Prof. Dr. Friedel Bolle Übungen Allokationstheorie

Prof. Dr. Friedel Bolle Übungen Allokationstheorie 2

From Nicholson: Microeconomic Theory.

## Aufgabe 5

Suppose there are only three goods  $(X_1, X_2, \text{ and } X_3)$  in an economy and that the excess demand functions for  $X_2$  and  $X_3$  are given by

$$ED_2 = -3P_2/P_1 + 2P_3/P_1 - 1$$

$$ED_3 = 4P_2/P_1 - 2P_3/P_1 - 2$$
.

- (a) Show that these functions are homogeneous of degree zero in P<sub>1</sub>, P<sub>2</sub>, and P<sub>3</sub>.
- **(b)** Use Walras' law to show that if  $ED_2 = ED_3 = 0$ ,  $ED_1$  also must be 0. Can you use Walras' law to calculate  $ED_1$ ?
- (c) Solve this system of equations for the equilibrium relative prices  $P_2/P_1$  and  $P_3/P_1$ . What is the equilibrium value for  $P_3/P_2$ ?

## Aufgabe 6

Suppose two individuals (Smith and Jones) each have 10 hours of labor to devote to producing either ice cream (X) or chicken soup (Y). Smith's utility function is given by

$$U_S = X^{.3}Y^{.7}$$

Where as Jones's is given by

$$U_J = X^{.5}Y^{.5}$$
.

The individuals do not care whether they produce X or Y, and the production function for each good is given by

$$X = 2 L$$

$$Y = 3 L$$

Where L is the total labor devoted to production of each good. Using this information.

- (a) What must the price ratio,  $P_X/P_{Y_1}$  be?
- **(b)** Given this price ratio how much X and Y will Smith and Jones demand? (Hint: Set the wage equal to one here.)
- **(c)** How should labor be allocated between X and Y to satisfy the demand calculated in part (b)?

## Aufgabe 7

Return to problem 6 and now assume that Smith and Jones conduct their exchanges in paper money. The total supply of such money is \$ 60, and each individual wishes to hold a stock of money equal to ½ of the value of transactions made per period.

- (a) What will the money wage rate be in this model? What will the nominal prices of X and Y be?
- **(b)** Suppose the money supply increases to \$ 90. How will your answers to part (a) change? Does this economy exhibit the classical dichotomy between its real and monetary sectors?