

# 53. Interprocedural Abstract Interpretation with PAG

Prof. Dr. rer. nat. Uwe Aßmann  
Institut für Software- und  
Multimediatechnik  
Lehrstuhl Softwaretechnologie  
Fakultät für Informatik  
TU Dresden  
<http://st.inf.tu-dresden.de>  
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- 1) Interprocedural analysis
- 2) Ab.I. with PAG

## Obligatory Literature

- ▶ Alt, Martin, Martin, Florian, Generation of efficient interprocedural analyzers with PAG. In: Mycroft, Alan, Static Analysis. Lecture Notes in Computer Science, 1995. Springer Berlin / Heidelberg  
" <http://www.springerlink.com/content/y583778583740462/>
- ▶ Martin, Florian. PAG – an efficient program analyzer generator. International Journal on Software Tools for Technology Transfer (STTT), Volume 2, Number 1, 46-67, DOI: 10.1007/s100090050017, Special section on program analysis tools  
" <http://www.springerlink.com/content/1pb55yv4mq4emywl/>
- ▶ Auch Technischer Bericht der U Saarbrücken:  
" <http://scidok.sulb.uni-saarland.de/volltexte/2004/203/>

## Ressources

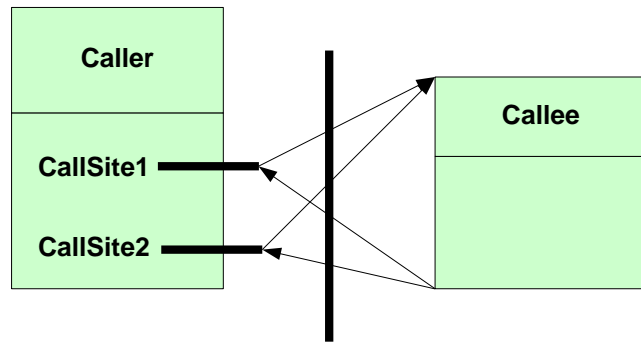
- ▶ F. Martin. PAG - an efficient program analyser generator. Software Tools for Technology Transfer STTT 1998, 2:46-67, Springer
- ▶ [www.absint.de](http://www.absint.de) (also aiSee)
- ▶ [www.cs.uni-sb.de/~martin/pag](http://www.cs.uni-sb.de/~martin/pag)
- ▶ F. Martin Generating Program Analyzers. PhD Thesis. Universität Saarbrücken.
- ▶ Martin Trapp. Optimierung Objekt-Orientierter Programme. Springer Verlag, Heidelberg, January 2001.
- ▶ Ole Agesen, Jens Palsberg, and Michael I. Schwartzbach. Type inference of SELF. In Oscar Nierstrasz, editor, ECOOP'93-Object-Oriented Programming, 7th European Conference, volume 707 of Lecture Notes in Computer Science, pages 247-267, Kaiserslautern, Germany, 26-30 July 1993. Springer.

## 53.1 Different Approaches to Interprocedural Analysis

- Abstract interpreters can treat calls in different ways.
- From ignoring and summarizing them, to expanding them or lazily expanding them.

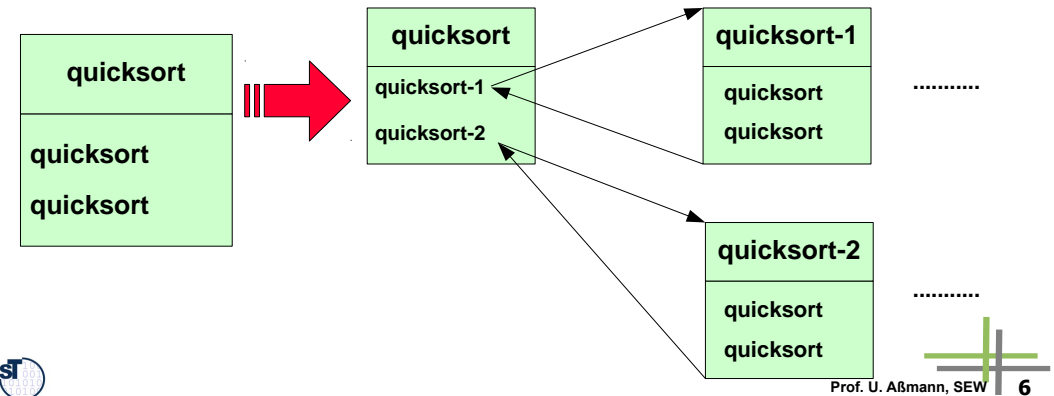
## Invalidating Approach to Abstract Interpretation (Worst-Case Assumption)

- ▶ During the abstract interpretation, all information is invalidated by a call
  - " After the call, worst case value is assumed (top of lattice)
  - " Every procedure is analyzed in isolation
- ▶ Conservative (know nothing about calls)
- ▶ Improvement:
  - " Invalidate everything that might be written by the callee
  - " However then alias analysis must run before



## The Cloning/Inlining Approach to Abstract Interpretation

- ▶ **Inlining abstract interpretation (interprocedural analysis)** copies a procedure's body for every call and propagate information separately in body (builds up a interprocedural control flow graph, ICFG)
- ▶ Corresponds to *inlining* into every callee
- ▶ Leads to bloat of code and analysis information
  - Is space-exponential in nesting depth of call graph



## The Functional Approach to Abstract Interpretation

- ▶ Also called *effect calculation approach*
- ▶ **Functional interprocedural analysis** calculates a function/effect  $E_f$  for every procedure  $f$ 
  - " Which is applied to the current input values at a caller to receive the output values after the call
    - Parametric execution with an "abstract" function  $E_f$
- ▶  $E_f$  is stored in a table, mapping abstract input value to abstract output value (i.e., an associative array of abstract values)
- ▶ Whenever the analysis reaches the callee, the current abstract input value is looked up
  - " If found, reuse output value
  - " Otherwise reanalyze body

## The $k$ -Call Context Approach to Abstract Interpretation

- ▶ The  **$k$ -contextual interprocedural analysis** maintains the calling context with a limited stack of depth  $k$ 
  - Also called  *$k$ -call string approach*
  - The call history of the called procedure is incorporated in the underlying lattice  $D$  (*call strings*)
- ▶ Different bodies at different call sites are distinguished by the call strings
  - In case of  $k=1$  all call sites are distinguished
  - $K=2$  all call sites, with calling context of callers
  - $K=3$ : all call sites, all calling contexts of the grandfathers
  - ...

## Expanded Supergraphs

- ▶ The analysis information (the abstract values) are replicated for every caller (multiplicity)
  - Procedures are not inlined, but parameter information is replicated
- ▶ Connectors connect the right incarnation of the value to a caller site
- ▶ Example
- ▶  $\text{mult}(n) = 1 \implies$  no call sites are distinguished
- ▶  $\text{mult}(P_i) = k_i$  where  $i$  is number of call sites  $\implies$  call string length 1
- ▶  $\text{mult}(P_i) = k_i * n \implies$  call string length  $n$

## The Lazy Cloning Approach to Abstract Interpretation

- ▶ [Agesen: Type inference for SELF]
- ▶ Idea: do a *lazy cloning (on-demand replication)* of the parameter values
- ▶ During propagation, store all input values of functions analyzed so far
- ▶ If an input value for a function differs from an already memoized one, clone the parameter (i.e., distinguish it)
- ▶ Cloning parameters only
- ▶ Cloning them on demand
- ▶ Cloning can be restricted
  - " Analysis works less precise but costs less memory



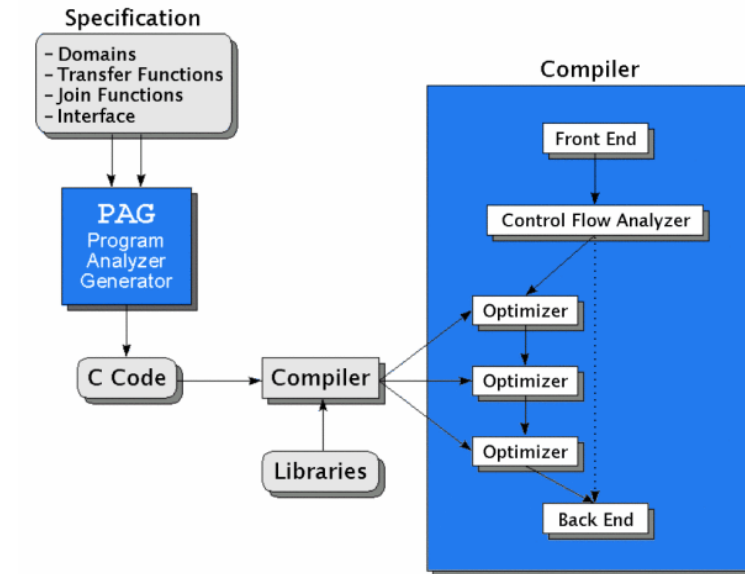
## The Interprocedural Phi-Approach to Abstract Interpretation

- ▶ M. Trapp (Optimization of object oriented programs) introduces interprocedural phi functions (i-phi)
- ▶ i-phis are "small-ifs" or "ifs for one value"
- ▶ Every formal parameter of a procedure gets as input an i-phi
- ▶ The i-phi depends on the control flow condition

## 53.2 Interprocedural Analysis with PAG



- ▶ Intra- and interprocedural analysis
- ▶ Extended super graph for interprocedural case (cloning of parameter information for call sites)
- ▶ Special Languages for:
  - " DDL for the specification of the intermediate program representation
  - " DDL for the Lattice (abstract domains)
  - " Functional language for the abstract interpreter (abstract/flow/transfer functions)



## Node Orderings for Visits during Abstract Interpretation

- ▶ During the interprocedural abstract interpretation, instruction nodes are ordered in the worklist. Different orderings are possible, for which PAG can generate implementations:
  - ▶ DFS: depth-first
  - ▶ BFS: breadth-first
  - ▶ SCC-D: strongly connected components in visit order depth first.
  - ▶ SCC-B: same in breadth first
  - ▶ WTO-D: SCCs, but ordered in weak topological ordering of Bourdoncle. Depth-first.
  - ▶ WTO-B: same, but breadth-first

## PAG-DDL: Data Type Specifications

- ▶ Basic sets
  - " Snum (signed numbers), unum, real, chr, string
- ▶ Basic Lattices
  - " Lsnum (lattice of signed numbers), lunum, bool, a..b, enum
- ▶ Type constructors for lattices
  - " Disjoint sum
  - " Tuple construction \*
  - " Powerset operator
  - " List operator
  - " Function on S1 -> S2

## PAG-DDL: Lattice Specifications

- ▶ Lattice operators
  - flat: Set  $S \rightarrow$  Lattice
  - lift(Lattice L)
  - powerset: Set  $\rightarrow$  Lattice
  - dual(Lattice L)
  - reduce(Lattice E, reduction function f)
- ▶ Tuple space
- ▶ Function space (function lattice)  $S \rightarrow L$ , pointwise ordering

## Example: PAG-DDL for Live Variables Analysis

```
// a simple powerset lattice for signed numbers
GLOBAL
    maxvar: snum
SET
    vars = [0..maxvar]
LATTICE
    varset = set(vars)
    var = lift(varset)
```



## Example: PAG-DDL for Caches

```
GLOBAL
    storeMin: unum
    storeMax: unum
    cacheSize: unum
    aWays: unum<24
SET
    storeLine = [storeMin..storeMax]
    direct= [0..cacheSize]
LATTICE
    cacheLine=[0..aWays]
    age = lift(cacheLine)
    assoc = storeLine -> age
    cache = direct -> assoc
    dfi = cache * cache
```



## Example PAG-DDL for Intervals as Abstract Domain

```
LATTICE
    upperBound = lsnum
    lowerBound = dual(lsnum)
    interv = lowerBound *upperBound
    env = snum -> interv // variables to intervals
    dom = lift(env)
```



## Example PAG-DDL for Heap Analysis

### LATTICE

```
node = set(snum)           // nodes abstract vars
edge = node * snum * node
edges = set(edge)
sedge = snum * node
sedges = set(sedge)
shared = set(node)        // predicate
graph = sedges * edges * shared
dfi = lift(graph)
```

## PAG-DDL: Specification of Program Representation (Metamodel of the Language)

- ▶ Types of the nodes of the CFG can be specified.
  - " Constructor based
  - " With alternatives
- ▶ In general, other DDLs can be employed (e.g., UML)

```
SYNTAX
START: Unlabstat
Unlabstat: M_Assign(var:Var, exp:Exp)
           | M_While(exp:Exp, body:Stat*)
           ...
```



## Specification of Abstract Interpretation Functions

- ▶ Similar to function specification in ML
- ▶ Pattern matching on IR nodes
- ▶ Functions are annotated to control flow graph nodes
  - " Implicit parameter @ for data flow value
  - " Return a value
- ▶ Dynamic Functions (updatable)
  - " Application  $f(\{!x!\})$
  - " Updating of values  $f[n \rightarrow v]$
  - " Constant function  $[->v]$



## Specification of Abstract Interpretation Functions

- ▶ Lattices provide combine functions (merge, joins) for abstract values, when control flow joins
  - least-upper bound lub
  - greatest-lower bound glb
  - comparison relation  $<, >$
- ▶ Operations for latticed and lifted lattices
  - " drop, lift
- ▶ ZF Zermelo-Fränkel Set Expressions:
  - ▶  $[x !! x \leftarrow \text{set}, \text{if } x \geq 0]$



## Example: Analysis of a While Loop

```
// Source code expression:
// while(id <=exp)
// 1) pattern matching of the expression
M_While(M_Binop(M_op_leq(),
               M_Var_exp(M_simpl_var(id)),
               exp),_)
      ,true_edge):
// 2) the abstract interpretation function
let f <= @; // assignment of f to implicit data flow value
    id = val-Identifler(id);
in
    let erg = f{!id!} glb (top,(eval(exp,f))!2);
    in if is_ok(erg) then lift(f\[id->erg])=
        else bot;
    endif;
```

## Other Parts of the Specification

- ▶ Direction specification: forward/backward
- ▶ Carrier graph: control-flow graph
- ▶ Init value: default initialization of values
- ▶ Init\_start: init value of start node
- ▶ Equal: equality test for fixpoint detection
- ▶ Widening function
- ▶ Narrowing function



## Example

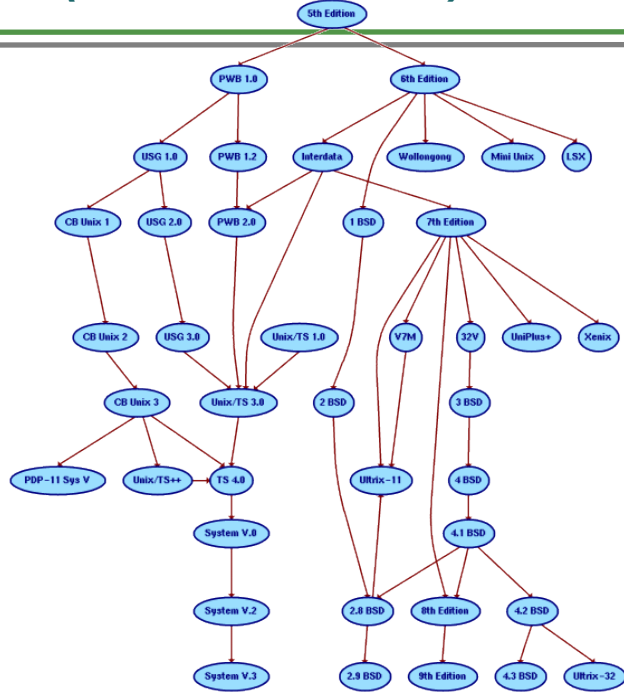
```
PROBLEM interval
direction: forward
carrier: dom
init_start: lift([->(dual(0),0)])
widening: wide
narrowing: narrow
```

## Debugging Specifications

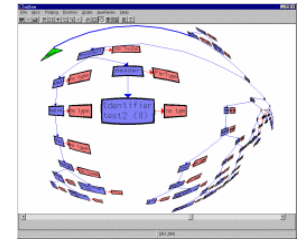
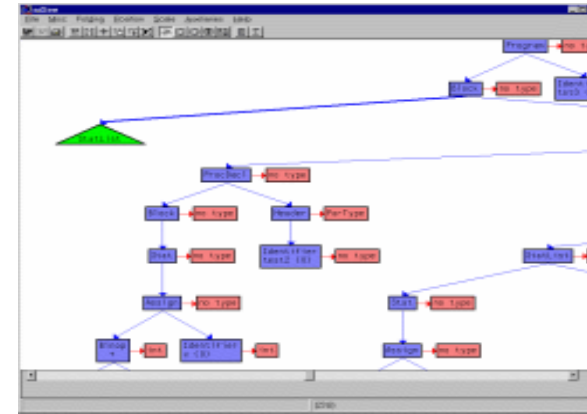
- ▶ Export to VCG file format (or aiSee)
- ▶ Many visualizations possible
- ▶ Specific ones for flow graphs
  - " Lattice values annotated without edges to the nodes or edges of the flow graph
  - " Zoom in/out
  - " Hiding relations
  - " Blocks of nodes as regions with different color



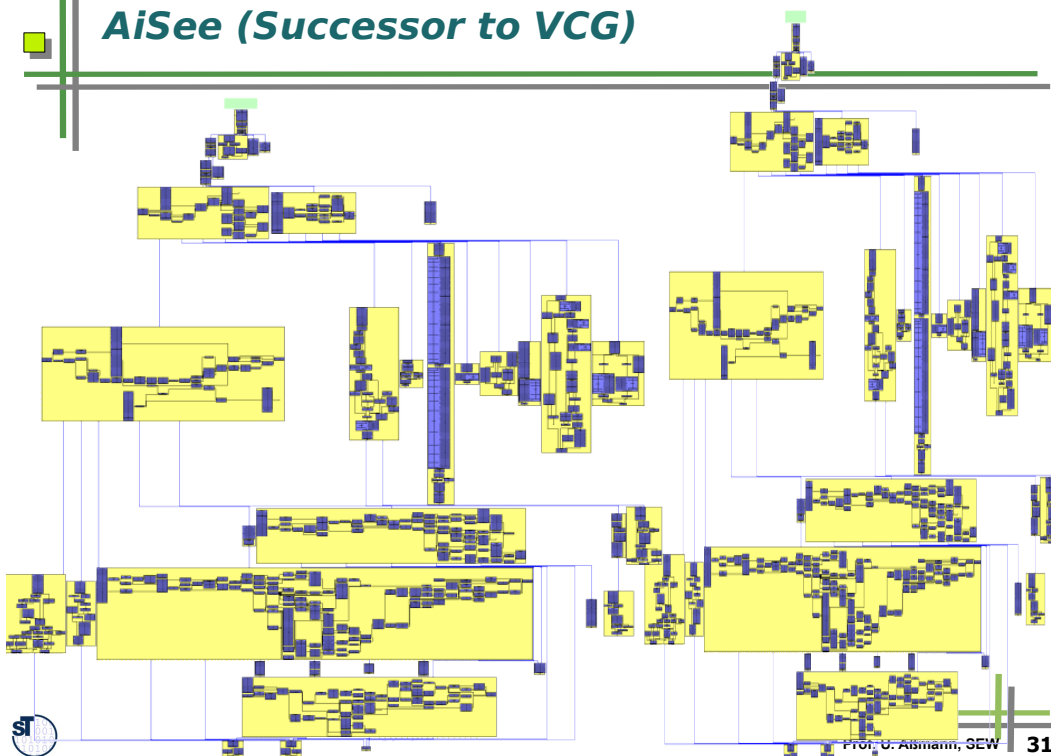
# AiSee (Successor to VCG)



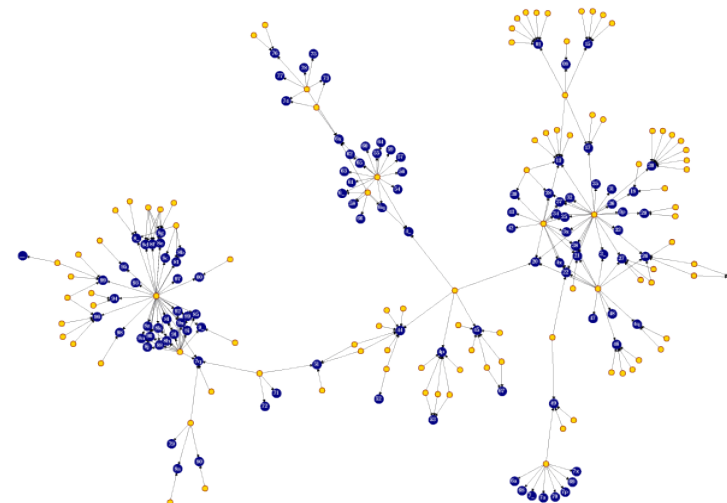
# AiSee (Successor to VCG)



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# AiSee (Successor to VCG)





## What have we learned?

- ▶ Interprocedural analysis can be done in several ways, spending different amount of resources, trading precision
- ▶ PAG is a tool to generate interprocedural analyzers
  - offering a specification language for lattices of abstract values
  - industrial strength
  - useful to specify many analyses, such as
    - classical data-flow analysis
    - cache analysis
    - heap analysis
    - alias analysis

*The End*

