for markups, but not for omitted intangibles. The adjustment for markups alone raises measured TFP growth by approximately 9bps, or one-fifth of the decline. The remaining lines report TFP growth in the post-1997 sample when adjusted for both markups and omitted intangibles. Altogether, the decline is 33bps (or 67%) smaller after adjusting for both markups and intangibles produced by all three key sectors highlighted above. Thus markups and intangibles together can account for 2/3 of the observed decline in TFP growth.²⁵ Adjusting only for professional services, or for professional services plus management, yields somewhat lower effects from one-third to one-half of the total decline in measured TFP growth.

²³ In anticipation of the analysis of Section 3.3.3, this figure reports the times series for these ratios for the entire postwar era, 1947–2018. The ratios of unadjusted to adjusted GDP reported in the top panel of Fig. 3 differ somewhat from those used in this section because the industry classification of the Input-Output accounts changed in 1963 and 1997, as explained in Section 3.3.3. Appendix Figure A2 reports the time series for the same moments from 1997 to 2018 only, using definitions of the omitted intangibles based on the more granular classifications of the post-1997 IO tables.

²⁴ In Fig. 4, it is also worth briefly highlighting the Petroleum and Coal Products commodity group. As a widely used intermediate input, it has a low value of \hat{b} . Additionally, as indicated by Table 2, this group experienced a high rate of relative price increase over the period. As result, reclassifying intermediate expenditures on this group as purchases of capital goods would lead to a large upward adjustment to TFP growth. However, as argued before, these are typically used up in production within the year, which rules out reclassifying them as omitted capital goods.

²⁵ Appendix Figure A3 reports the annual time-series underlying the averages of Table 4. These time-series show that the adjustment for omitted intangibles produces a sizable upward revision of TFP growth in two periods: the early2000/s, and the Great Recession. In particular, during the Great Recession, the difference between measured and adjusted TFP growth is almost a full percentage point.

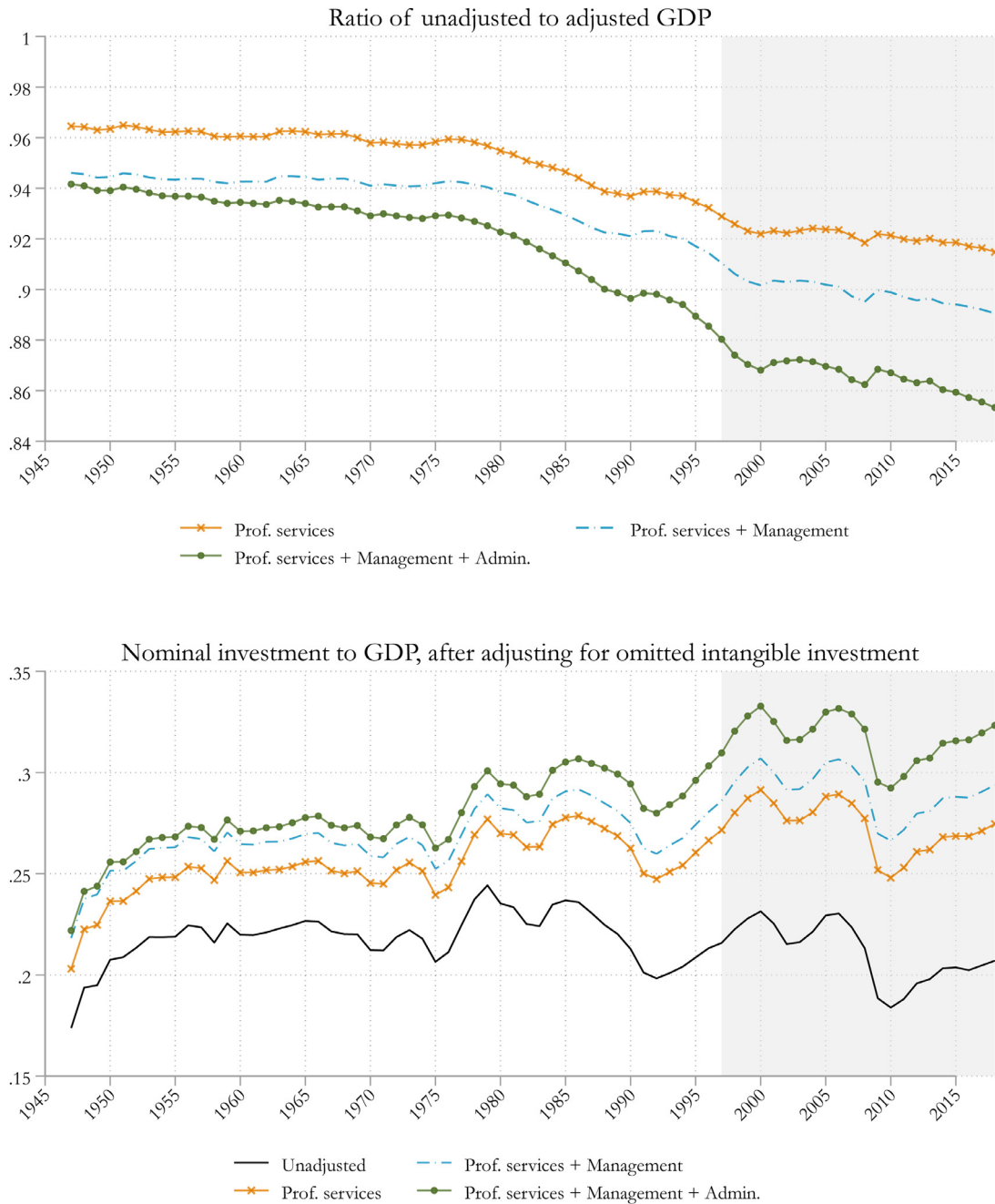


Fig. 3. Time series for the ratio of unadjusted GDP to GDP adjusted for omitted intangibles (top panel), and for the ratio of investment to GDP without and with adjustments for omitted intangibles (bottom panel), for the 1947–2018 period. The 1997–2018 period is highlighted in grey. The top panel reports the time series for $\hat{b}_t = P_t Y_t / (P_t Y_t + M_t)$, where $P_t Y_t$ is nominal GDP, and M_t is the nominal value of intermediate input use of a group of services, where the latter is obtained from the Use tables of the benchmark Input-Output accounts. Each line corresponds to the ratio obtained when treating a different group of services as misclassified intangible investment. The bottom panel reports the time series $\hat{I}_t = (Q_t I_t + M_t) / (P_t Y_t + M_t)$, where $Q_t I_t$ is measured aggregate spending on investment goods, also obtained from the Input-Output accounts. Appendix Figure A2 reports the time series for the same moments from 1997 to 2018 only, using definitions of the omitted intangibles based on the more granular classifications of the post-1997 input/output tables.

3.3.3. Comparing pre- and post-1997 data

The previous section shows that measurement bias from markups and intangible capital can explain up to two thirds of the decline in the Solow residual. It is however possible that the Solow residual before 1997 also requires upward adjustments because of markups and intangibles. More generally, since the rise in intangible capital and markups are thought to have accelerated after the 1990s, comparing the pre- to post-1997 data provides a “placebo” test for our hypothesis that both trends have contributed to an increase in the mismeasurement of TFP growth.

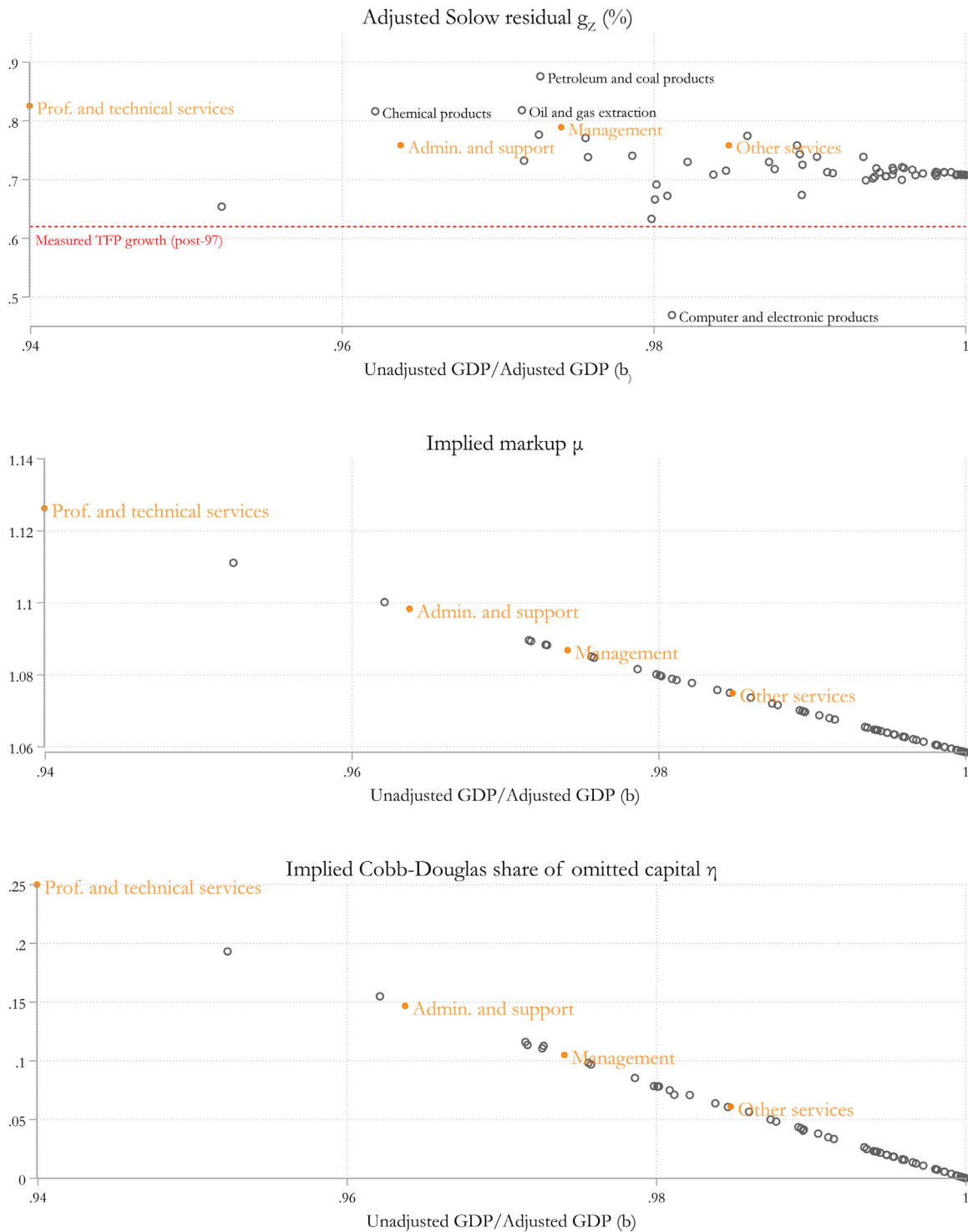


Fig. 4. Implied moments when adjusting for individual commodity or sector groups. The moments in each panel are computed using second of the two approaches described in Section 3.1, applied to individual commodity or service groups among the 61 reported in the Input-Output tables. The top panel reports TFP growth adjusted for both intangibles and markups, the middle panel reports the implied markup, and the bottom panel reports the implied Cobb-Douglas share of omitted intangible capital in the production function. Key service sectors are highlighted in orange.

Table 4

TFP growth, after adjusting for omitted intangibles and for markups. The first line reports TFP growth estimated using a model without markups and without omitted capital on the 1947–1996 data; the simple Solow residual is, in that case, a correct measure of GDP. The second line reports the simple Solow residual in the post-1997 sample. The third line reports TFP growth adjusted for markups, and the third to sixth lines report measured TFP growth after adjusting for both markups and omitted intangibles. The adjustments are made following the second of the two approaches described in Section 3.1, which uses data on both expenditures and prices. GDP adjustments, \hat{b} , are reported in the first column, and relative price growth rates, g_{Qz} , are reported in the third column.

	\hat{b}	\hat{g}_{Qz} (%)	g_z (%)	μ	η
1947–1996	0	0	1.11	1.00	0
1997–2018					
No adjustment, no markups	0	0	0.62	1.00	0
No adjustment, markups	0	0	0.71	1.06	0
Adjusted for Prof. services	0.94	0.59	0.83	1.13	0.25
Adjusted for Prof. services + Manag.	0.92	0.78	0.90	1.15	0.35
Adjusted for Prof. services + Manag. + Admin.	0.89	0.65	0.95	1.19	0.50
Adjusted for Organization capital (Compustat)	0.91	0.78	0.91	1.16	0.38

The first empirical challenge in doing so is that the service and commodity groups used in the Input-Output tables change twice before 1997. More specifically, the 1947–1962 Input-Output tables have a substantially coarser definition of service and commodity groups.²⁶ Given this limitation, we aggregate up service and commodity groups in the 1963–1996 and 1997–2018 data so that they match the 43 groups of the 1947–1962 data. Table 5 then reports the magnitude of these GDP adjustments, both before and after 1997.

The top panel of Table 5 shows that omitted intangibles would have led to adjustments to the level of GDP even before 1997.²⁷ However, the adjustment is substantially larger in the post-1997 period. The last two columns of the top panel of Table 5 report the change in \hat{b} for each group; it is generally negative, with t -tests confirming that the drop is statistically significant. The bottom panel of Table 5 repeats these computations, using aggregates of the three service groups most likely to represent misclassified intangible investment and discussed in the previous section. Taken together, the ratio of unadjusted to adjusted GDP for these three service groups is 0.92 pre-1997, but falls to 0.87, after 1997.

Nevertheless, the fact that $\hat{b} < 1$ even before 1997 means that one should, in principle, adjust the Solow residual also before 1997. In order to do so, as discussed in the previous section, data on the growth rate of relative prices of omitted intangibles is required. However, the second empirical challenge is that there are, to our knowledge, no price deflators available, at the required level of aggregation, for the 1947–1996 period.²⁸ We therefore assume that relative price growth is the same as in the post-1997 period.

The adjusted Solow residuals which we obtain are reported in Table 6. With all three key service sectors accounted for, the pre-1997 Solow residual is 1.21% p.a., versus 1.11% in the baseline. Crucially, this upward adjustment is smaller than the upward adjustment for the post-1997 sample.²⁹ Thus after adjusting for markups and intangibles in both the pre- and post-1997 periods, the Solow residual only fell by approximately 21bps after 1997, instead of an unadjusted decline of 49bps, confirming our baseline findings.

3.4. Robustness

Appendix A.2.4 reports results from four robustness checks. First, our results also hold using BLS price data. Second, the magnitude of the adjustments for omitted intangibles obtained from firm data (potentially including own-account intangible investment) is similar to that obtained from the Input-Output tables. Third, later breakpoints weaken our results somewhat, because the price of omitted intangibles grew more slowly (relative to the PCE deflator) in the 2004–2007 period. However, even with a 2004 breakpoint, our mechanism still explains one-third of the decline in the Solow residual. Finally, our results are robust to using alternative values for the depreciation rate of omitted intangibles, δ_2 .

²⁶ There are 43 groups in the 1947–1962 tables, instead of 60 in the 1963–1996 tables and 61 in the 1997–2018 tables. The historical Input-Output tables we use in the analysis are available at https://apps.bea.gov/industry/xls/io-annual/IOUse_Before_Redefinitions_PRO_1947-1962_Summary.xlsx and https://apps.bea.gov/industry/xls/io-annual/IOUse_Before_Redefinitions_PRO_1963-1996_Summary.xlsx, respectively. In particular, the service groups most likely to include omitted intangible investment after 1997 are not consistently defined across periods. For instance, prior to 1997, the Administrative and Support Services group is included in a larger group, which also contains Waste Management services.

²⁷ The GDP adjustments in this exercise after 1997 are mechanically large than in our previous exercise, because of the coarser definitions of commodity and service groups which we are constrained to use.

²⁸ The historical GDP by industry tables, available at https://apps.bea.gov/industry/xls/GDPbyInd_VA_SIC.xls, do not include price deflators. The Gross Output by industry tables, available at https://apps.bea.gov/industry/xls/GDPbyInd_GO_SIC.xls, report price deflators, but only for the 1977–1997 period, and with a different industry classification (that does not adequately cover service groups) relative to the input-output accounts.

²⁹ Adjusted TFP growth for the post-1997 sample is, itself, higher than in Table 3, because the estimates of \hat{b} obtained using the coarser industry classification are higher than in our baseline analysis.

Table 5

Change in GDP adjustment between 1947–1996 and 1997–2018, for the 10 commodity and service groups with the largest GDP adjustments after 1997. The top panel of the table reports the 10 commodity of service groups with the smallest value of unadjusted GDP to adjusted GDP for the 1997–2018 period. The data are from the Use tables of the benchmark Input-Output accounts. For each period and each commodity or service, the first column is the average value of $\hat{b}_t = P_t Y_t / (P_t Y_t + M_t)$, where $P_t Y_t$ is nominal GDP, and M_t is the nominal value of intermediate input use of the commodity or service. Averages are computed over the 1947–1996 and 1997–2018 periods, respectively. The definition of the groups differs from Table 2 because the industry classification of the Input-Output accounts changed in 1963 and in 1997; see main text for details. The last column of the table reports the change in the adjustment ratio \hat{b} across periods, and the t -statistic for the one-sided t -test on the difference of means across the two samples. The bottom panel of the table reports similar moments, computed for the aggregated service sectors highlighted in the top panel of the table, and where purchases of intangible capital goods is most likely to be misclassified as expenditure on intermediate inputs.

	\hat{b} (average)		$\Delta \hat{b}$	t -stat
	1947–1996	1997–2018		
<u>Services</u>				
Prof., scient. & techn. services	0.955	0.921	−0.033***	−15.40
Finance and Insurance	0.957	0.929	−0.028***	−13.72
Real estate	0.973	0.952	−0.021***	−13.15
Admin. and waste services	0.984	0.959	−0.025***	−13.84
Information	0.979	0.967	−0.013***	−9.89
Management of companies	0.981	0.974	−0.007***	−17.60
<u>Commodities</u>				
Chemical products	0.966	0.962	−0.004***	−9.89
Oil and gas extraction	0.978	0.972	−0.007**	−2.78
Petroleum and coal products	0.980	0.973	−0.007***	−3.48
Food, beverage, tobacco	0.956	0.976	0.020***	6.07
All commodities and services	0.982	0.983	0.001	1.25
* : $p < 0.05$, ** : $p < 0.01$, *** : $p < 0.001$.				
	\hat{b} (average)		$\Delta \hat{b}$	t -stat
	1947–1996	1997–2018		
Prof. services	0.955	0.921	−0.033***	−15.40
Prof. services + Manag.	0.937	0.899	−0.038***	−18.11
Prof. services + Manag. + Admin.	0.924	0.866	−0.057***	−16.23
* : $p < 0.05$, ** : $p < 0.01$, *** : $p < 0.001$.				

Table 6

Change in implied moments, between 1947–1996 and 1997–2018, after adjusting for the bias induced by markups and omitted intangible investment. The columns marked “1947–1996” report adjusted moments for the 1947–1996 period, while the columns marked “1997–2018” report adjusted moments for the 1997–2018 period. The last column reports the implied change in the rate of growth of TFP. The line marked “No adjustment, no markup” uses a model with no markups and no intangibles; the line marked “No adjustment, markup” uses a model with no intangibles but positive markups; and the remaining lines adjust for both omitted intangibles and markups, using different service groups to measure omitted intangible investment.

	1997–2018				1947–1996				Δg_Z (%)
	\hat{g}_{Q_2} (%)	g_Z (%)	μ	η	\hat{g}_{Q_2} (%)	g_Z (%)	μ	η	
No adj., no markups	0	0.620	1.00	0	0	1.107	1.00	0.00	−0.487
No adj., markups	0	0.708	1.06	0	0	1.106	1.00	0.00	−0.398
Prof. serv.	0.59	0.866	1.15	0.33	0.59	1.164	1.05	0.17	−0.298
Prof. serv.+Manag.	0.78	0.942	1.18	0.44	0.78	1.202	1.07	0.25	−0.261
Prof. serv.+Manag.+Admin.	0.65	1.004	1.22	0.60	0.65	1.212	1.08	0.30	−0.208

4. Conclusion

A recent literature has argued that the recent decline in the rate of economic growth in the US is attributable to a decline in TFP growth (Cette et al., 2016; Fernald et al., 2017; Gordon, 2016). In this paper, we have studied whether this decline in measured TFP growth could reflect measurement bias caused by a simultaneous rise in rents (Barkai, 2020) and a rise in the importance of firms' use of intangible capital, which may not be properly measured (Corrado et al., 2009), Crouzet and Eberly.

If the price of omitted intangible capital is rising sufficiently fast, an upward bias in measured capital growth (and therefore, a downward bias in measured TFP growth) can occur. However, such mismeasurement would also imply that the level of measured GDP is biased downward, by an amount equal to the flow of intangible investment. This, in turn, would

tend to generate a rising measured labor share, at odds with the data. Rising markups, in tandem with rising intangibles, can offset this force and allow simultaneously for a downward bias in measured TFP growth and a declining labor share. We articulated this argument more precisely in a balanced growth model featuring both intangibles and markups, and showed, using the input-output tables, that this mechanism could plausibly account for one to two-thirds of the decline in measured TFP growth.

Our results do not imply that the rate of growth of output is mismeasured. Rather, they attribute some of this decline to rising relative prices of certain forms of intangible capital. A difficult but worthwhile question is why these forms of intangible capital have become relatively more expensive. Additionally, outside of the balanced growth path, omitted intangibles may bias the measured growth rate of GDP, further exacerbating TFP growth biases. Finally, our balanced growth analysis assumes Cobb-Douglas substitutability between labor and capital, but deviations from this assumption may accentuate the wedge between the measured labor share and the output elasticity of labor, and amplifying measurement bias. We leave these questions to future research.

Transparency declaration

This article is part of a Conference Proceedings Supplement sponsored by the Study Center Gerzensee and Swiss National Bank.

Supplementary material

Supplementary material associated with this article can be found, in the online version, at doi:[10.1016/j.jmoneco.2021.09.005](https://doi.org/10.1016/j.jmoneco.2021.09.005).

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